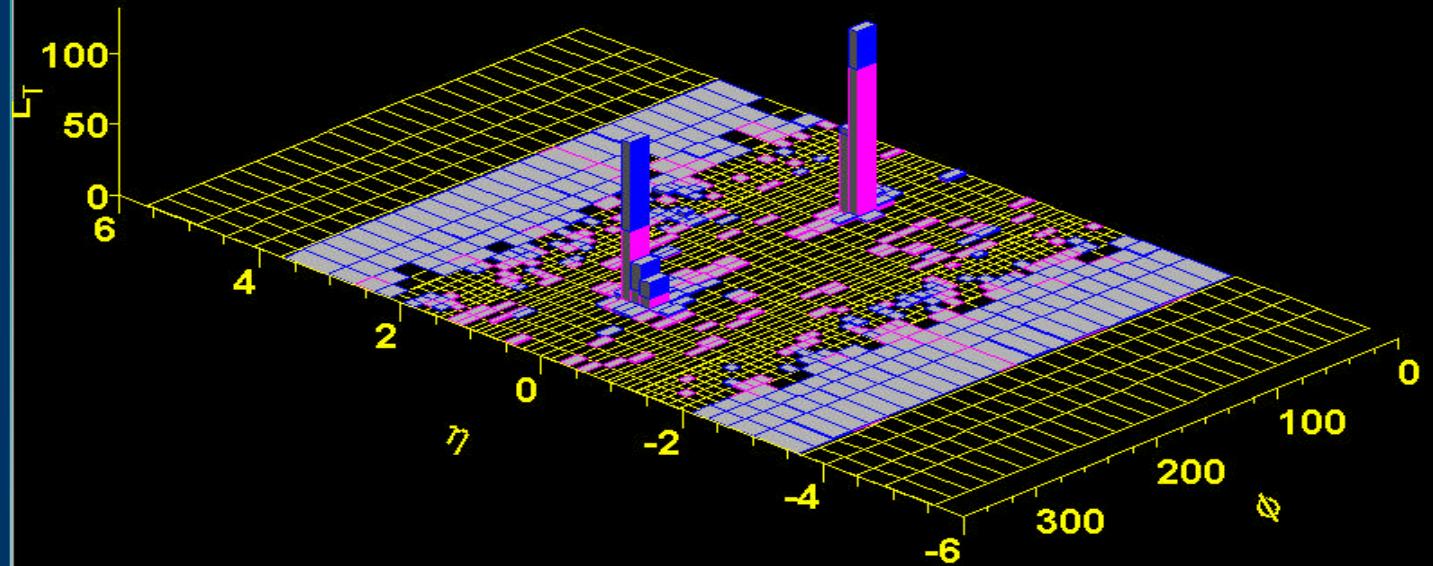


# **New SUSY Results with Missing Energy at CDF**

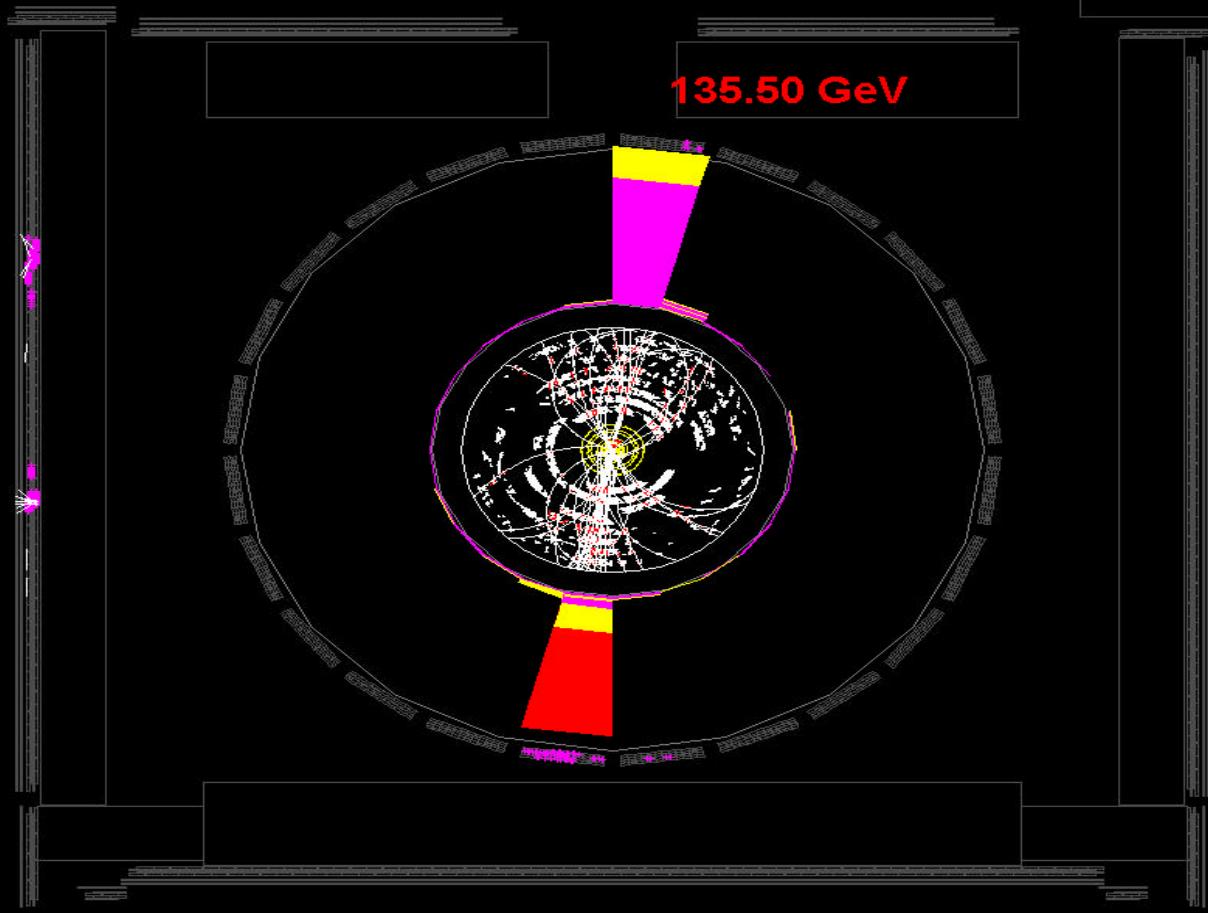
**Maria Spiropulu  
EFI/UofC  
Dec 14 2000**

BNL Particle Physics Seminar

Event : 7973 Run : 102837 EventType : 0 TRIG: Unpr. - Fired bits: 1,41,14,15,21,22,23,24,26,30, Pr. - Fired bits: 22, , Myron mode 0



Event : 7973 Run : 102837 EventType : 0 TRIG: Unpr. - Fired bits: 1,41,14,15,21,22,23,24,26,30, Pr. - Fired bits: 22, , Myron mode 0



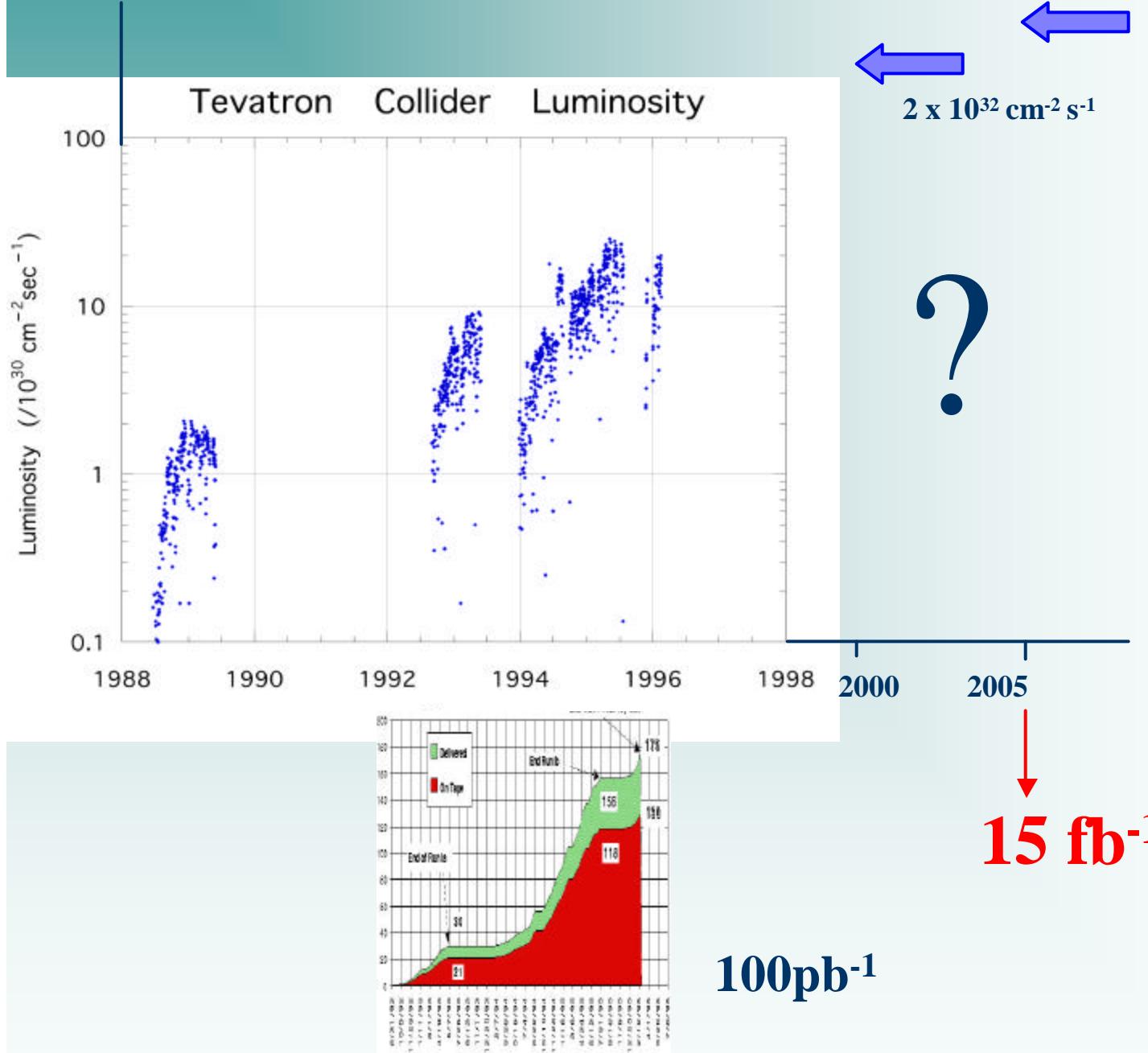
# Tevatron

Protons run the 4 mile ring  
about 50000/sec



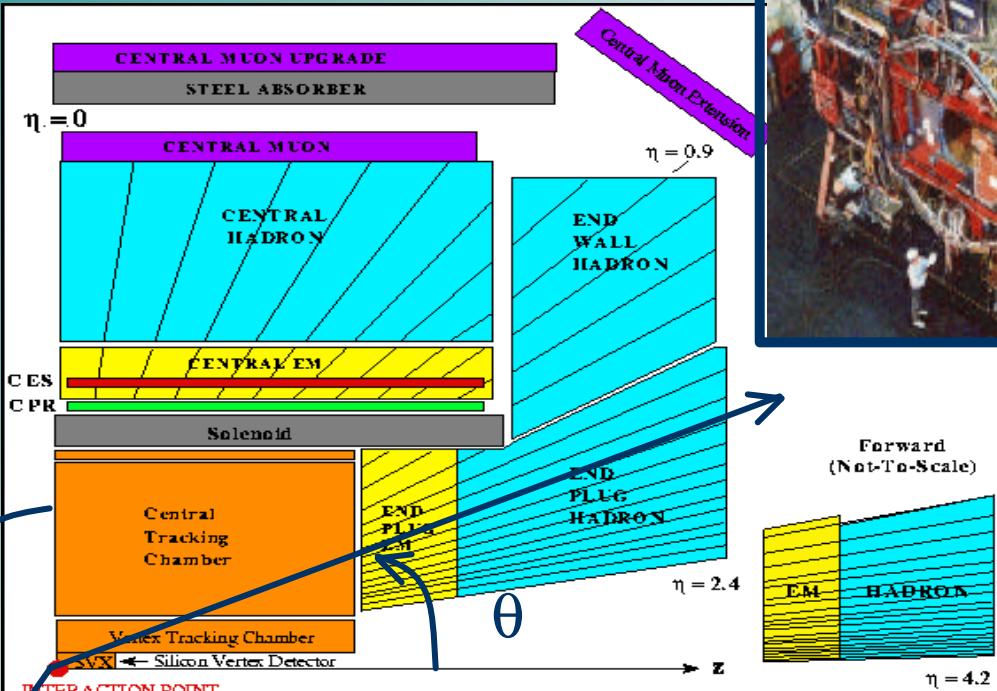
# Tevatron

## Discovery of top, $B_c$



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# Missing $E_T$



$$\vec{E}_T + \sum \vec{E}_T = \vec{0}$$

$$h = -\log(\tan \frac{q}{2})$$

$$\left( \begin{array}{l} E^x_T = -\sum_i E^i_T \cos(q_i) \\ E^y_T = -\sum_i E^i_T \sin(q_i) \end{array} \right)$$

$$-4.2 < h < 4.2$$

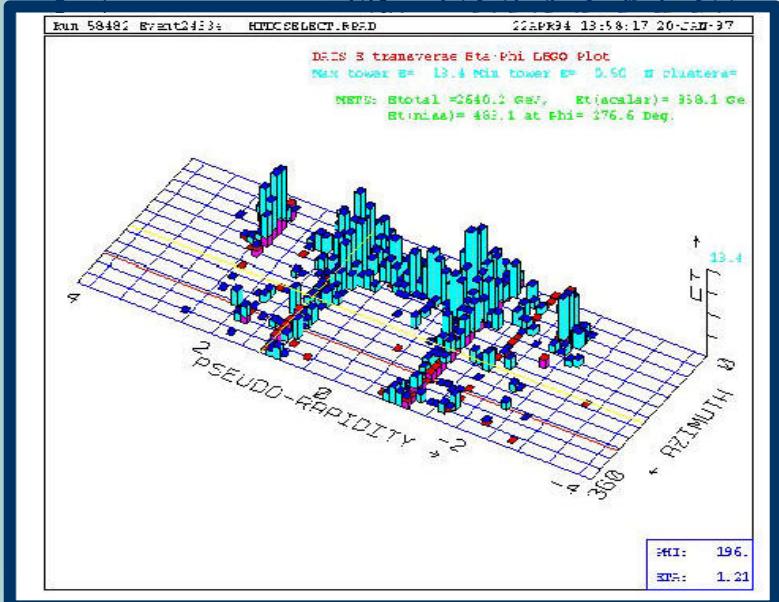
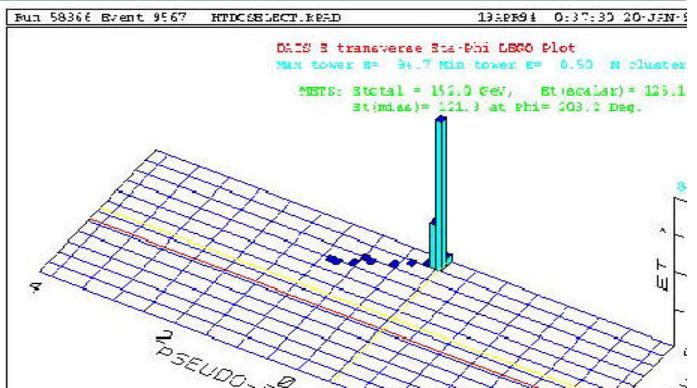
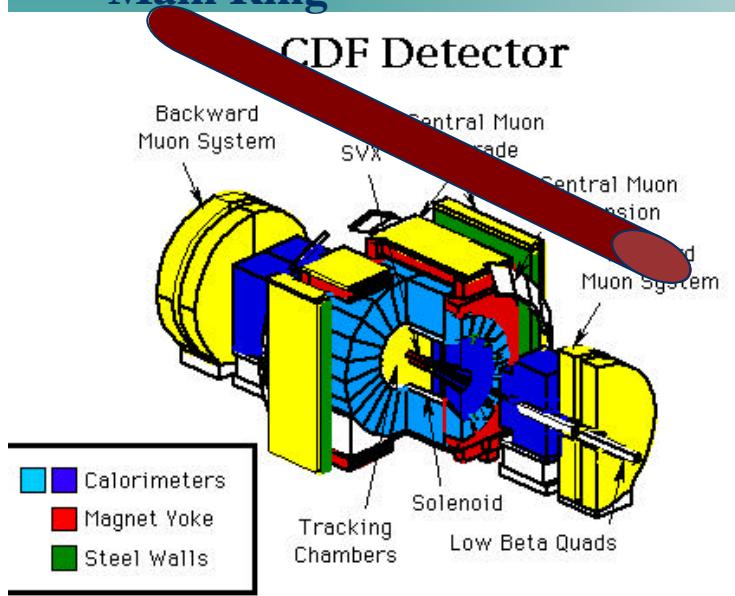
Missing Energy provides the classic R-parity conserving SUSY signature ( $R=(-1)^{3B+L+2S}$ ) but appears in many other phenomenological paradigms

**MET + 3 jets (squarks, gluinos), MET + c-tagged jets (scalar top)  
MET + b-tagged jets (scalar bottom, Higgs), MET + monojet (gravitino/raviton) MET + photons (gravitino)**

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# Fake Missing Energy

## Main Ring

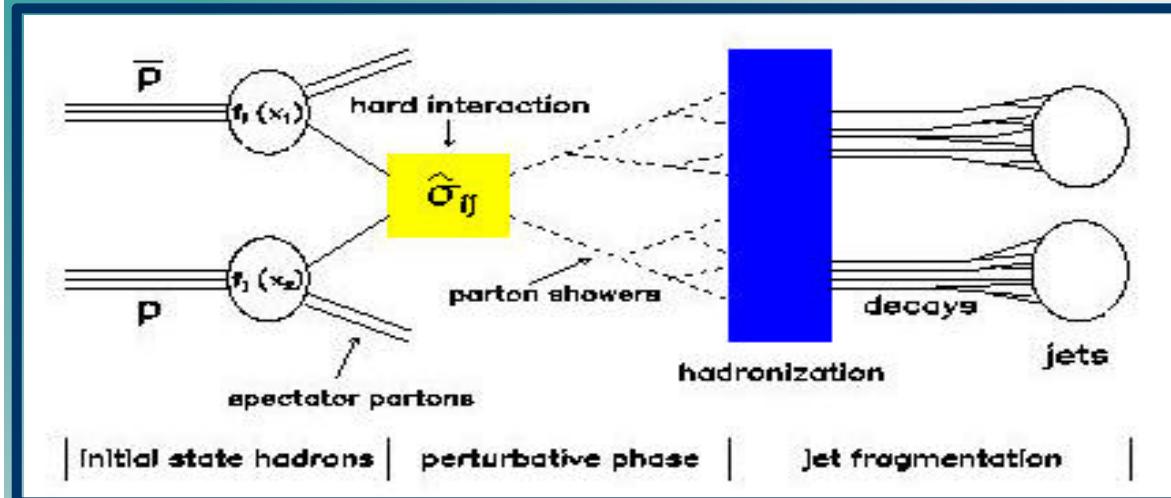


## INSTRUMENTAL SOURCES OF MISSING ENERGY

MAIN RING  
DETECTOR MALFUNCTIONS/NOISE  
COSMICS

These are eliminated with a set of  
timing and good jet quality  
requirements

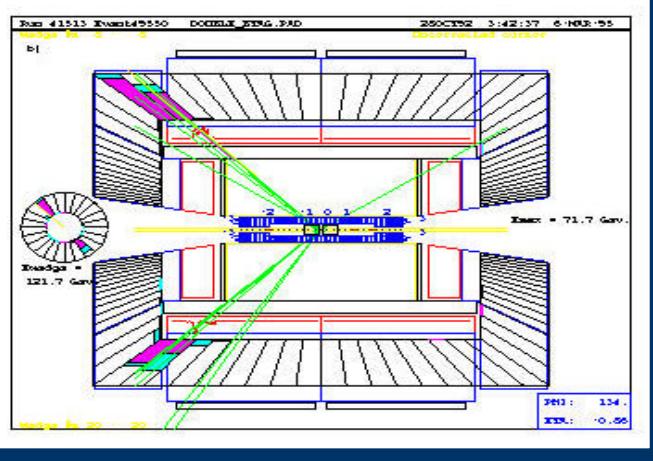
# Jets



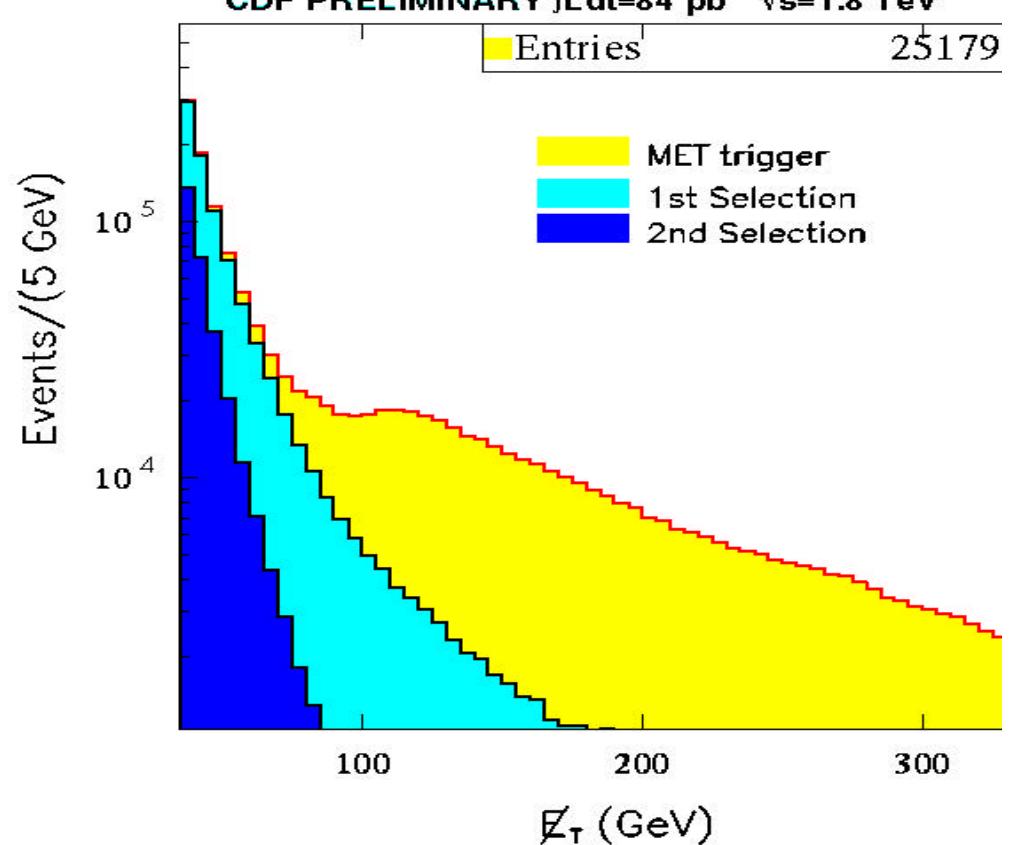
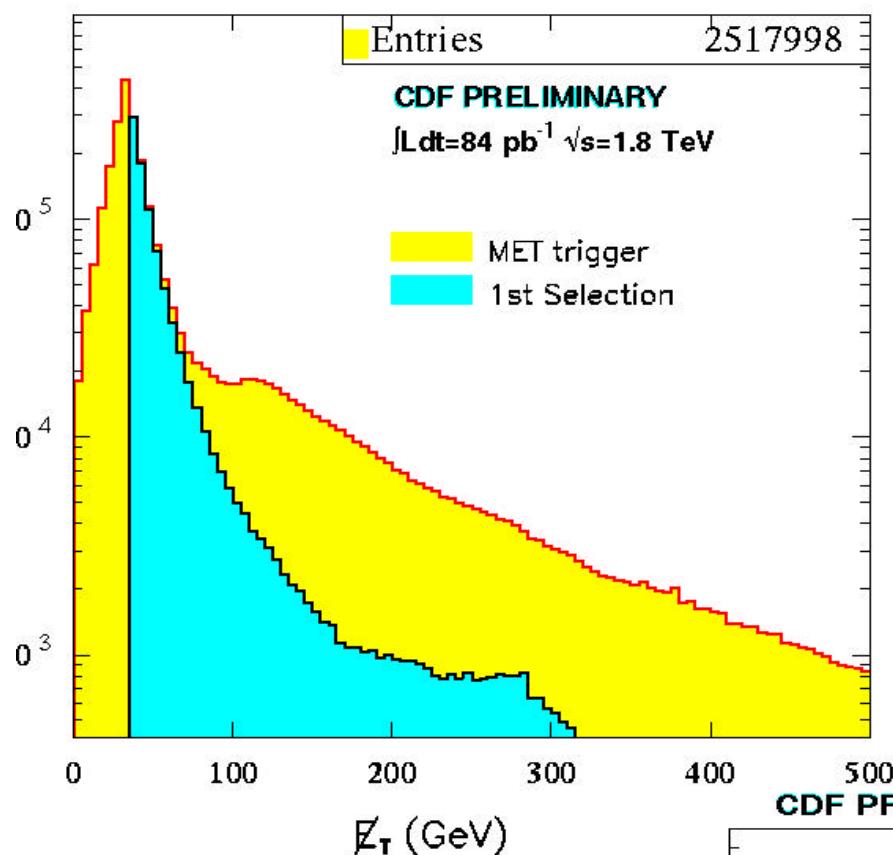
Jet variables used for  
“good jetiness” criteria

\* Charge Fraction (CH)

\* EM fraction (EMF)



# DATA PRE-SELECTION

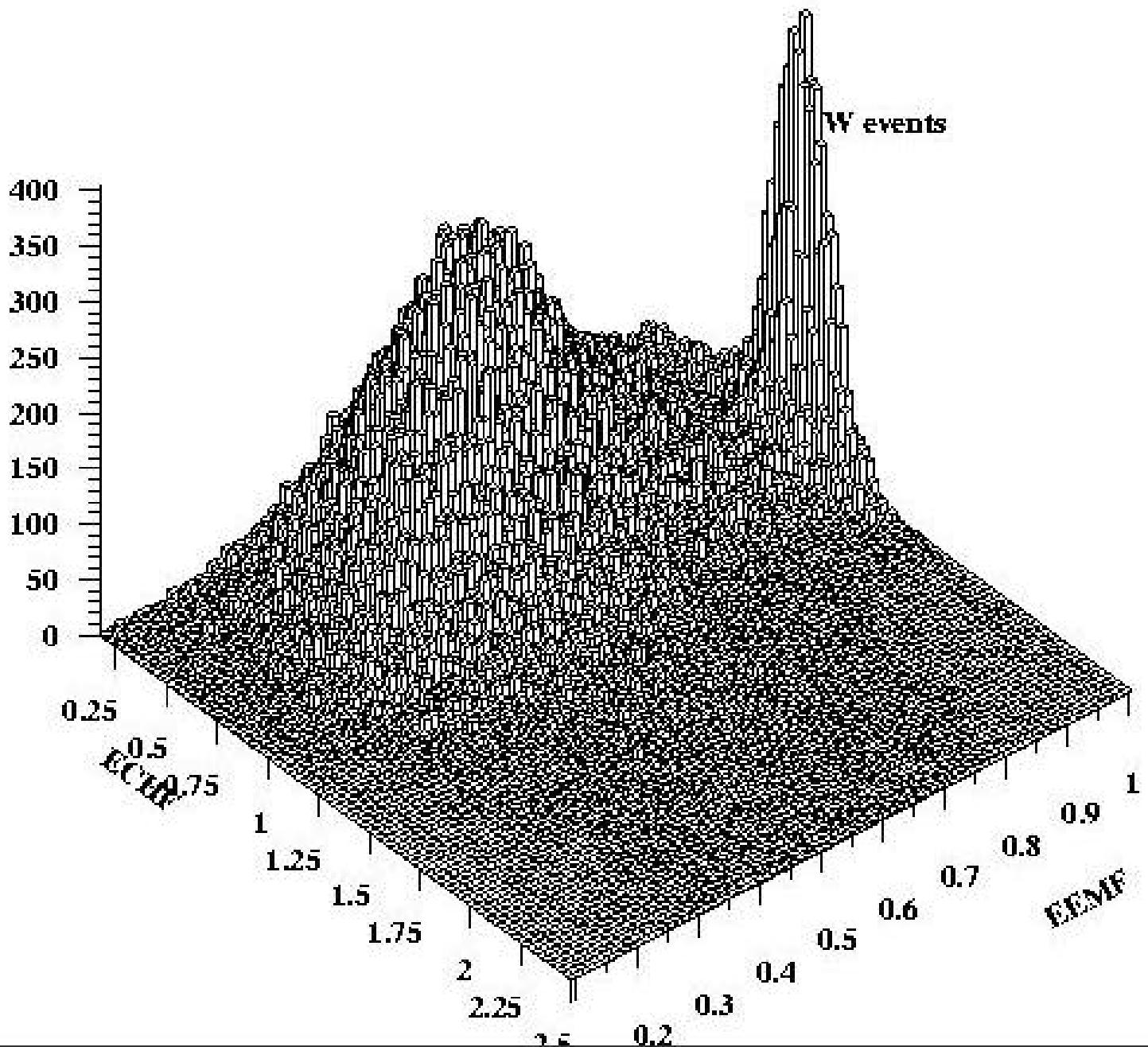


# ATA PRE-SELECTION

of 2517998 events	Number of events fail
$E_T$	1123734
Out-Time	506241
Stage 1 = $E_T \oplus$ Out-Time	1625603
Total passing Stage 1	892395

of 892394 events	Number of Events Fail
1 central jet	372978
EEMF	24992
ECHF	591449
Total passing Stage 2	300945

# See the W's !!



# MISSING ENERGY + MULTIJET STANDARD MODEL COMPONENT

$Z(\rightarrow ll) + \text{jets}$

$W(\rightarrow ln) + \text{jets}$

$t\bar{t}$ , single top

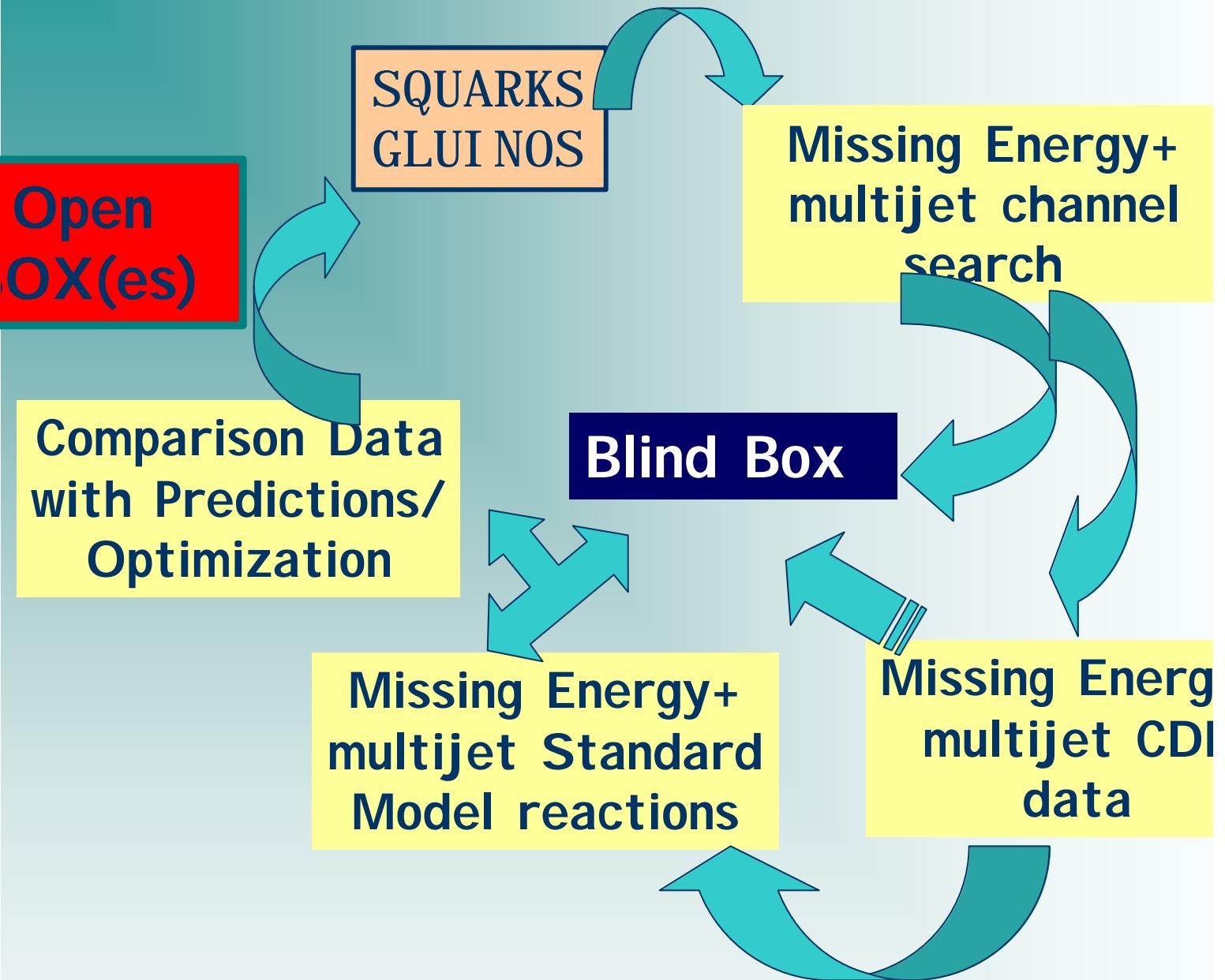
Di boson

QCD multijet

E  
W  
K

Note: The missing energy  
is a QCD sample

# SEARCH OUTLINE



## SUPERSYMMETRY

## Fermi on♦Boson

Solves the “hierarchy problem”

Apparently Unifies the three gauge couplings

$$R = (-1)^{3(B-L)+2S} \quad +1 \text{ (SM particles)} \\ -1 \text{ SUSY particles}$$

If R-parity is conserved

- sparticles are produced in pairs and eventually decay to the

Lightest

SUSY Particle (LSP)

- the LSP is stable and weakly interacting

$\Leftrightarrow$  missing energy signature

LSP is a good candidate for dark matter

Name	Spin	$R$	Mass Eigenstates	Gauge Eigenstates
Higgs bosons	0	+1	$h^0 \ H^0 \ A^0 \ H^\pm$	$H_u^0 \ H_d^0 \ H_u^+ \ H_d^-$
squarks	0	-1	$\tilde{u}_L \ \tilde{u}_R \ \tilde{d}_L \ \tilde{d}_R$ $\tilde{s}_L \ \tilde{s}_R \ \tilde{c}_L \ \tilde{c}_R$ $\tilde{t}_1 \ \tilde{t}_2 \ \tilde{b}_1 \ \tilde{b}_2$	$\tilde{u}_L \ \tilde{u}_R \ \tilde{d}_L \ \tilde{d}_R$ $\tilde{s}_L \ \tilde{s}_R \ \tilde{c}_L \ \tilde{c}_R$ $\tilde{t}_L \ \tilde{t}_R \ \tilde{b}_L \ \tilde{b}_R$
sleptons	0	-1	$\tilde{e}_L \ \tilde{e}_R \ \tilde{\nu}_e$ $\tilde{\mu}_L \ \tilde{\mu}_R \ \tilde{\nu}_\mu$ $\tilde{\tau}_1 \ \tilde{\tau}_2 \ \tilde{\nu}_\tau$	$\tilde{e}_L \ \tilde{e}_R \ \tilde{\nu}_e$ $\tilde{\mu}_L \ \tilde{\mu}_R \ \tilde{\nu}_\mu$ $\tilde{\tau}_L \ \tilde{\tau}_R \ \tilde{\nu}_\tau$
neutralinos	1/2	-1	M1 $\tilde{\chi}_1^0 \ \tilde{\chi}_2^0 \ \tilde{\chi}_3^0 \ \tilde{\chi}_4^0$	$\tilde{B}^0 \ \tilde{W}^0 \ \tilde{H}_u^0 \ \tilde{H}_d^0$
charginos	1/2	-1	M2 $\tilde{\chi}_1^\pm \ \tilde{\chi}_2^\pm \ \tilde{\chi}_3^\pm$	$\tilde{W}^\pm \ \tilde{H}_u^+ \ \tilde{H}_d^-$
gluino	1/2	-1	M3 $\tilde{g}$	$\tilde{g}$
gravitino/ goldstino	3/2	-1	$\tilde{G}$	$\tilde{G}$

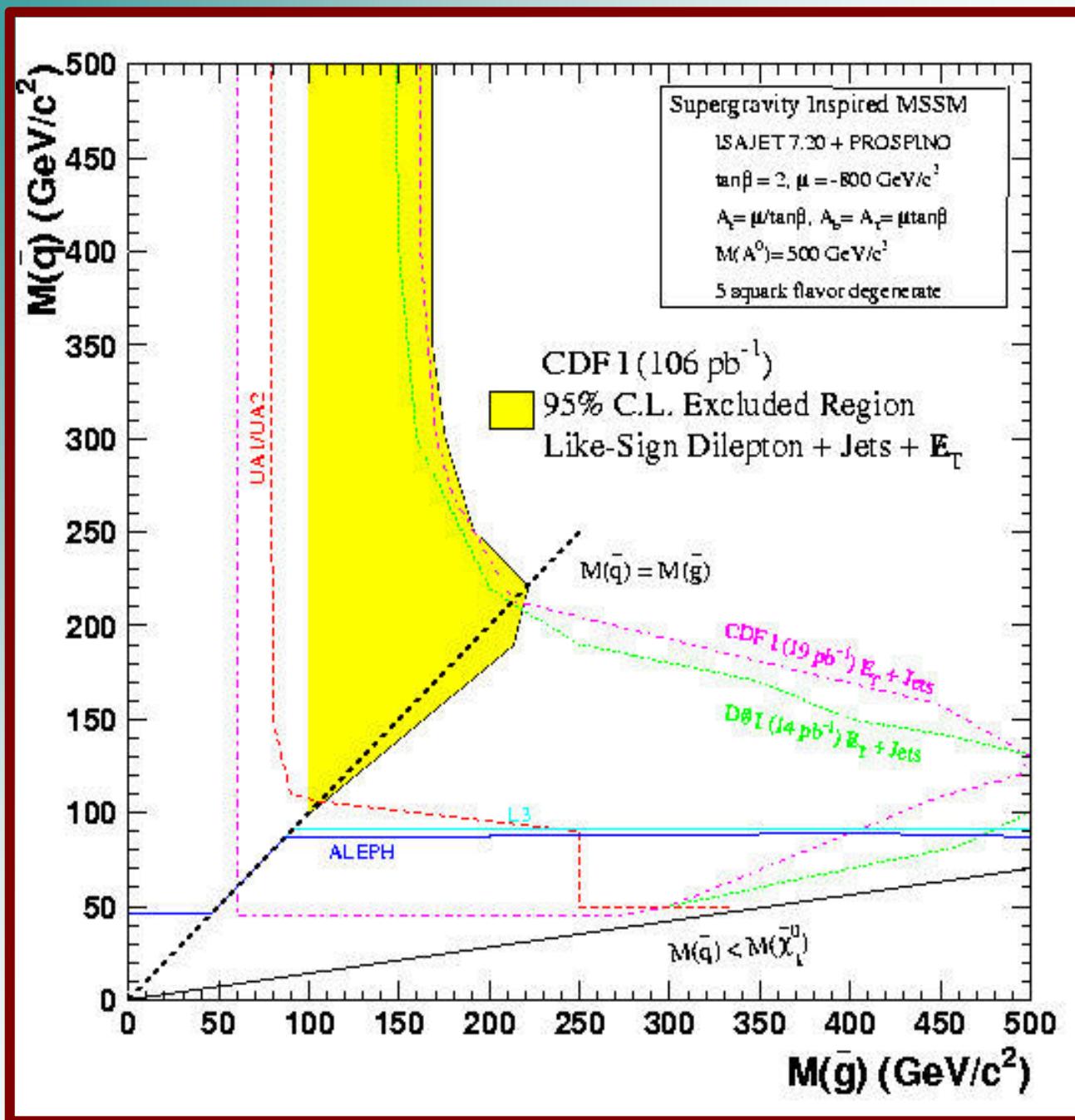
# The Super-Models

## SSM

$m_{\tilde{g}}$	gluino	mass	
$\mu$	Higgs	mass	parameter
$\tan \beta$	$\frac{v_2}{v_1}$		
A	mass	of CP - odd	Higgs
$m_{\tilde{l}}, m_{\tilde{q}}$	slepton	and squark	masses
$A_{\tilde{l}}, A_{\tilde{q}}$	trilinear		couplings

## SUGRA

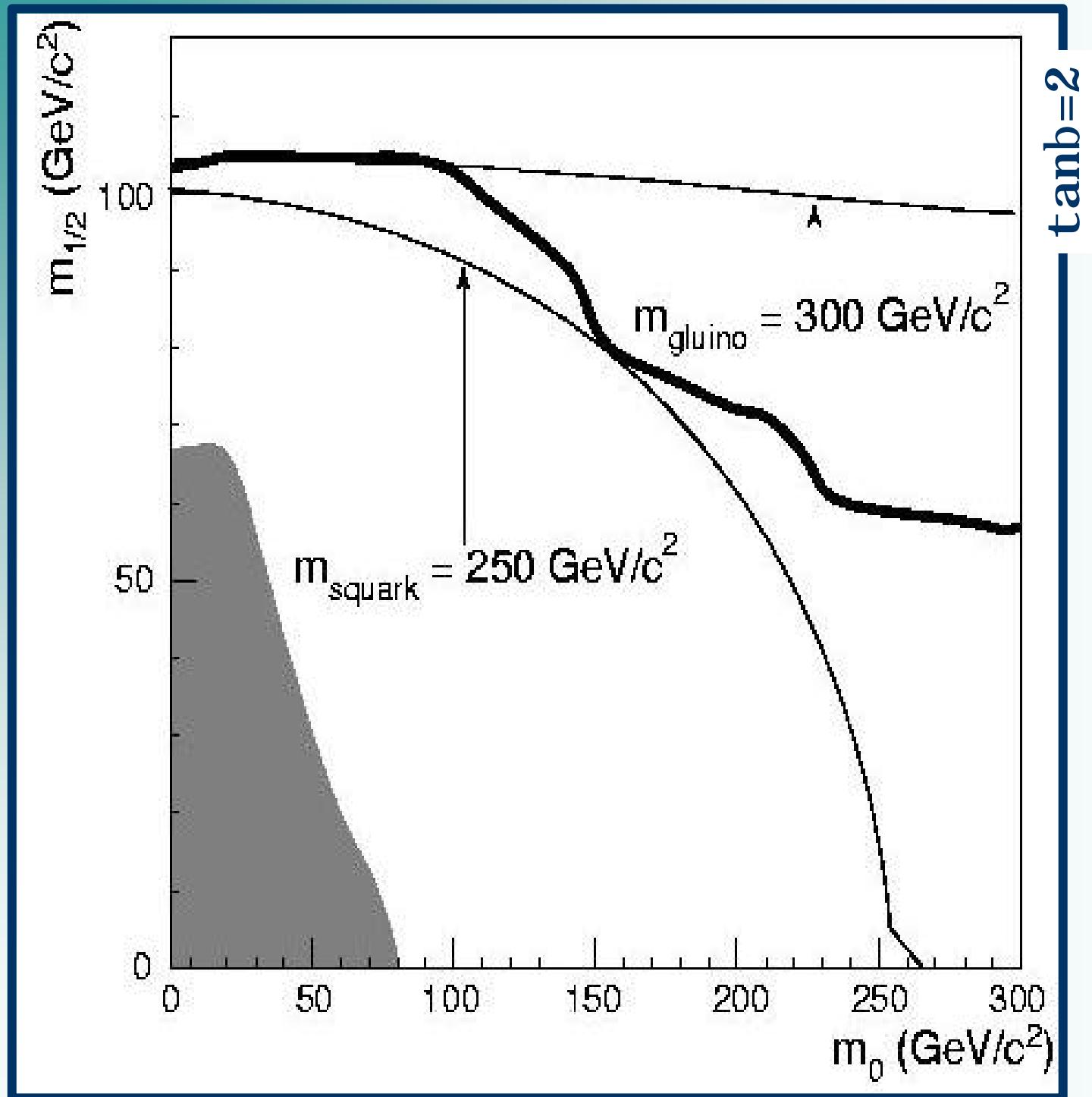
$M_{1/2}$	unified	gaugino	masses
$M_0$	unified	scalar	masses
$\tan \beta$	$\frac{v_2}{v_1}$		
$A_0$	unified	trilinear	couplings
sign $\mu$			



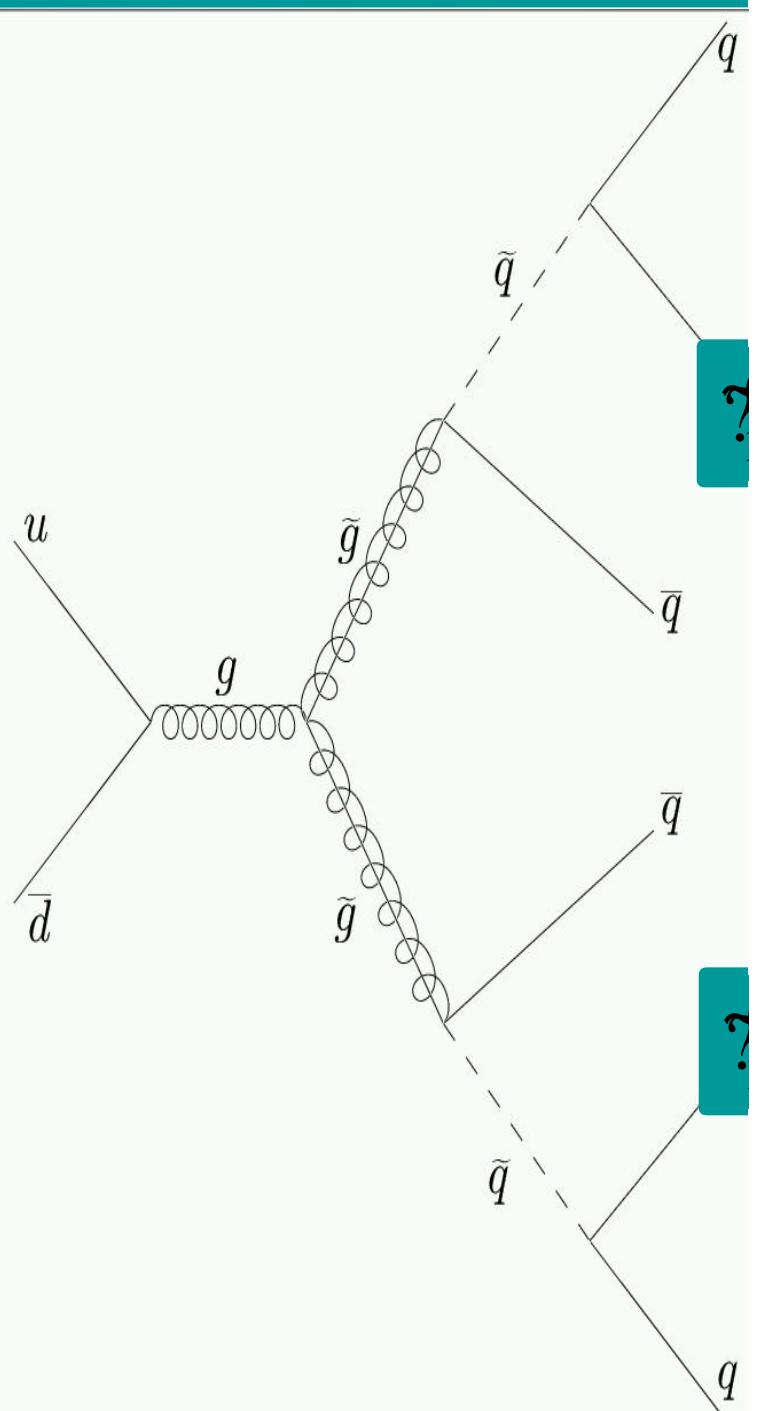
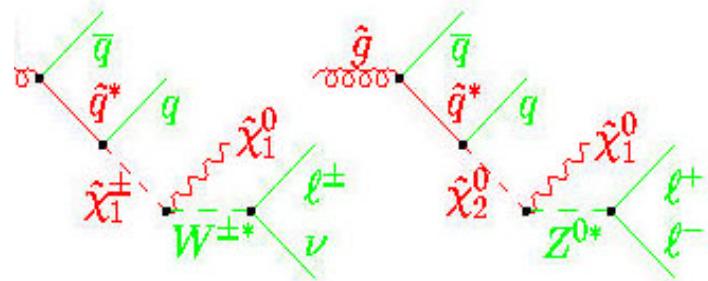
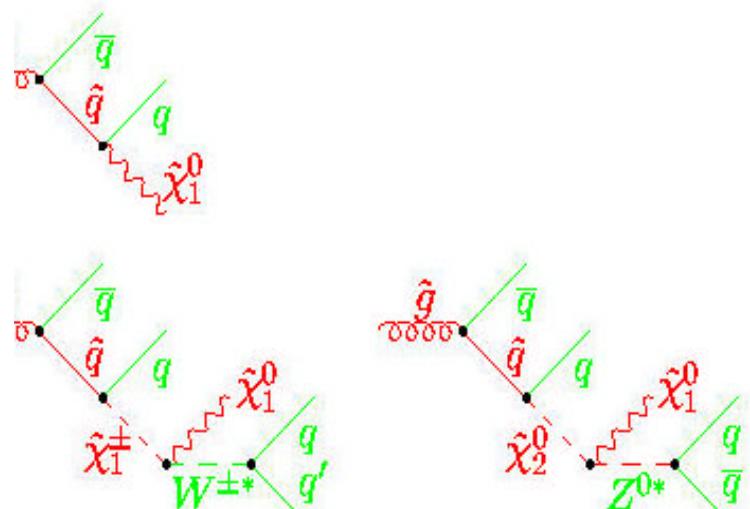
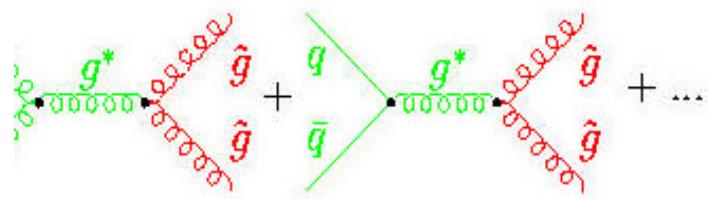
## Present Results

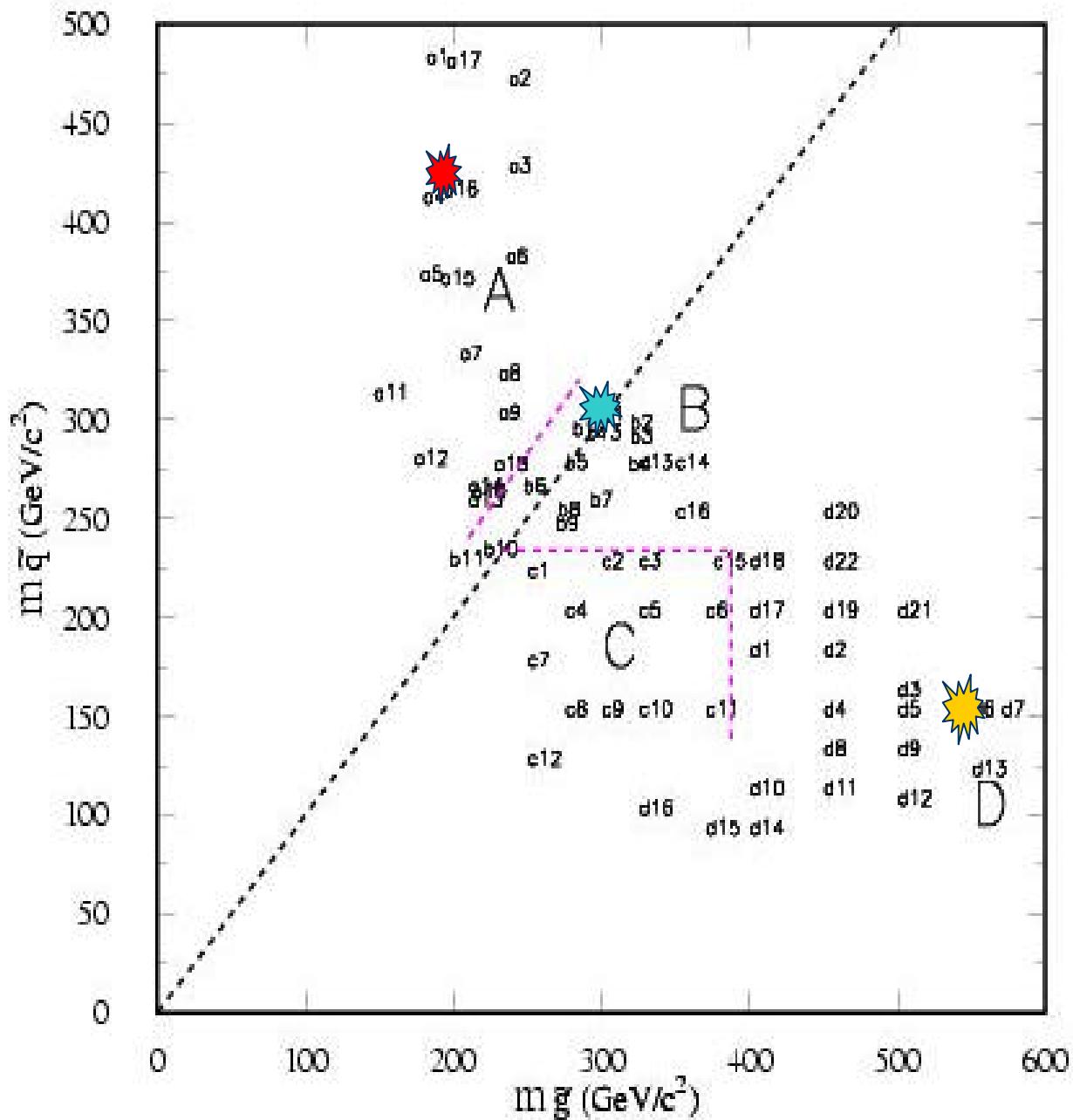
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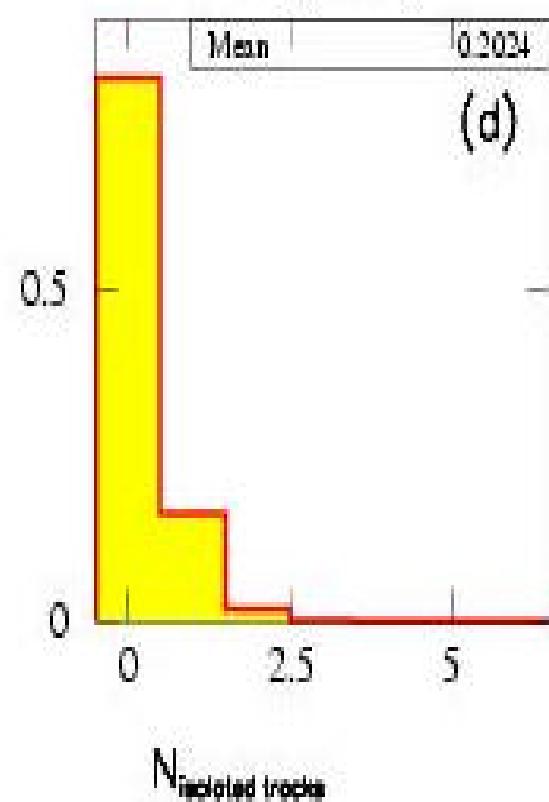
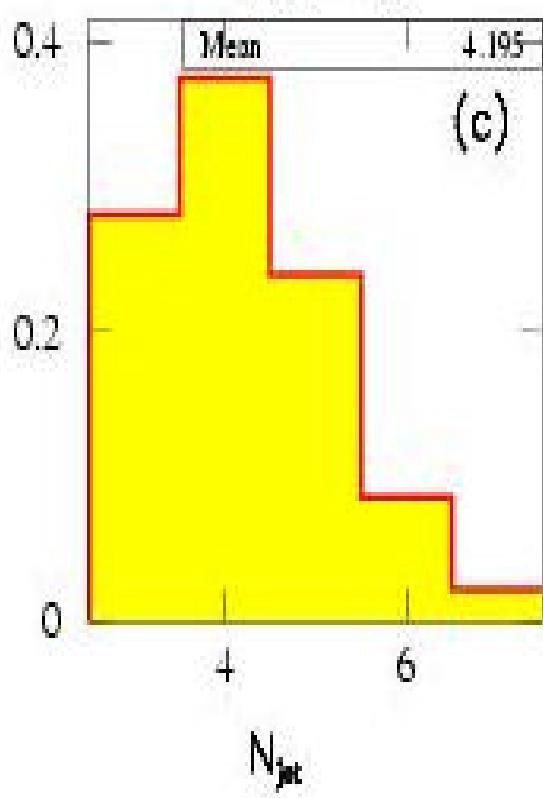
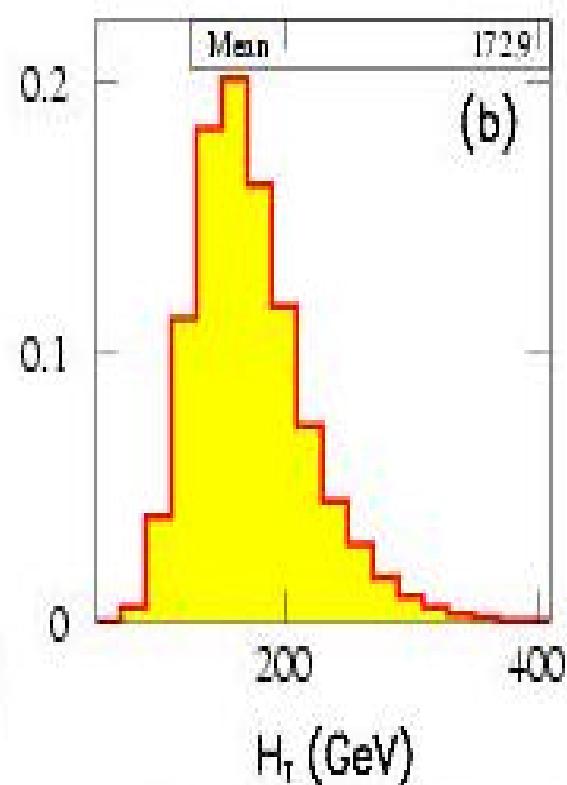
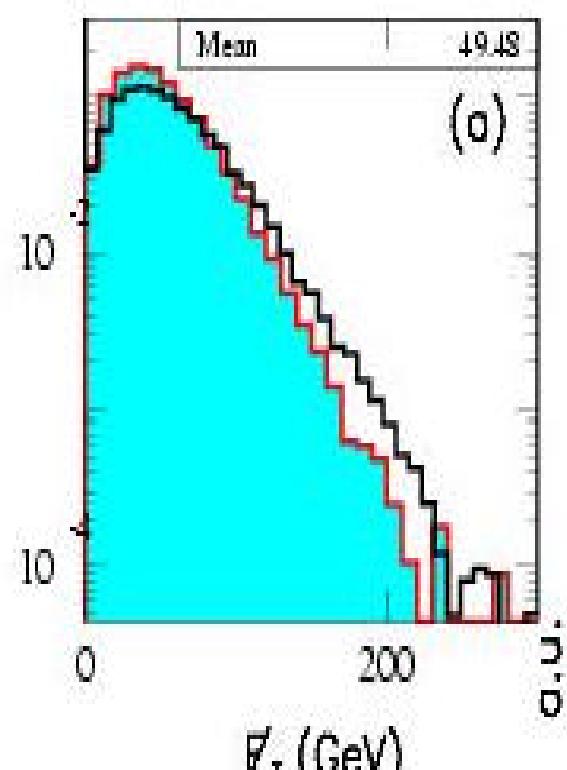
# mSUGRA DØ result

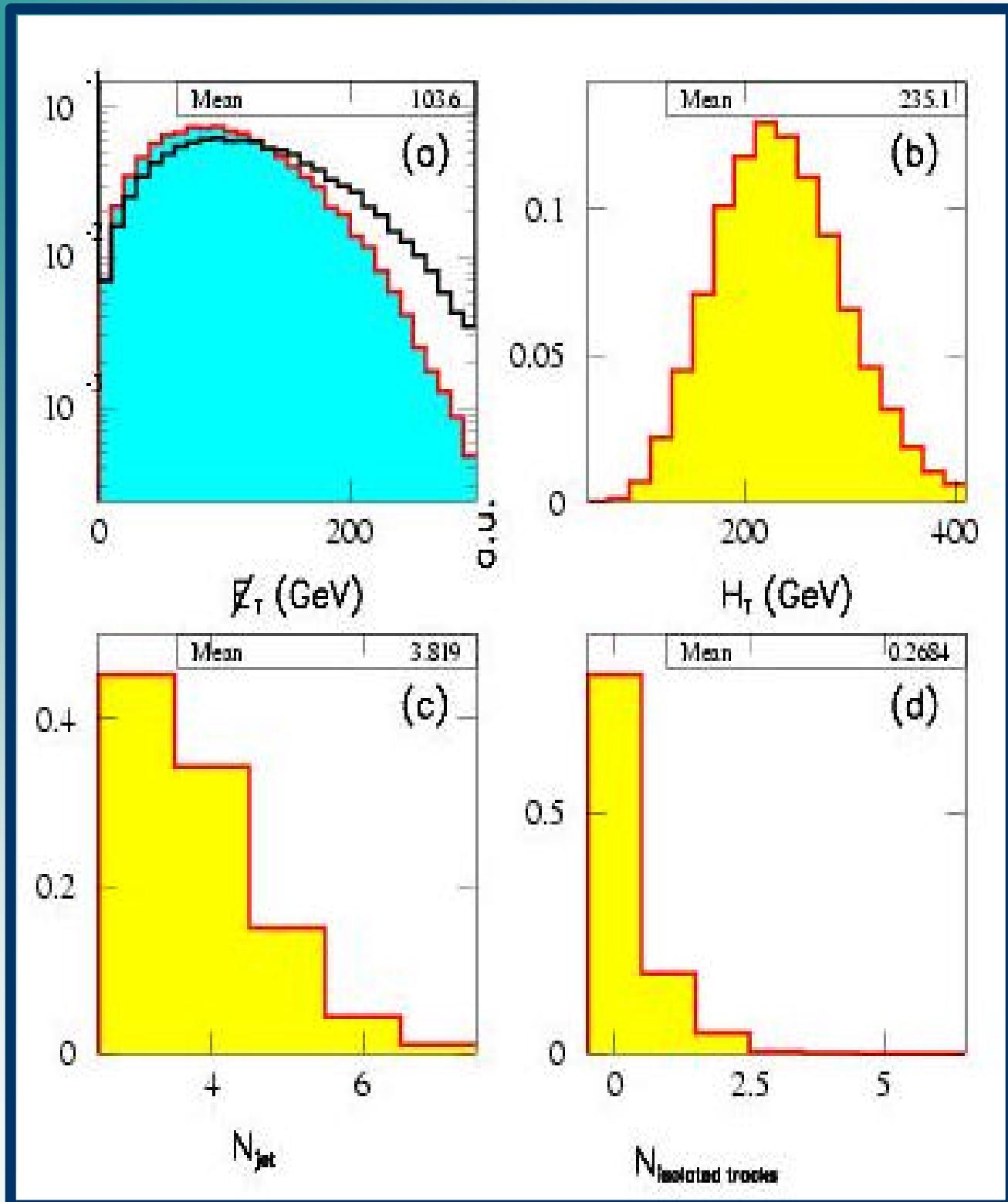


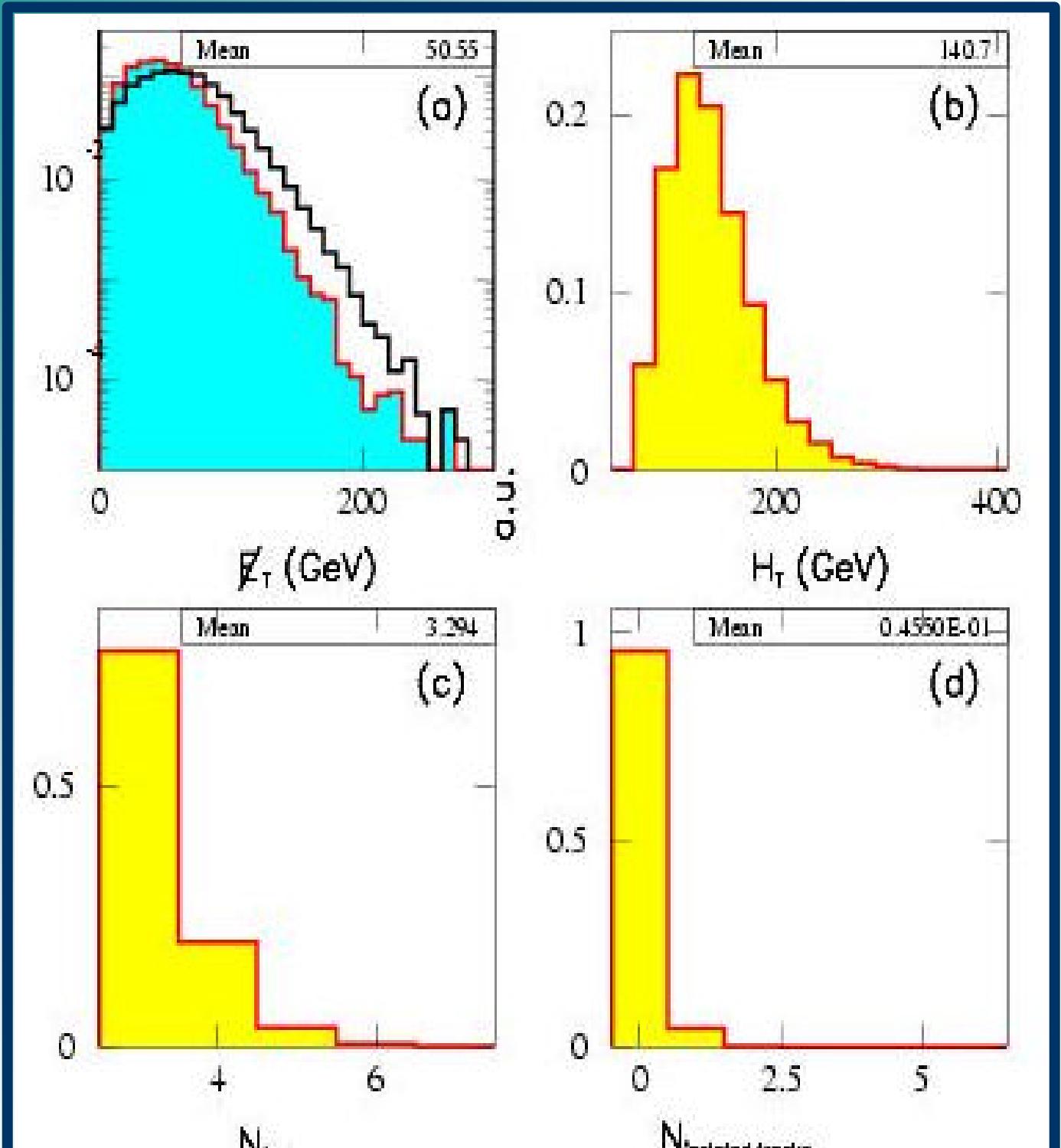
# Production/Decay Graphs











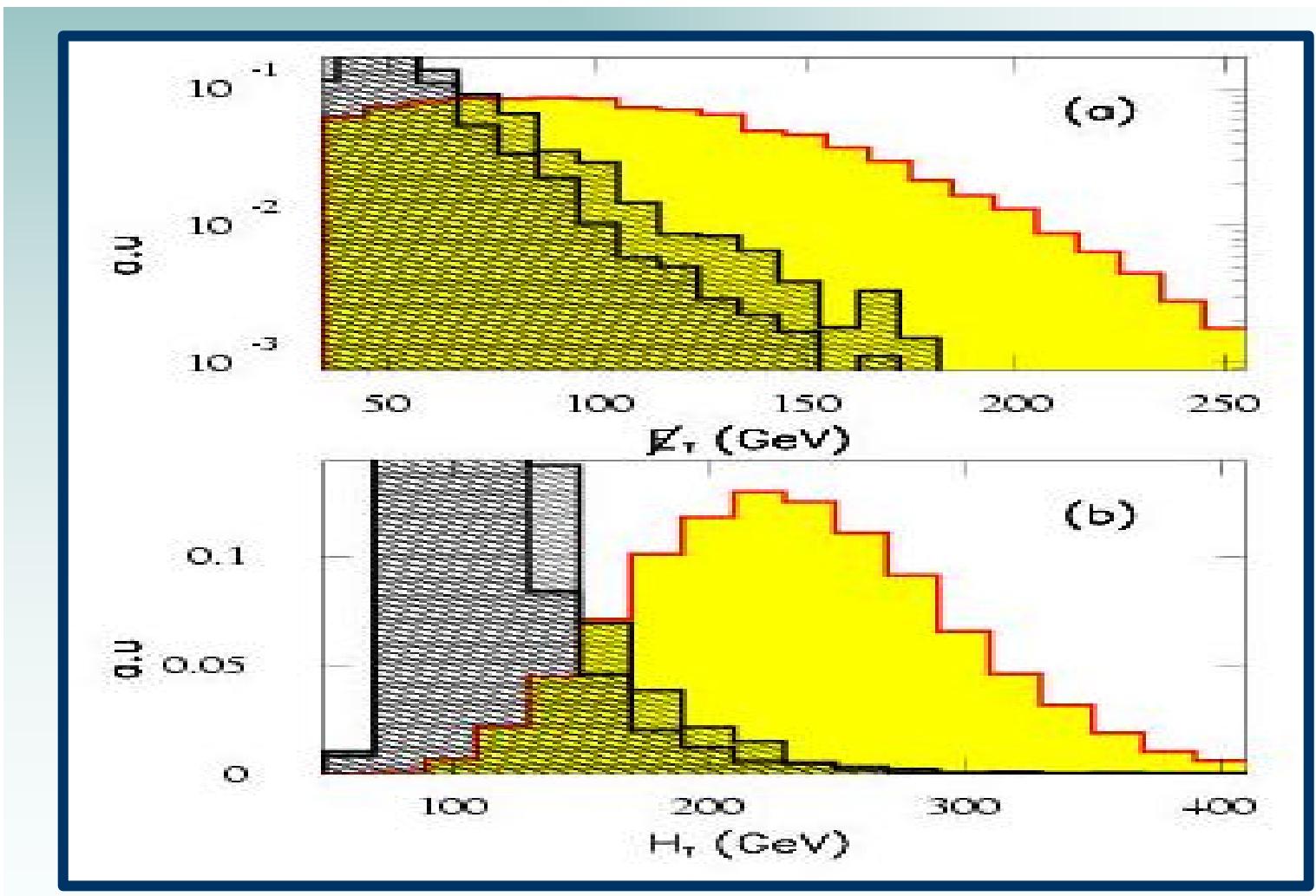
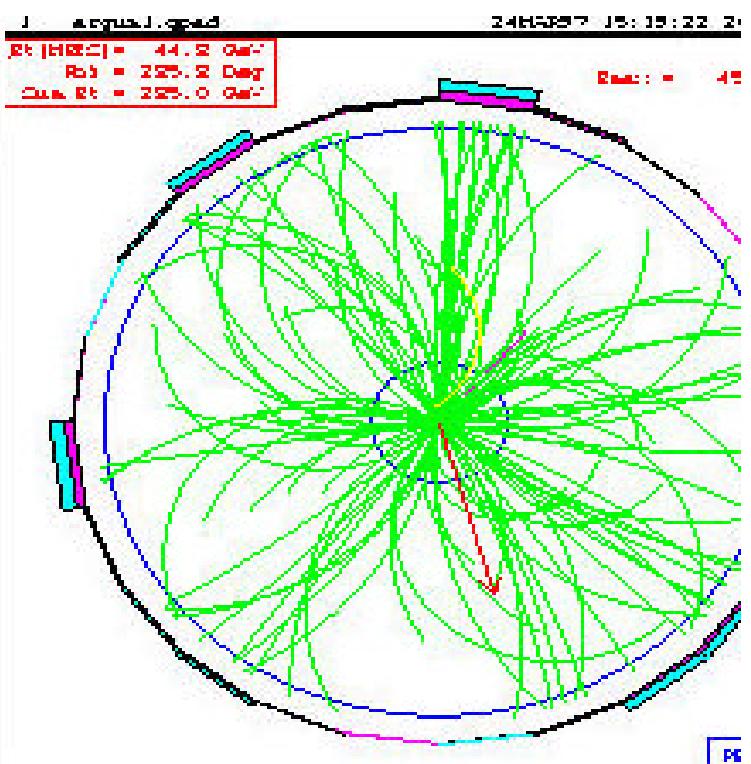
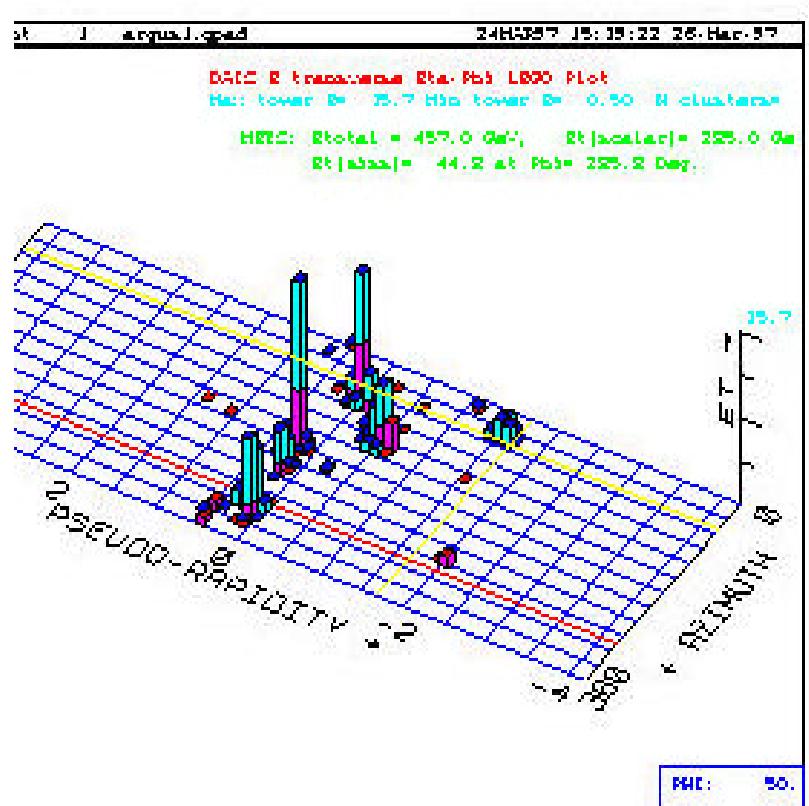
# ANALYSIS DRIVING VARIABLES

the Missing Transverse Energy  $E_T$

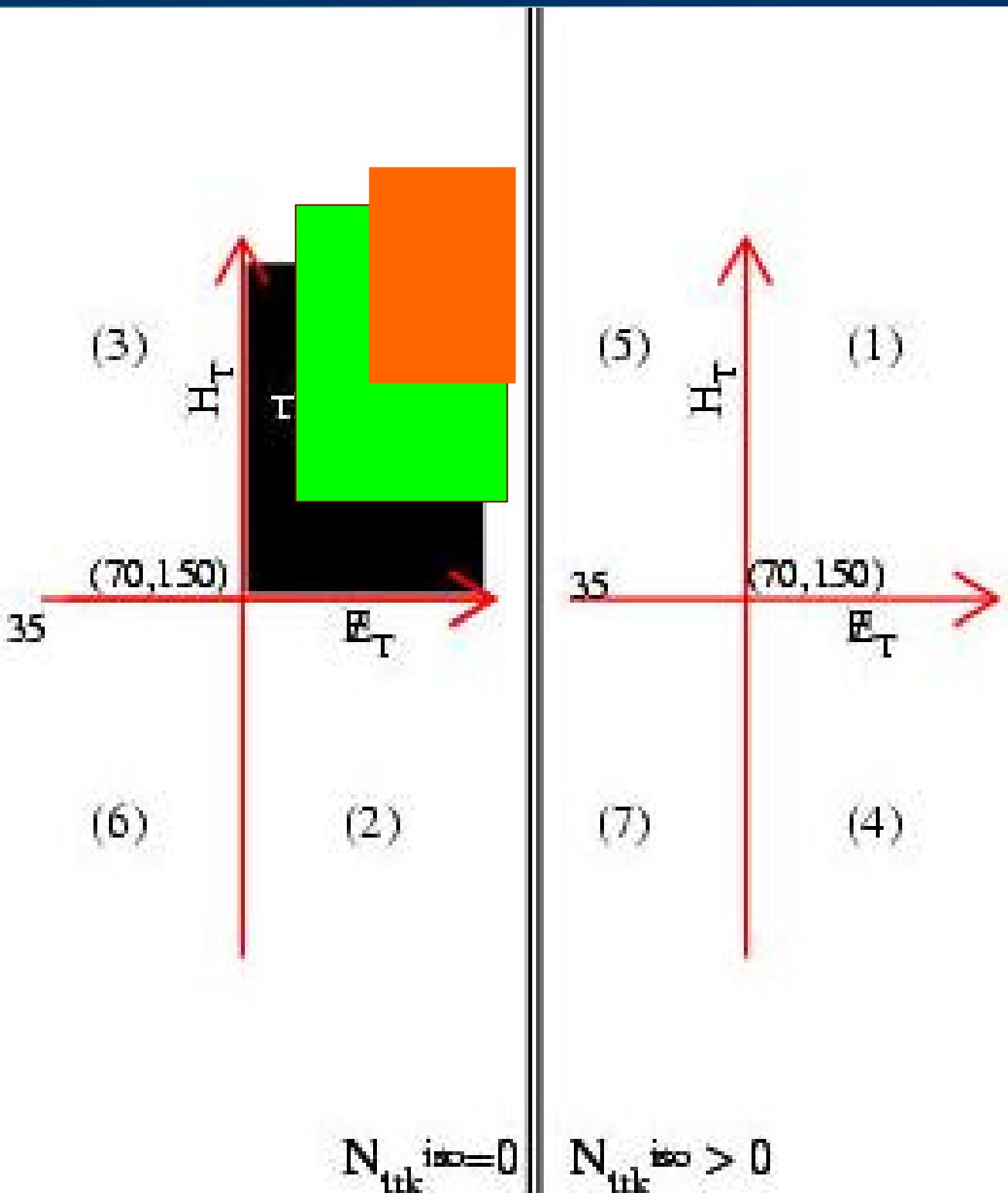
the Number of Jets  $N_{\text{jets}}$

$E_T(2^{\text{nd jet}}) + E_T(3^{\text{rd jet}}) + E_T$   $H_T$

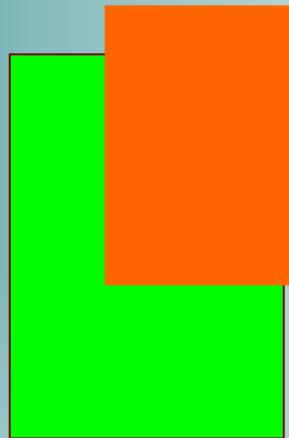
the Number of isolated tracks  $N_{\text{trk}}^{\text{is}}$



# "The BOX"



# **"The BOX"**



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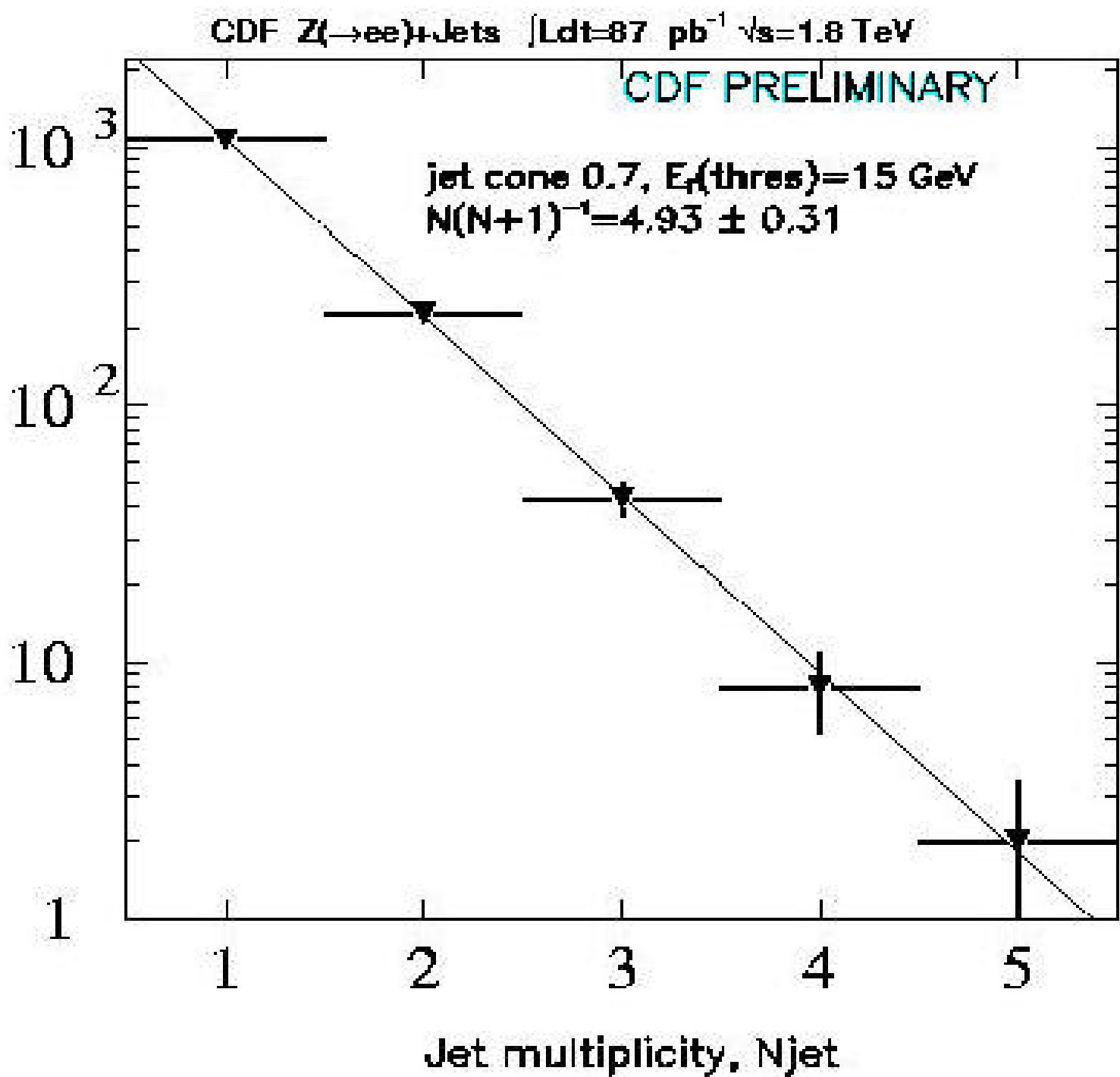
# $Z/W + \geq N$ jets ( $N=2, 3$ )

For this analysis the  $Z/W + N$  jet predictions are normalized to the Zee+O 2 jet CDF data using:

$$= \frac{N}{N+1} \left| \begin{array}{l} \text{DATA} \\ \text{to normalize the 3 jet} \\ \text{predictions using the 2 jet data} \end{array} \right.$$

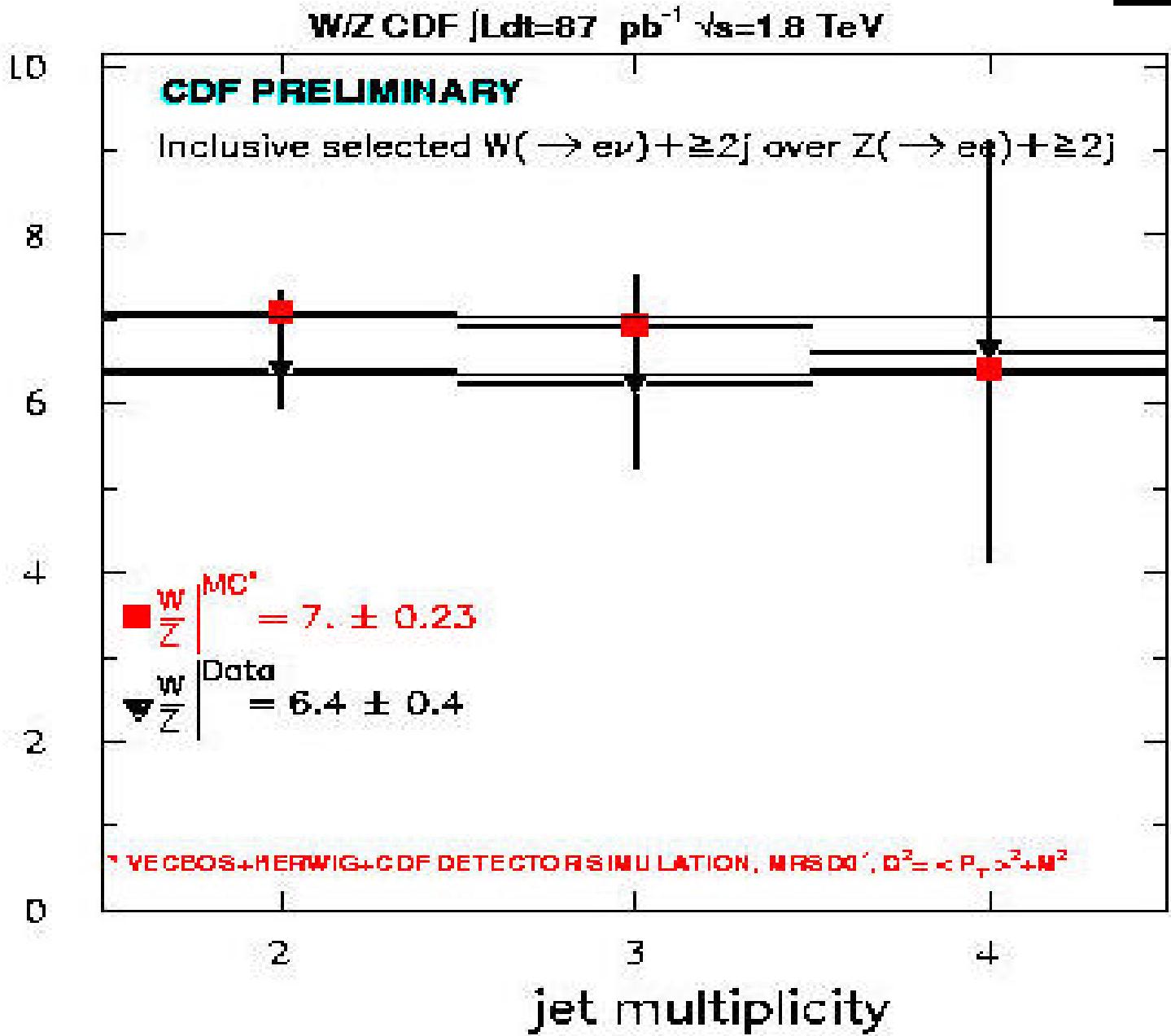
$$, = \frac{W}{Z} \left| \begin{array}{l} \text{MC} \\ \text{to normalize the W predictions} \\ \text{using the Z data} \end{array} \right.$$

# Ratios in the normalization: $L_{ds}/dN_{je}$

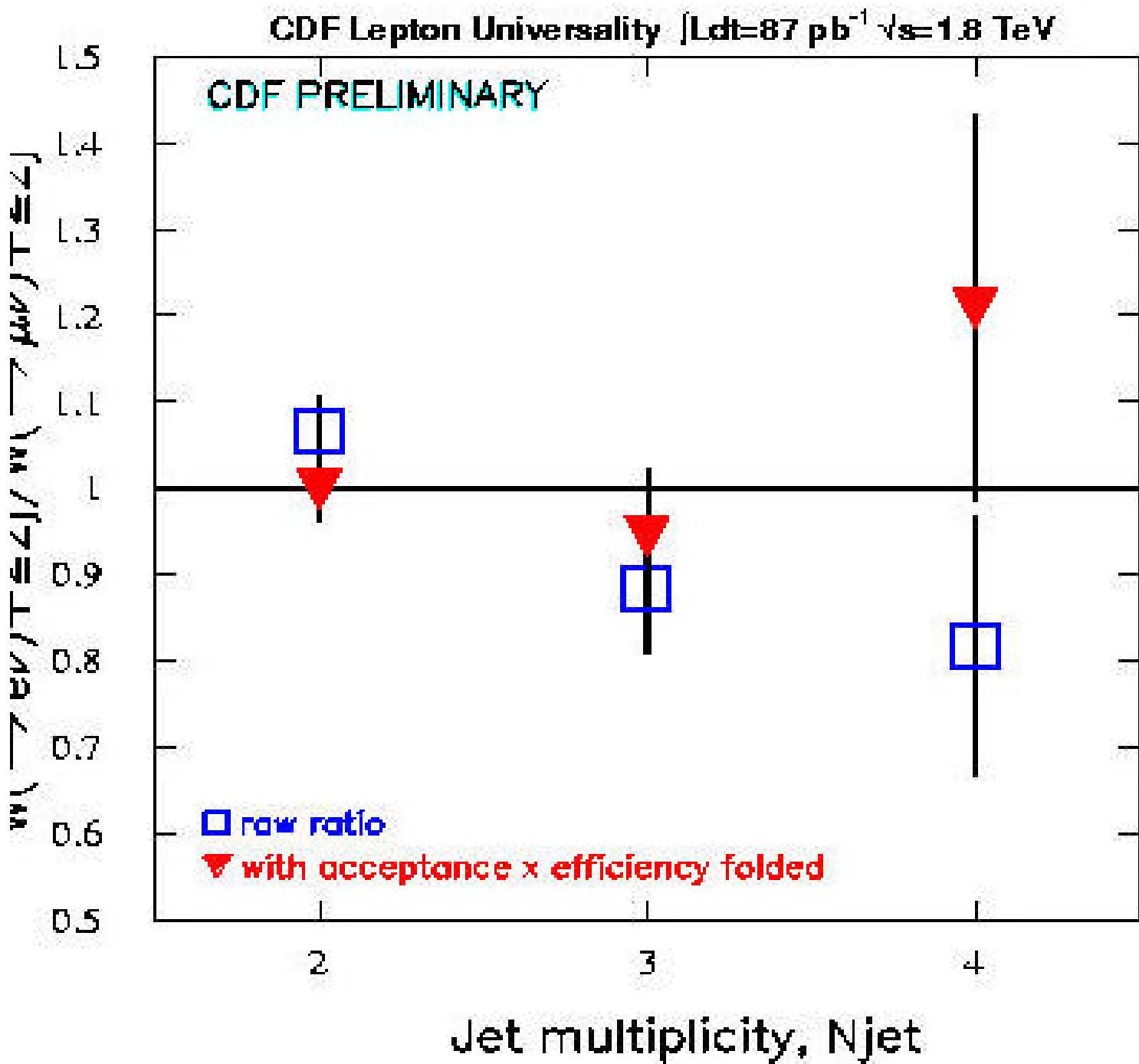


# Ratios in the normalization:

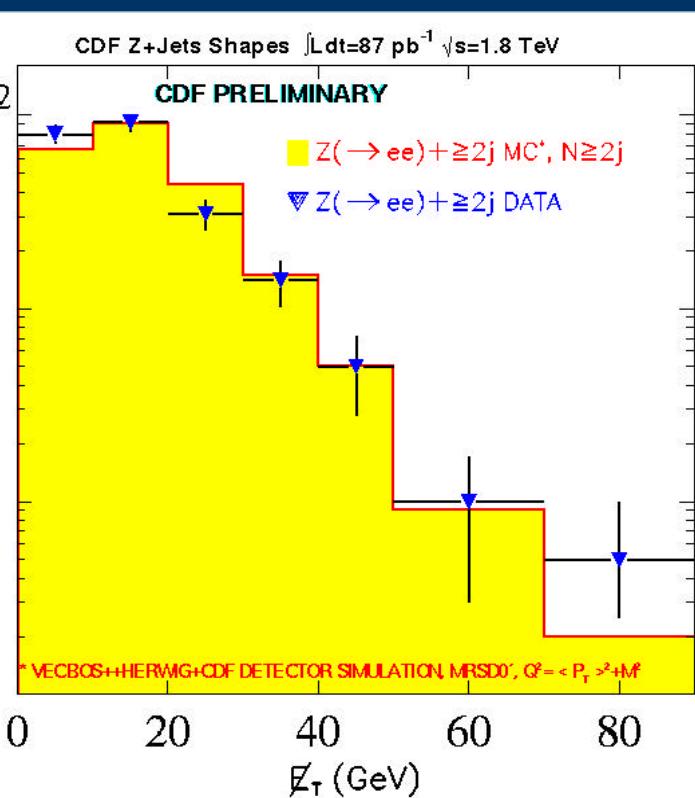
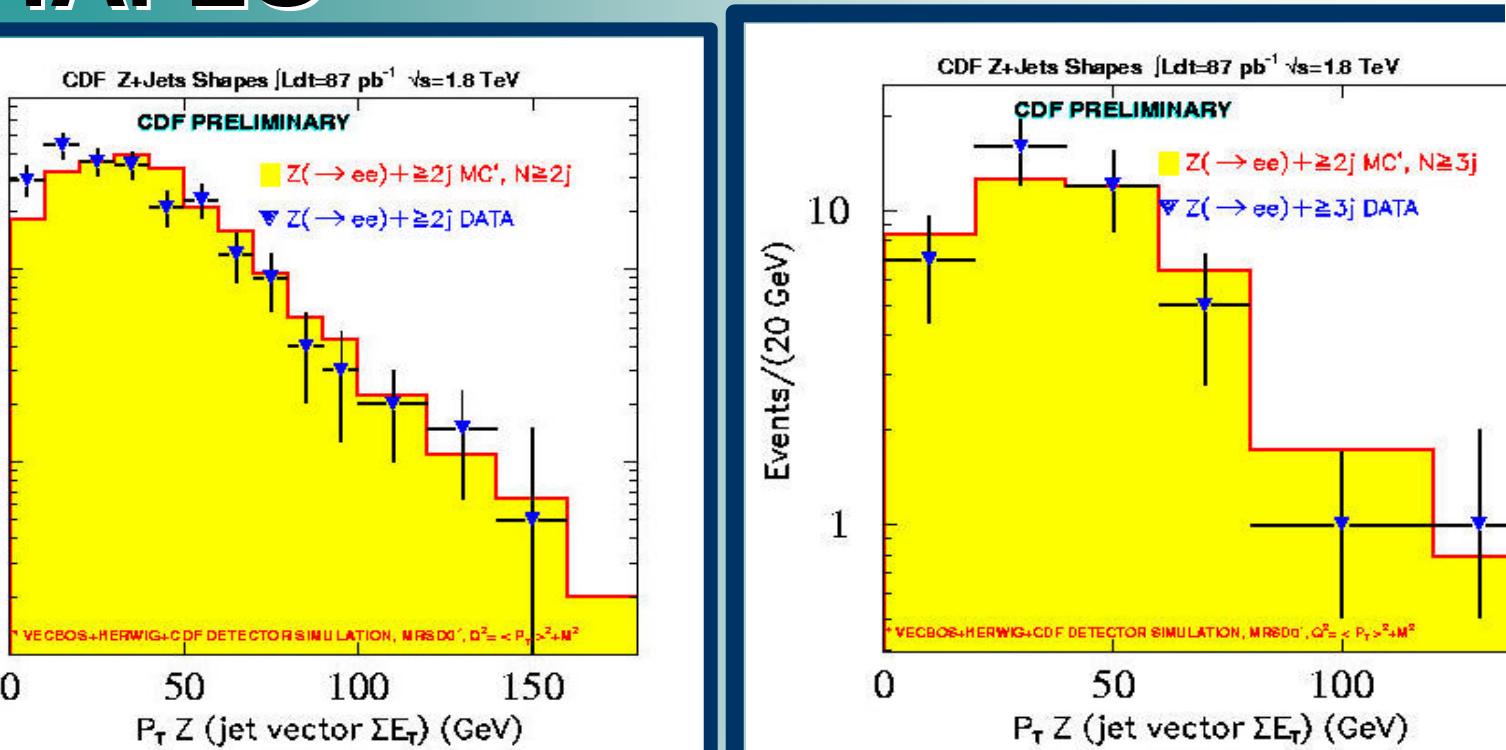
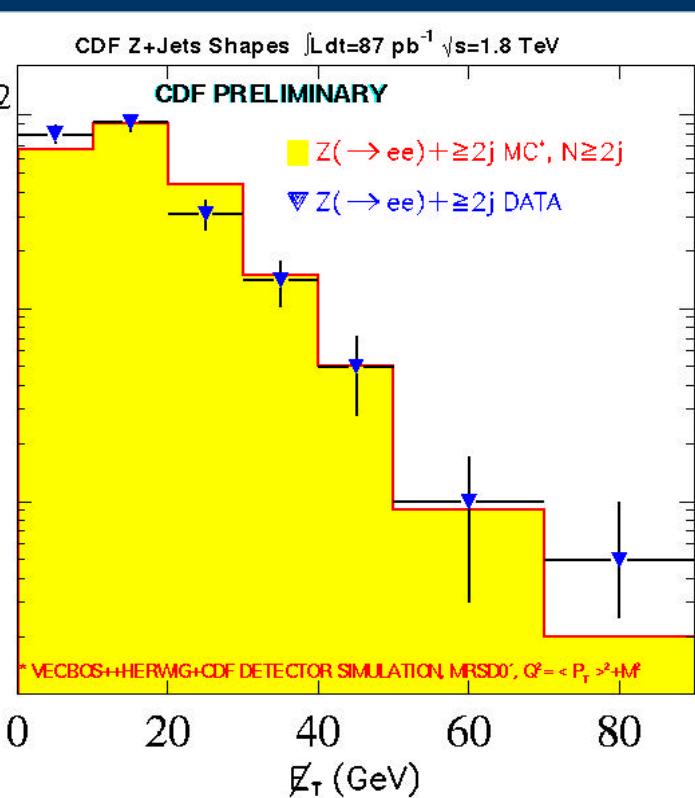
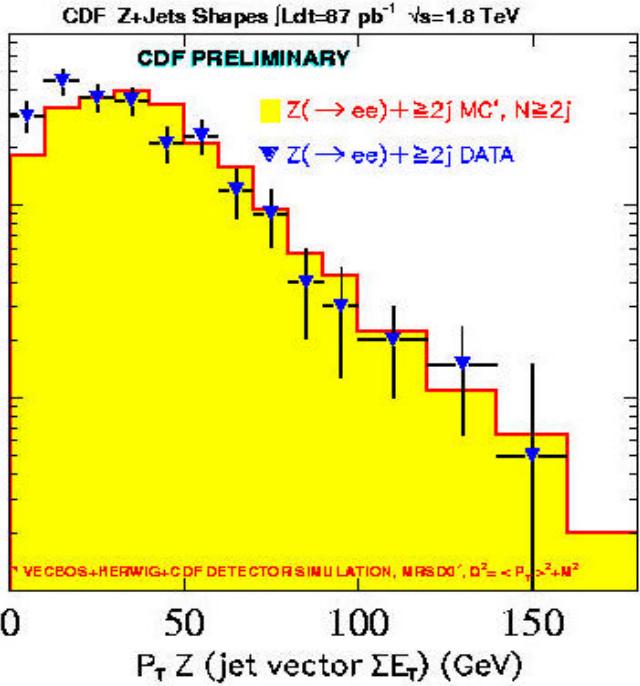
$\frac{W}{Z}$



# Lepton Universality ↪

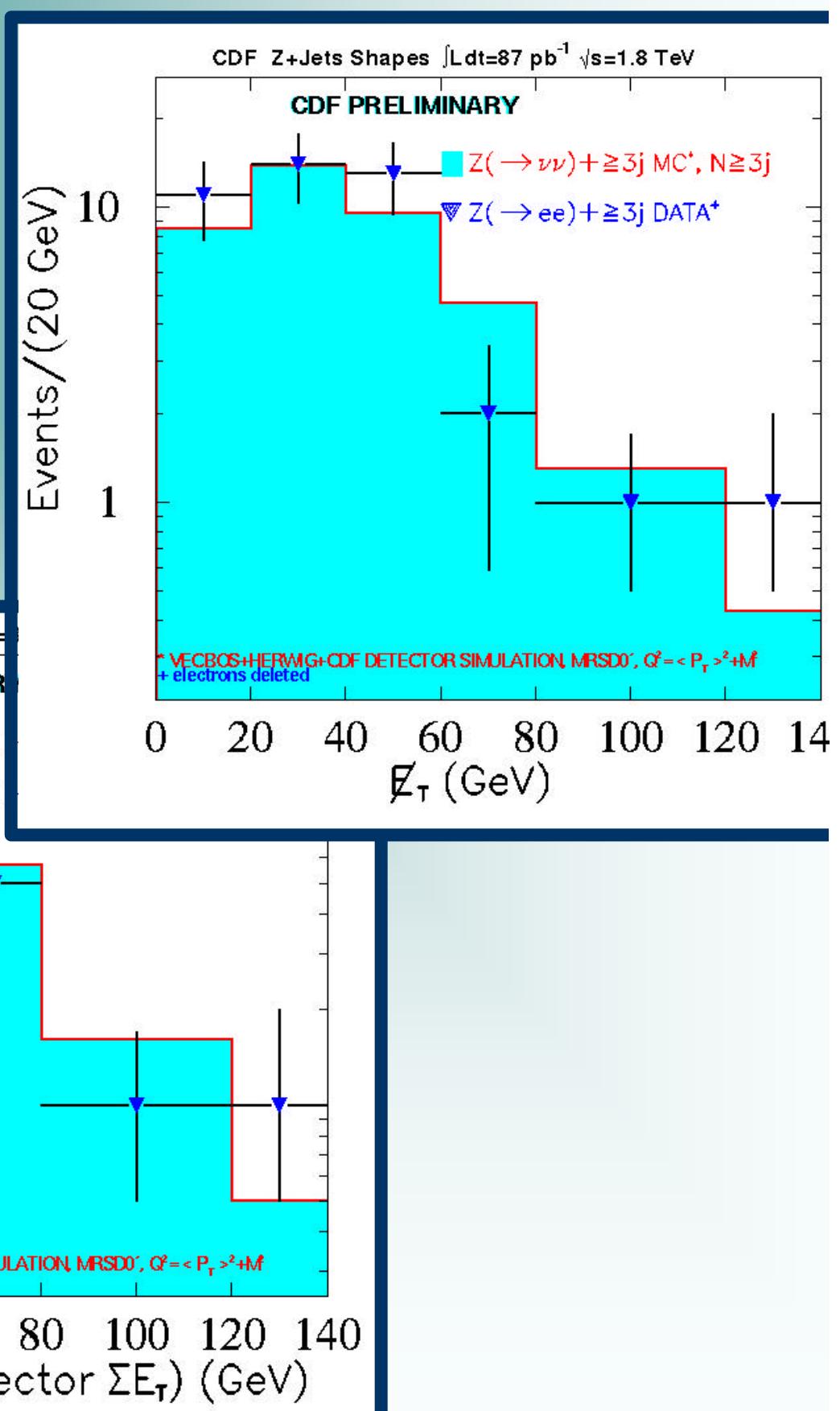


# + $\geq N$ jets ( $N=2, 3$ ) HAPES



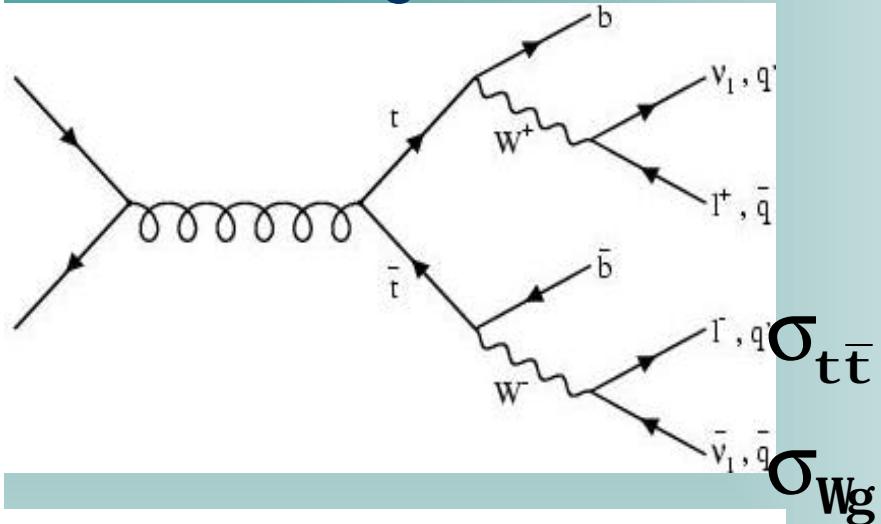
+  $\geq N$  jets ( $N=2, 3$ )

# HAPES



# $\bar{t}$ , single top, di boson

MC samples Luminosity norm  
using theoretical cross sections



$$= 5.06 \text{ pb} \pm 18\%$$

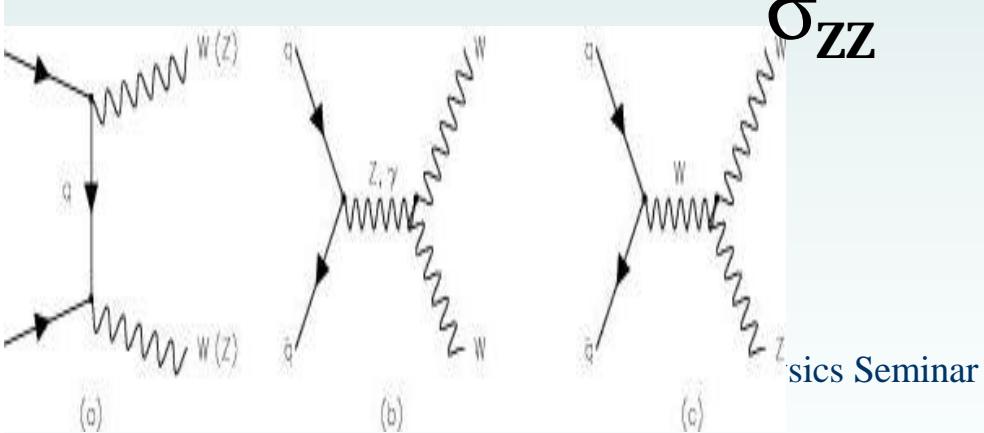
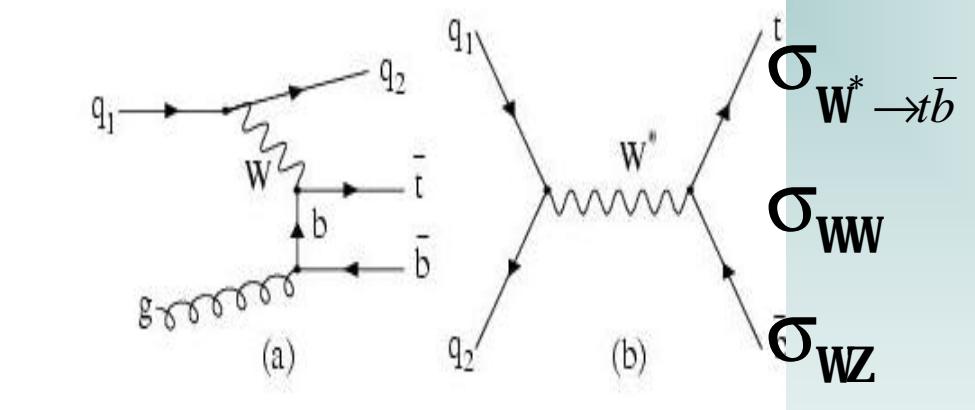
$$= 1.7 \text{ pb} \pm 17\%$$

$$= 0.73 \text{ pb} \pm 9\%$$

$$= 9.5 \text{ pb} \pm 7\%$$

$$= 2.6 \text{ pb} \pm 12\%$$

$$= 1. \text{ pb} \pm 20\%$$



## CD MULTI JET BACKGROUND

Simulate 3-jet events for a very low threshold trigger (JET20) and a higher threshold trigger (JET50).

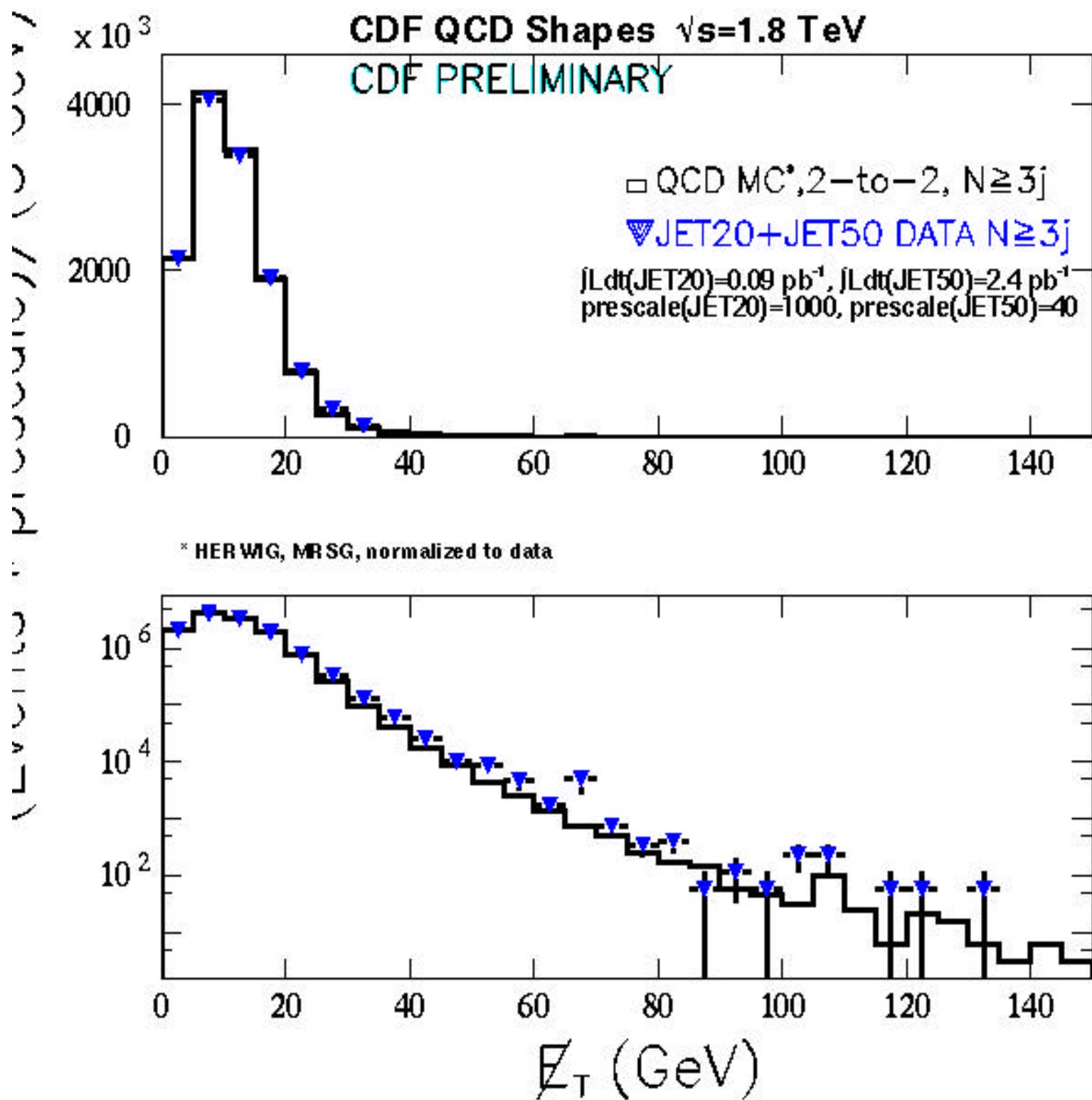
NO Missing Energy required- use the whole Missing Energy spectrum.

Fold in the trigger efficiencies measured the data.

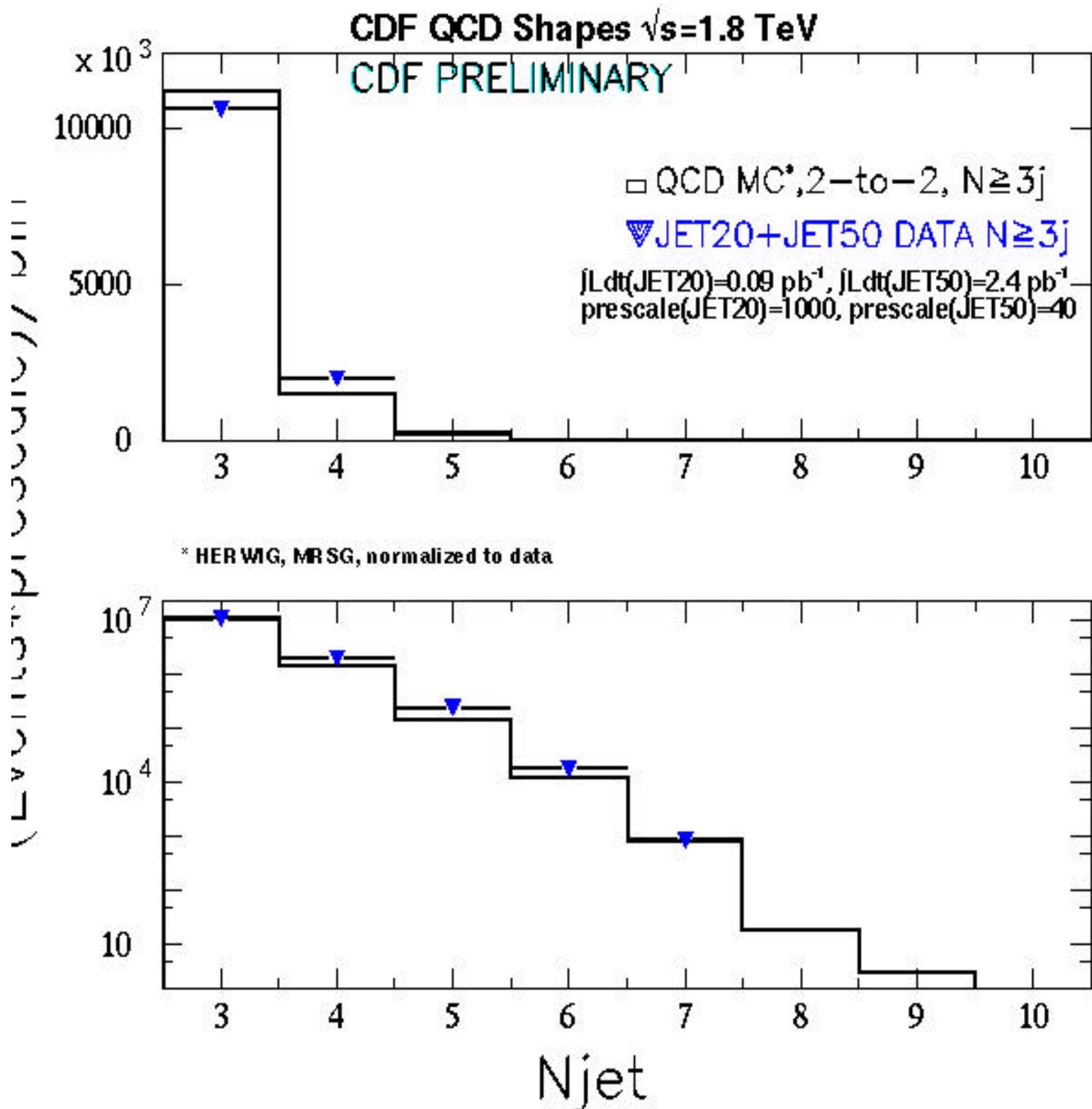
Merge samples and compare kinematic shapes between data and QCD predictions.

Measure the prescale factors and luminosity of the JET data samples used.

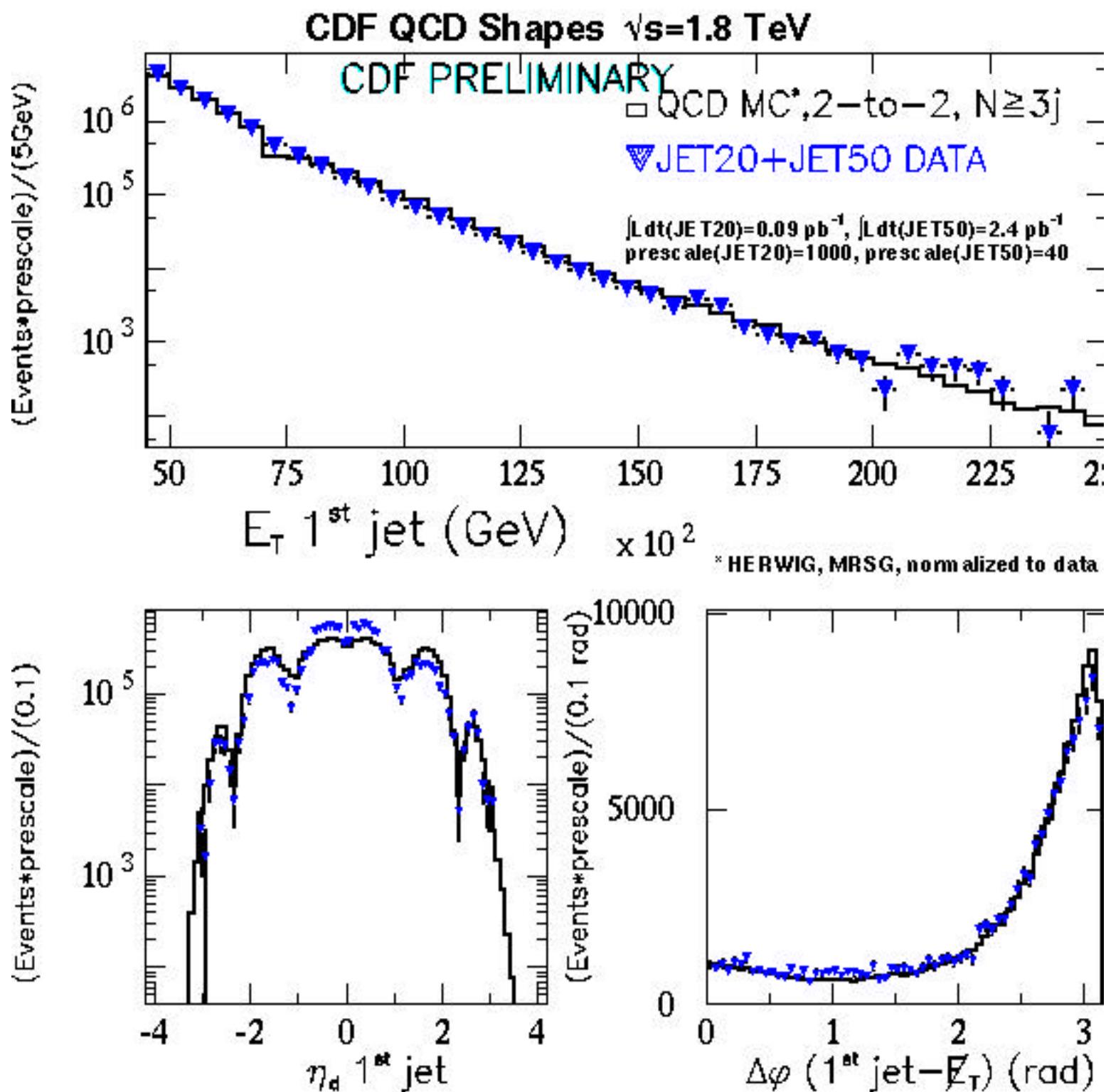
# CD MULTI JET BACKGROUND



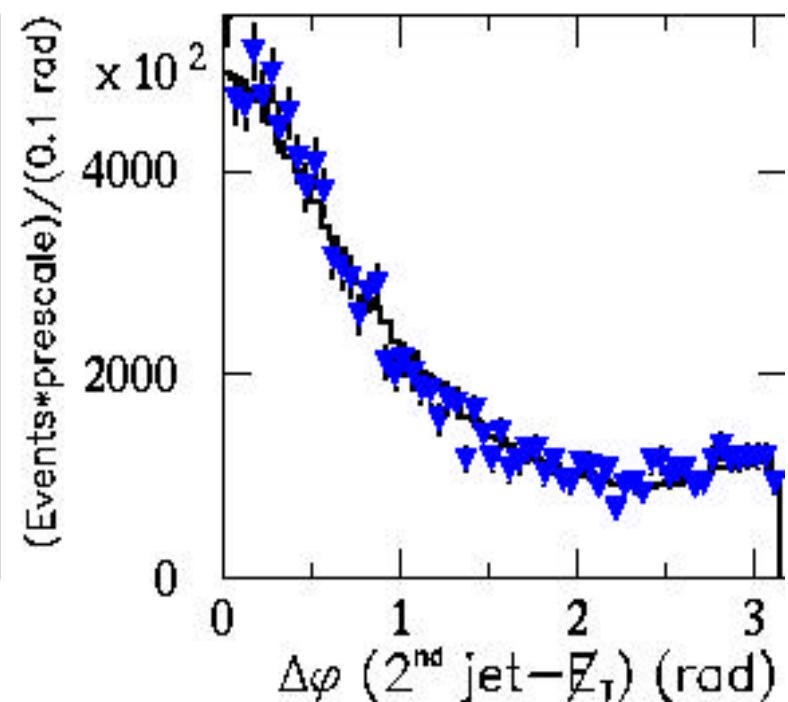
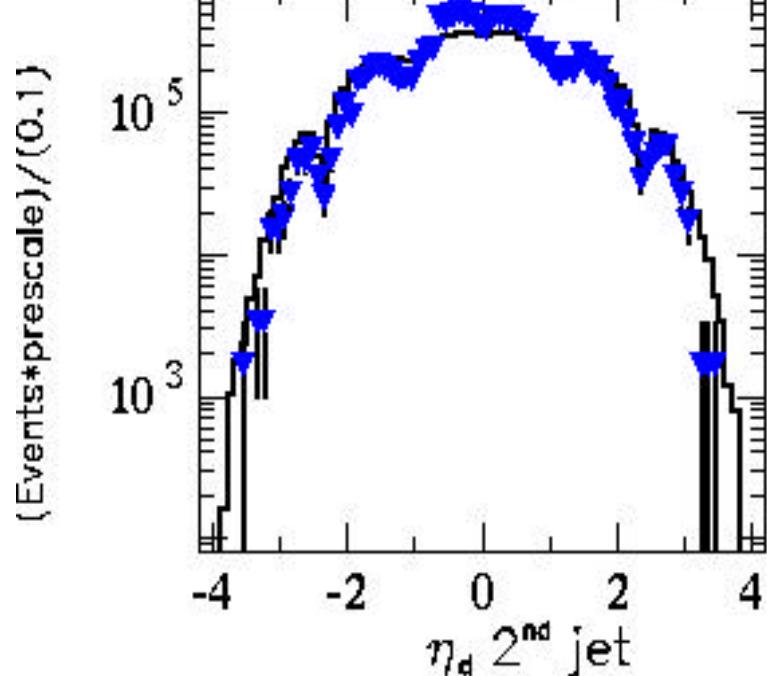
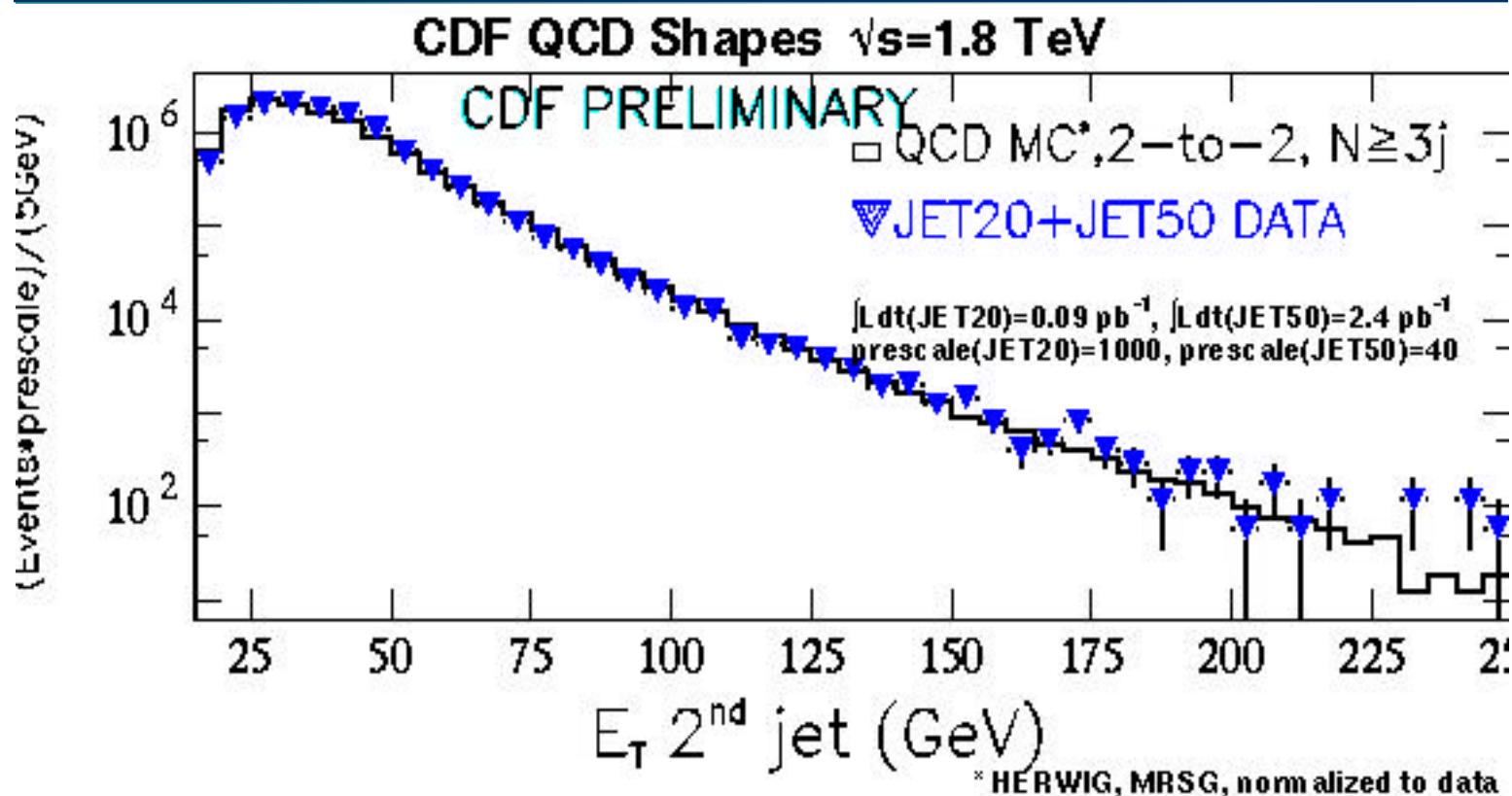
# CDF MULTI JET BACKGROUND



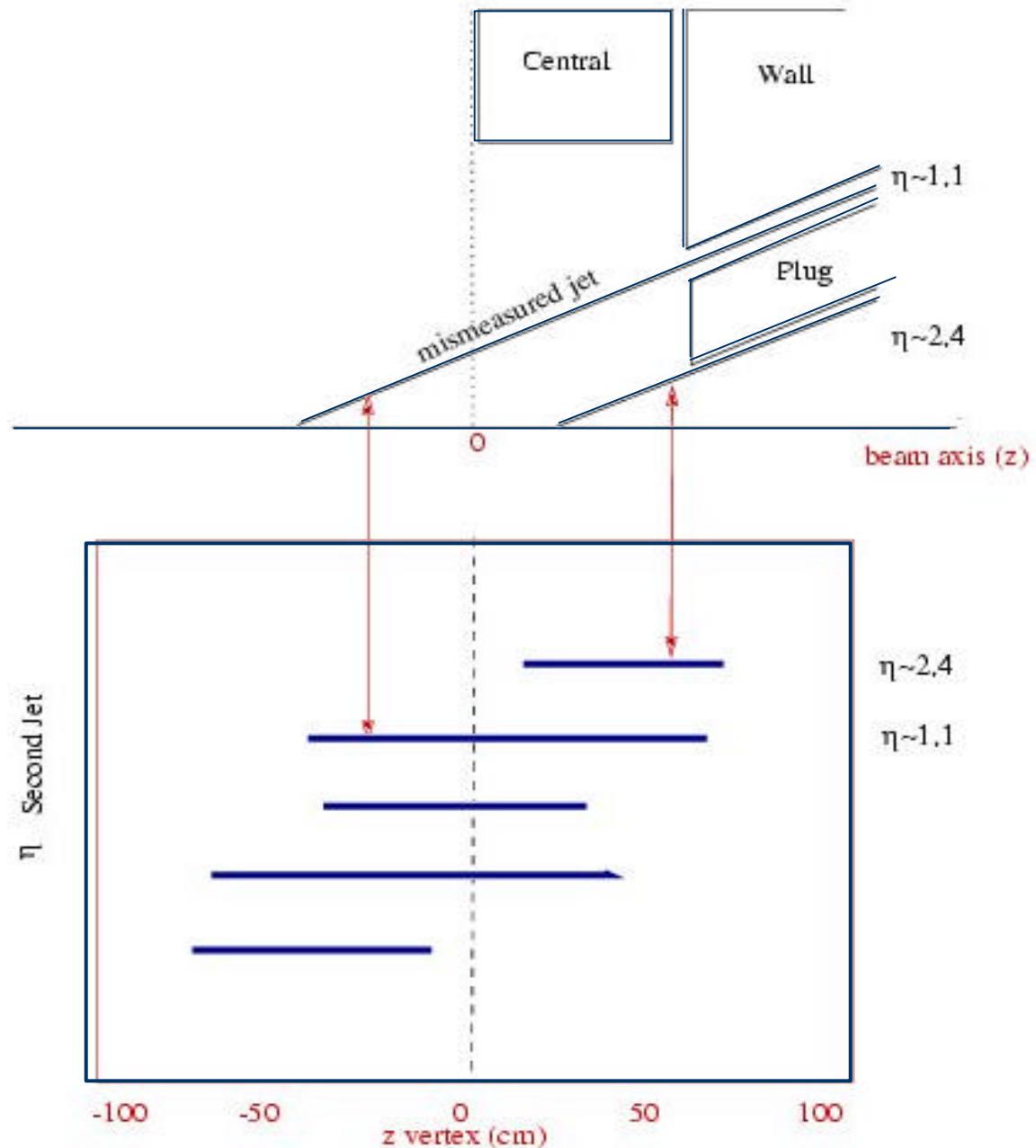
# CDF MULTI JET BACKGROUND



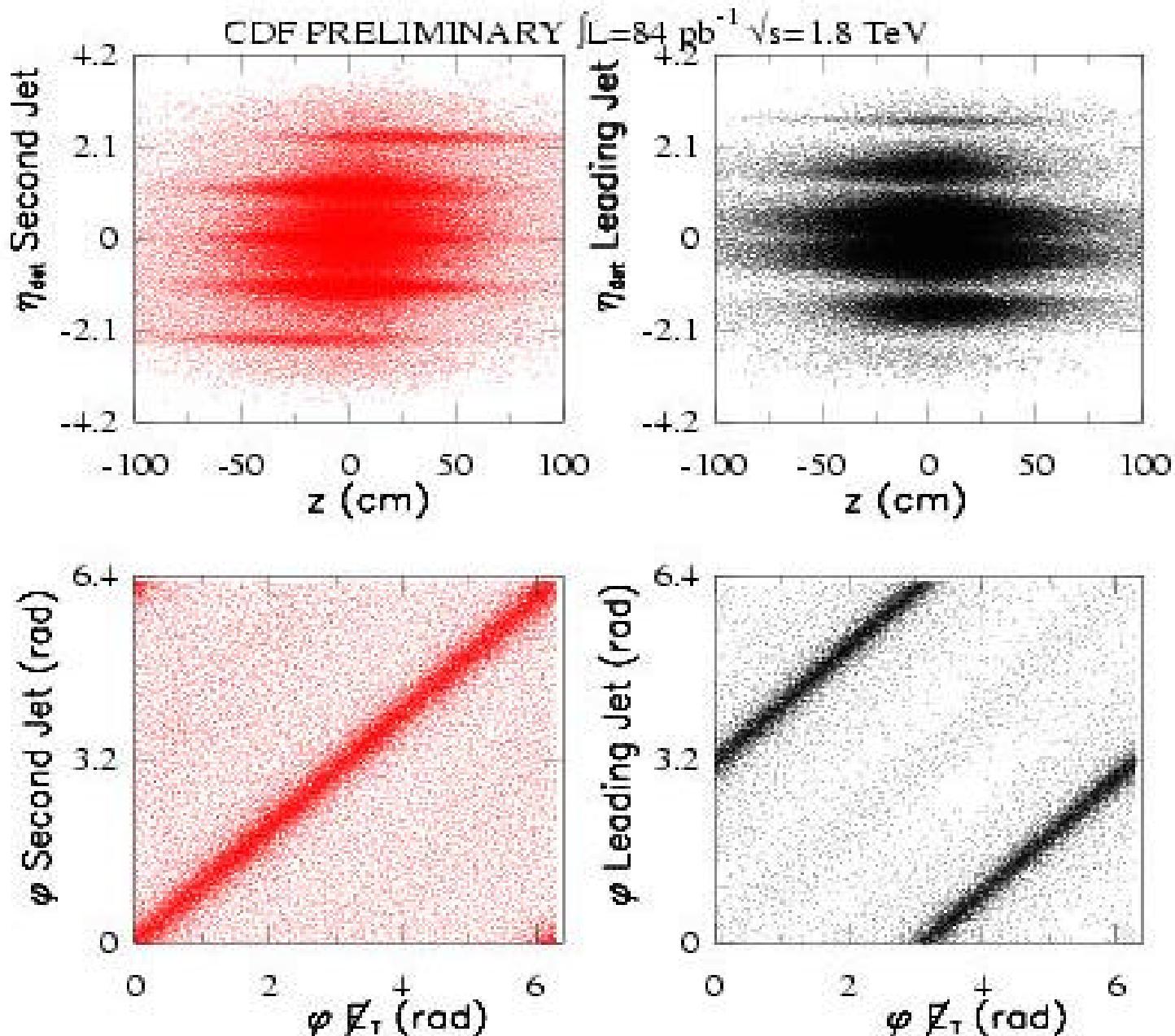
# CDF MULTI JET BACKGROUND



# Missing Energy from QCD mismeasurements

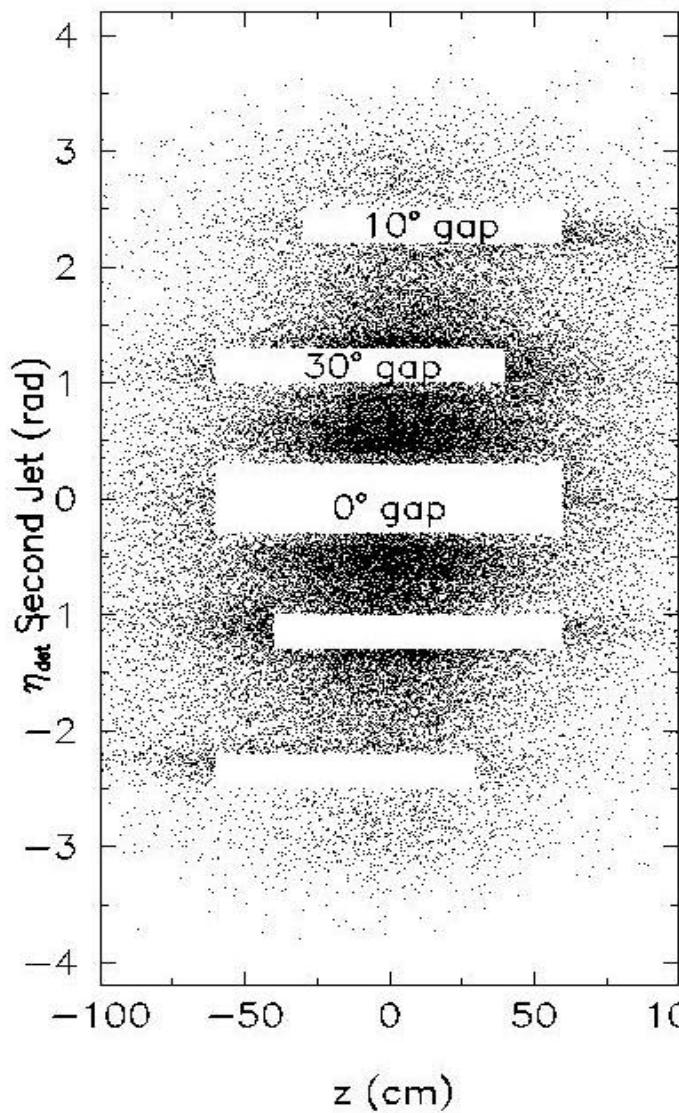


# Missing Energy from QCD mismeasurements

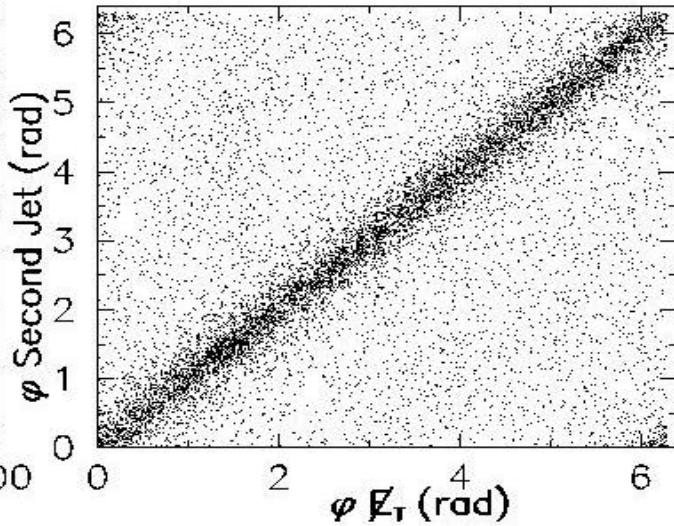


# Missing Energy from QCD mismeasurements

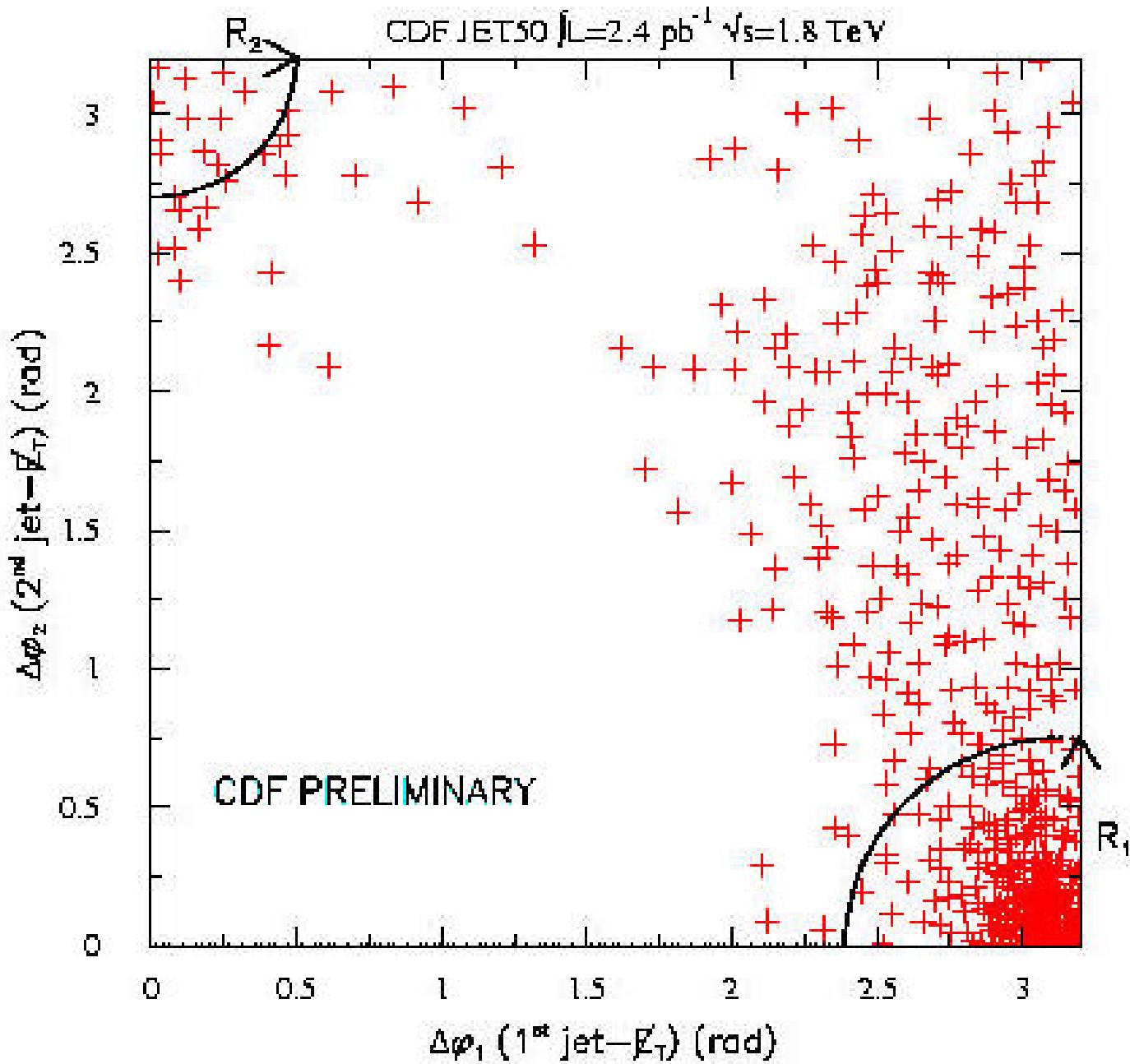
HERWIG(2-to-2)+CDF DETECTOR SIMULATION  $N \geq 3$  Jets  
JET FIDUCIALITY



If the  $\eta_{\text{det}}$  of the second jet is consistent with one of the gaps AND its  $\varphi$  is 0.5 radians or closer to the  $\varphi$  of the  $E_T$  then the event is vetoed.



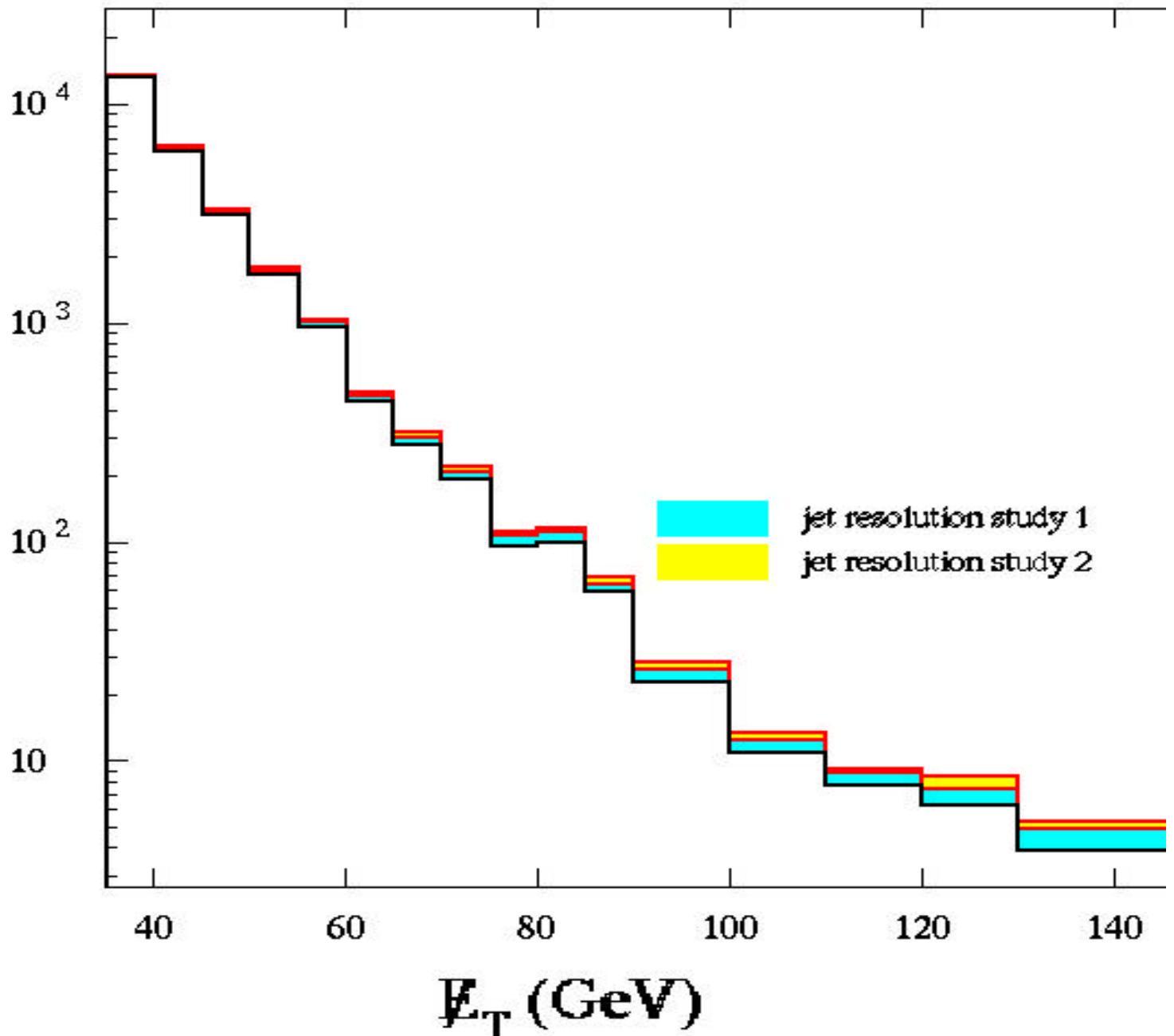
# Missing Energy from QCD mismeasurements



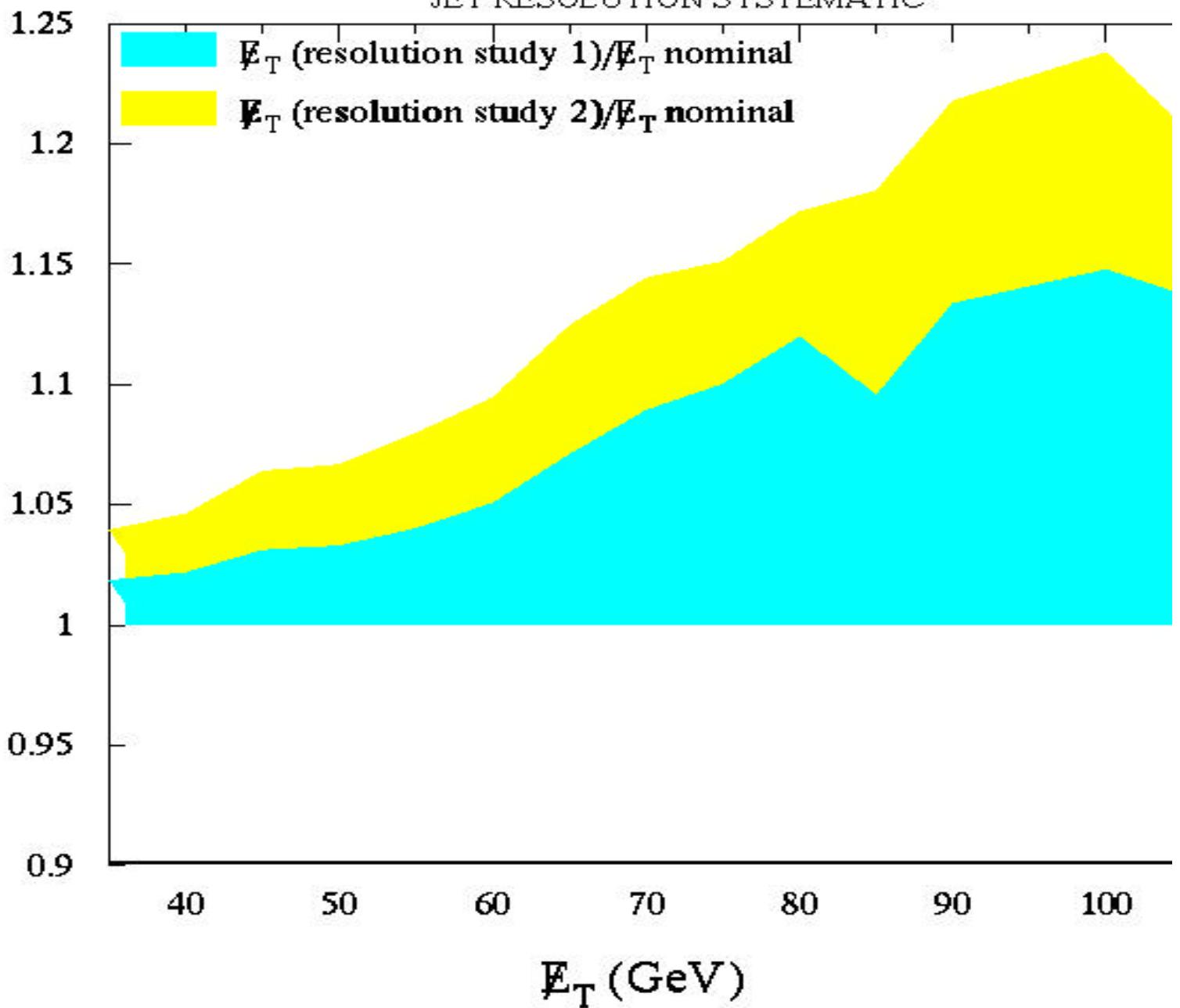
$$R_1 = \sqrt{\delta\phi_1^2 - (\pi - \delta\phi_2)^2}, R_2 = \sqrt{\delta\phi_2^2 - (\pi - \delta\phi_1)^2}$$

# COMMENTS ON THE QCD BACKGROUND

HERWIG(2-to-2)+CDF DETECTOR SIMULATION  $N \geq 3$  Jets  
JET RESOLUTION SYSTEMATIC



HERWIG(2-to-2)+CDF DETECTOR SIMULATION  $N \geq 3$  Jets  
JET RESOLUTION SYSTEMATIC



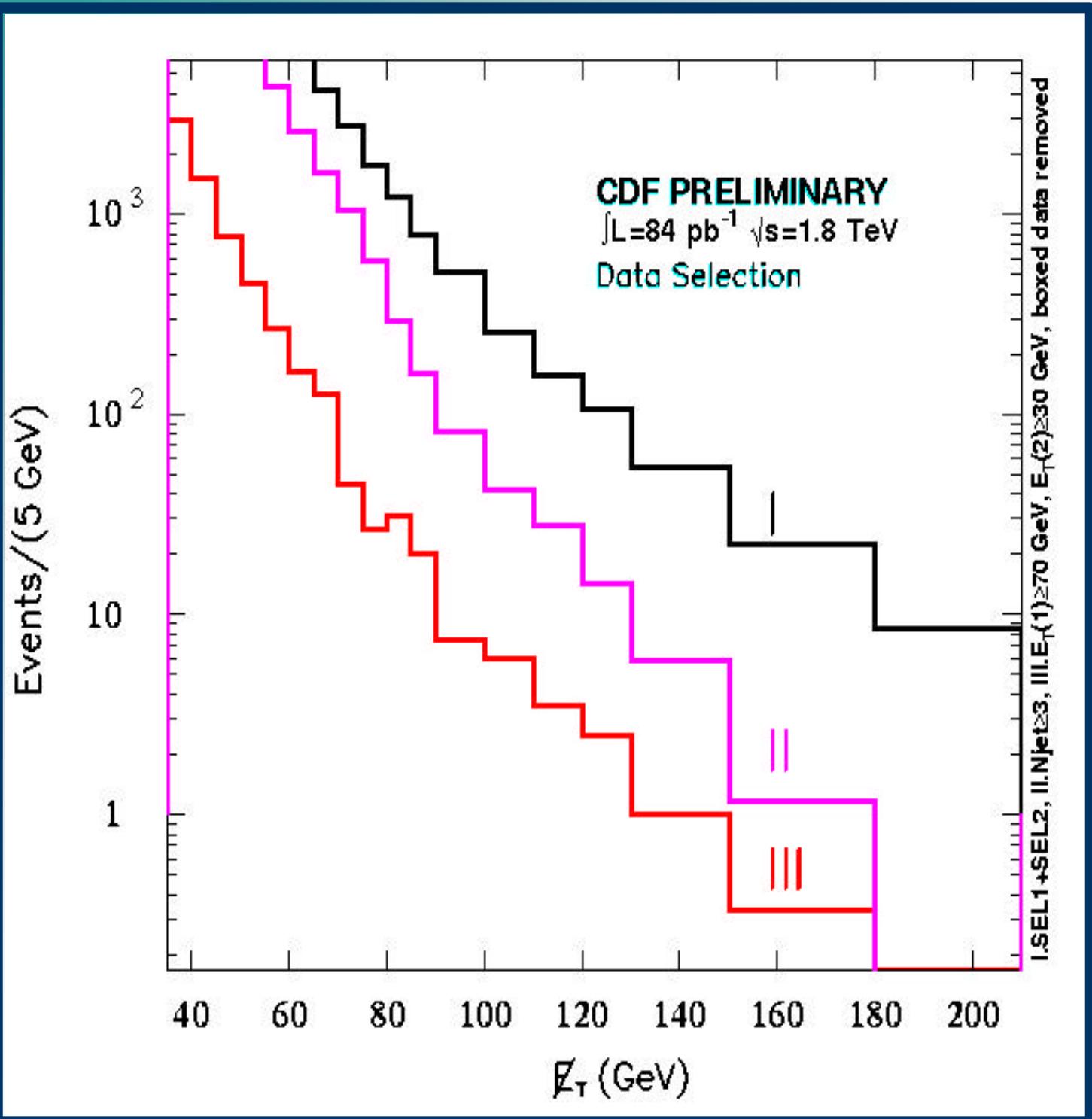
# Analysis Path

Requirement	Number of Events passing
Pre-Selection and Bad Run veto	286728, (I)
$N_{jet} \geq 3$ (cone .7, $E_T \geq 15$ GeV)	107509, (II)
Fiduciality fiducial 2nd,3rd jet	57011
2-D $\delta\phi$	23381
BOX data removed	
$E_T(1) \geq 70$ GeV $E_T(2) \geq 30$ GeV $ \eta_d (1 \text{ or } 2 \text{ or } 3) < 1.1$	6435, (III)
EMF(1),EMF(2) $\leq 0.9$	6013
L2 trigger	4679
$\delta\phi_{min} \geq 0.3$	2737

# Analysis Path

Requirement	Number of Events passing
Pre-Selection and Bad Run veto	286728, (I)
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BOX data removed	
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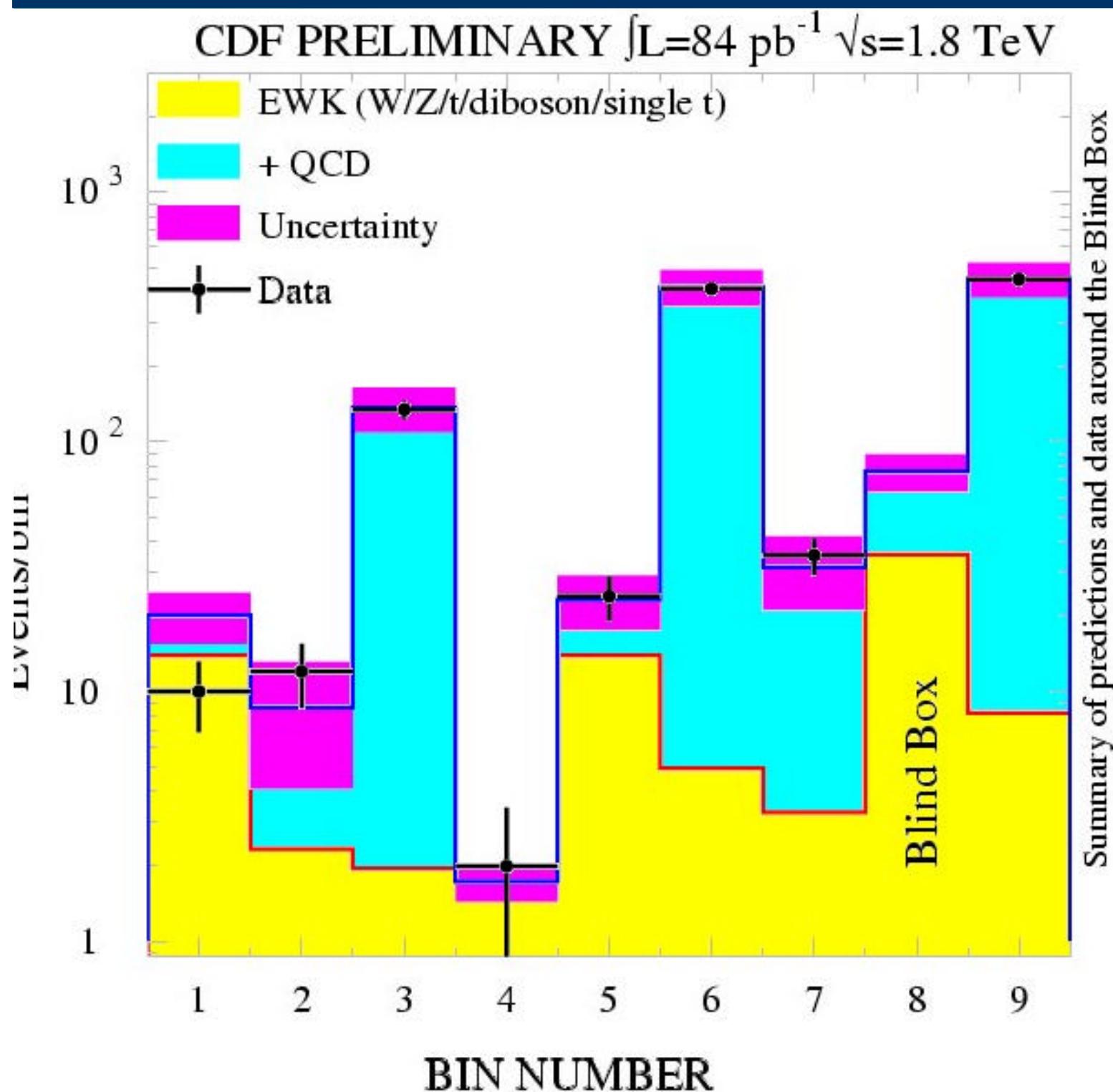
# Final Analysis Path



## Comparisons SM predictions-Data around the Blind Box

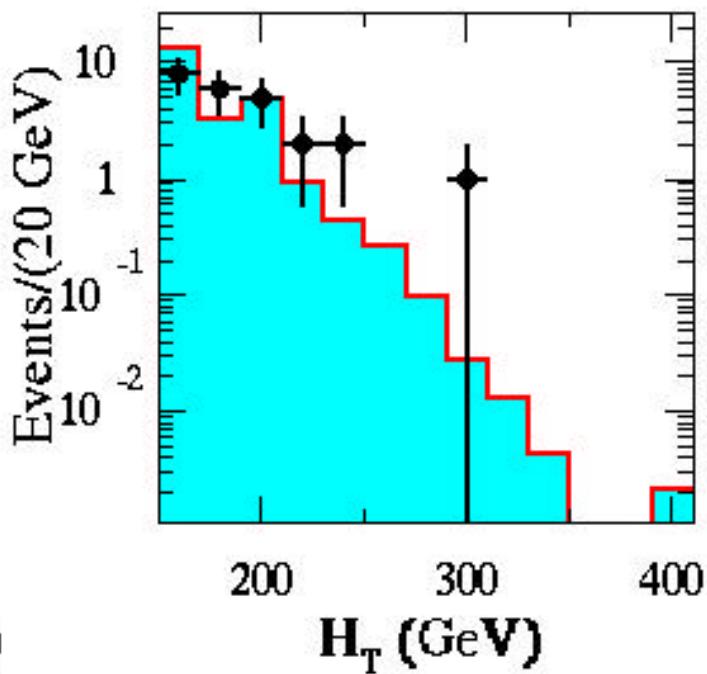
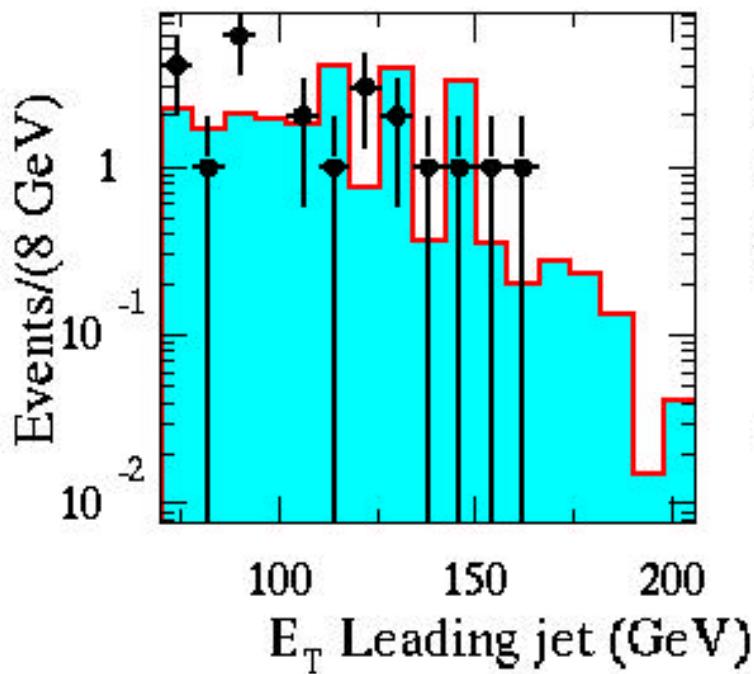
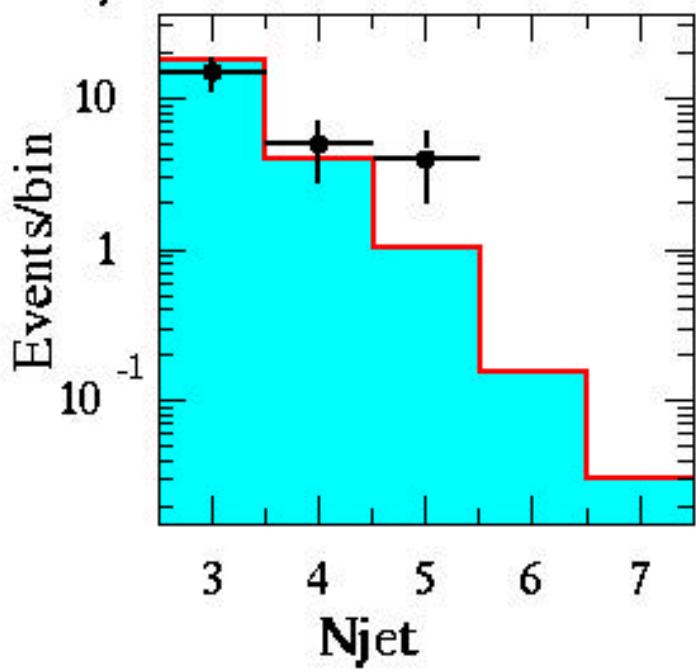
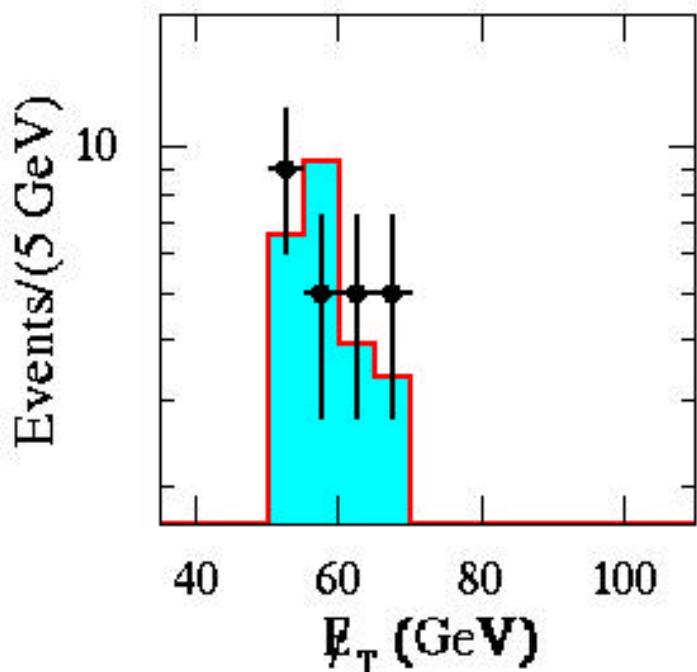
	Description	EWK	QCD	All	Data
1	$E_T \geq 70, H_T \geq 150, N_{trk}^{iso} > 0$	13.9	6.26	$20.2 \pm 4.7$	10
2	$E_T \geq 70, H_T < 150, N_{trk}^{iso} = 0$	2.3	6.26	$8.6 \pm 4.5$	12
3	$35 < E_T < 70, H_T > 150, N_{trk}^{iso} = 0$	1.95	134.6	$136.5 \pm 27.8$	134
4	$E_T > 70, H_T < 150, N_{trk}^{iso} > 0$	1.73	0	$1.73 \pm 0.3$	2
5	$35 < E_T < 70, H_T > 150, N_{trk}^{iso} > 0$	13.95	9.39	$23.34 \pm 5.7$	24
6	$35 < E_T < 70, H_T < 150, N_{trk}^{iso} = 0$	4.9	413.16	$418.1 \pm 68.8$	410
7	$35 < E_T < 70, H_T < 150, N_{trk}^{iso} > 0$	3.3	28.17	$31.4 \pm 10.2$	35
8	$E_T > 70, H_T > 150, N_{trk}^{iso} = 0$	35.3	40.69	$76.02 \pm 12.8$	?
9	$35 < E_T < 70, H_T < 150$	8.2	441.3	$449.5 \pm 72$	445

## Comparisons SM predictions-Data around the Blind Box

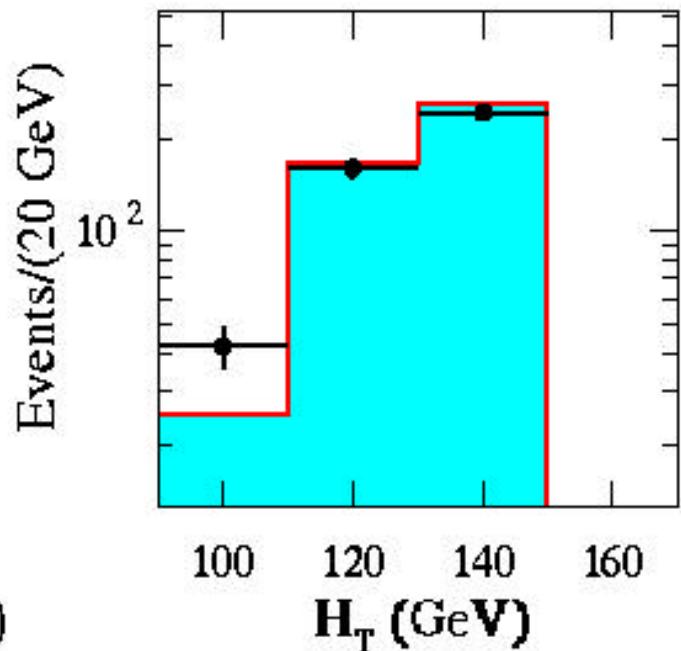
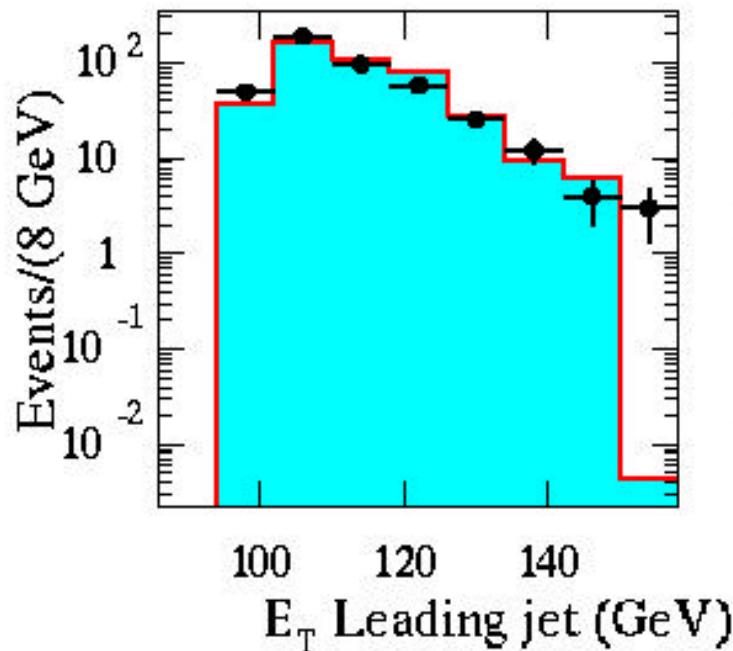
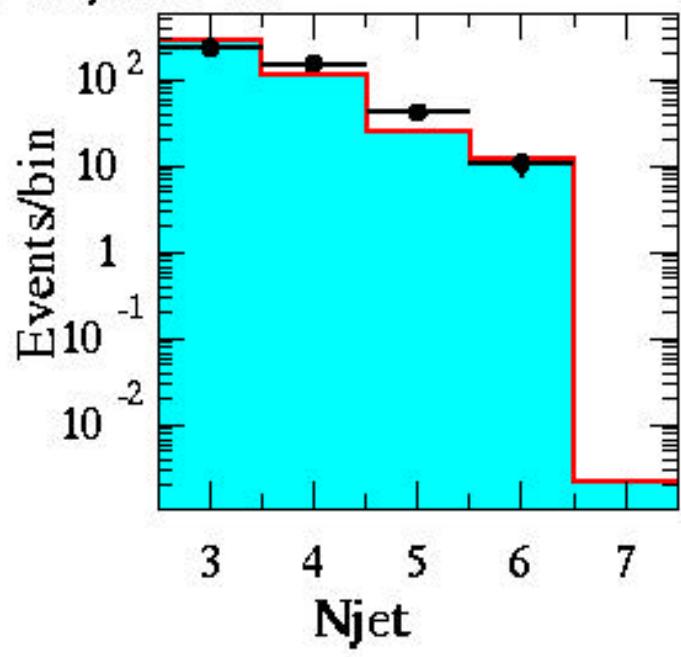
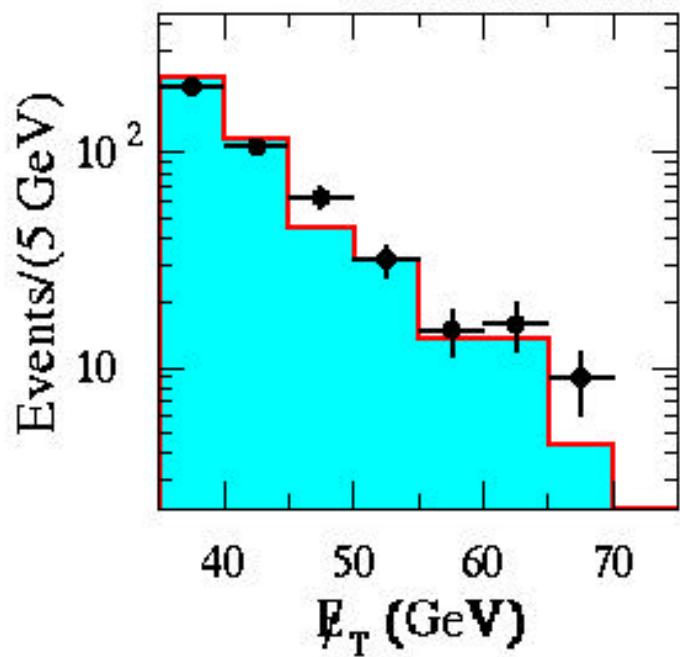


# HAPES AROUND THE BOX

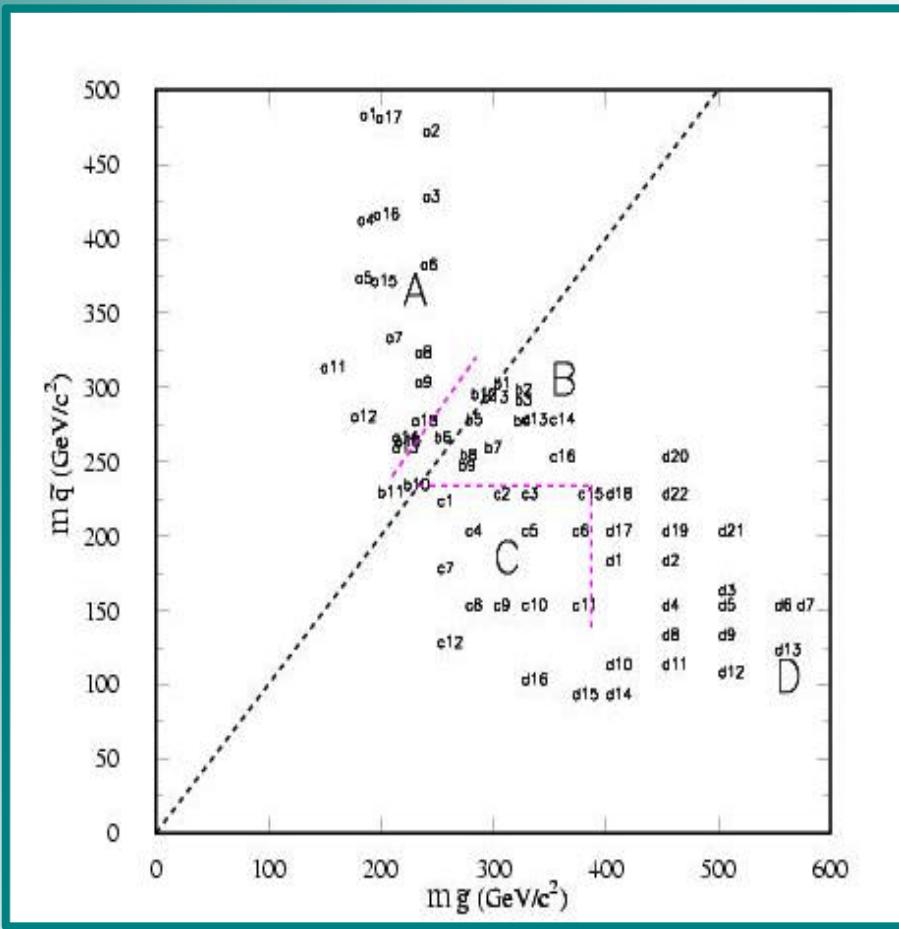
CDF PRELIMINARY  $\int L = 84 \text{ pb}^{-1}$   $\sqrt{s} = 1.8 \text{ TeV}$   
Bin5. SM Prediction=23.4, Data=24



CDF PRELIMINARY  $\int L = 84 \text{ pb}^{-1}$   $\sqrt{s} = 1.8 \text{ TeV}$   
Bin9. SM Prediction=450, Data=445



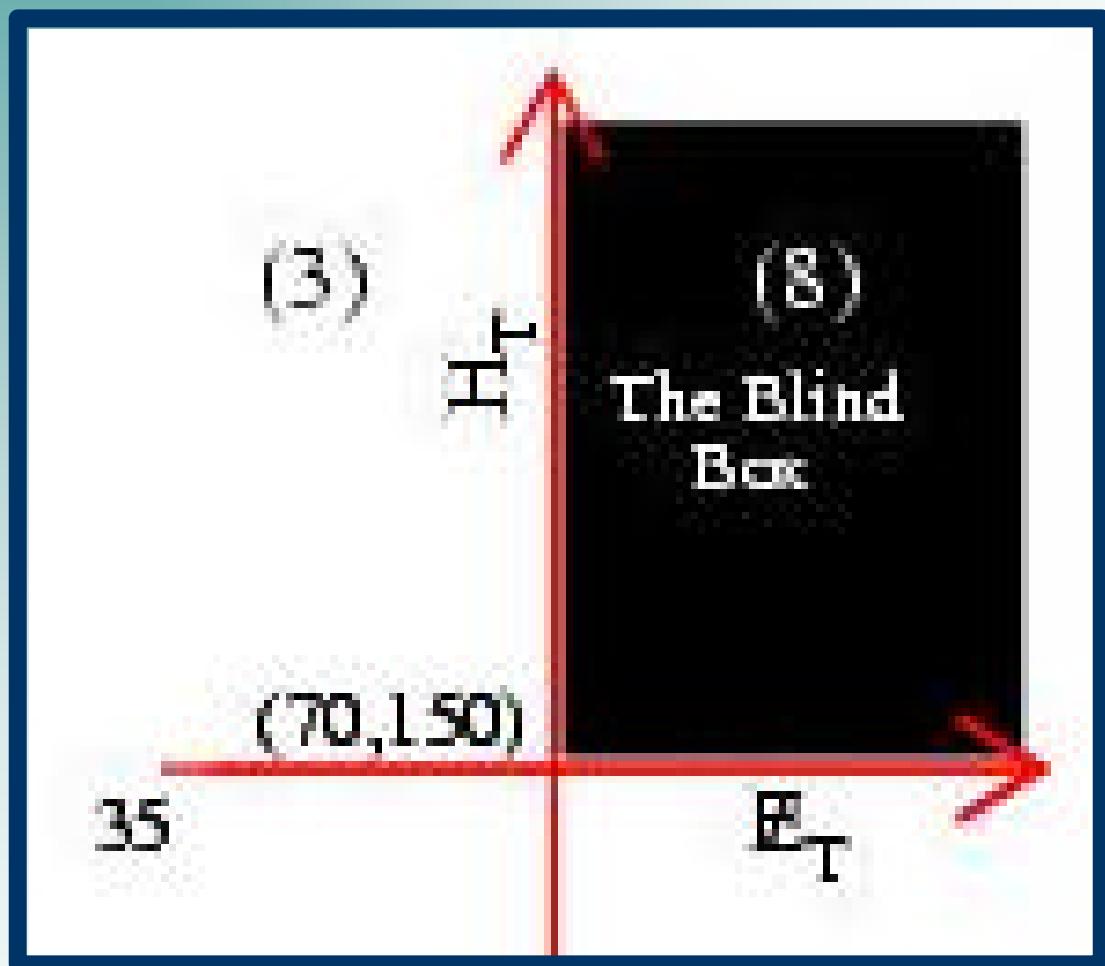
# OPTIMIZATION IN SUSY SPACE



Regions	$E_T, H_T$ (GeV)	Standard Model prediction
A/D	90,160	$32.7 \pm 6.7$
B	110,230	$3.7 \pm .5$
C	110,170	$10.6 \pm 1$

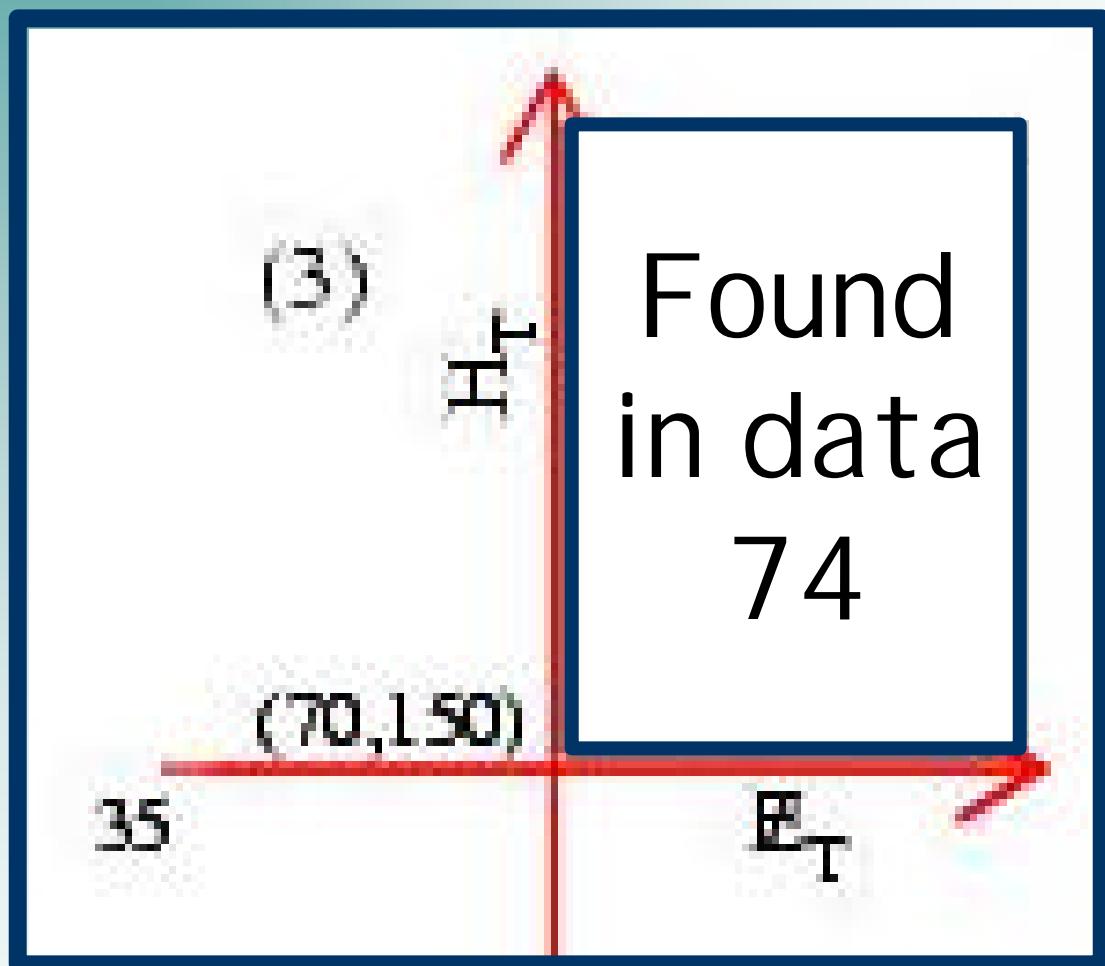
# "The BOX"

The Box: SM Expected 76 



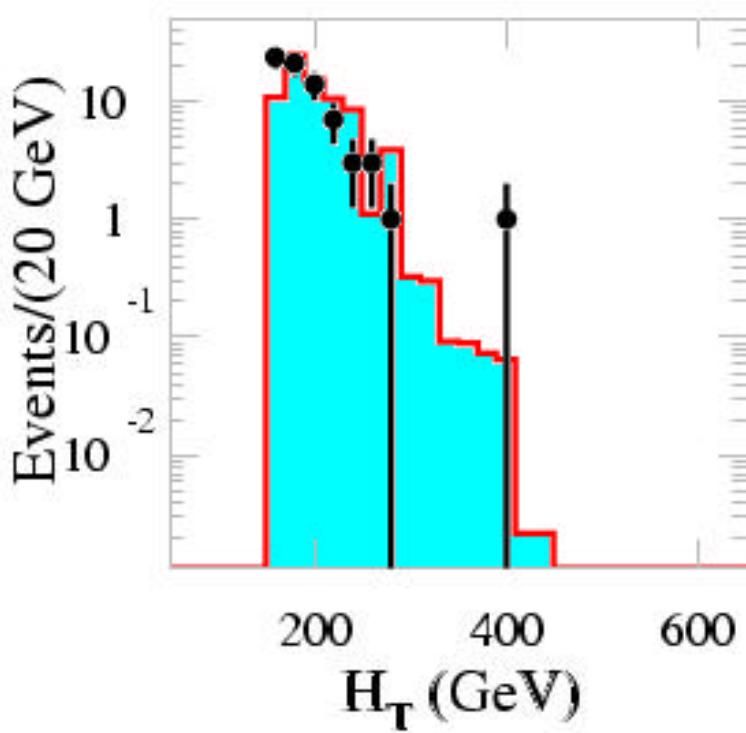
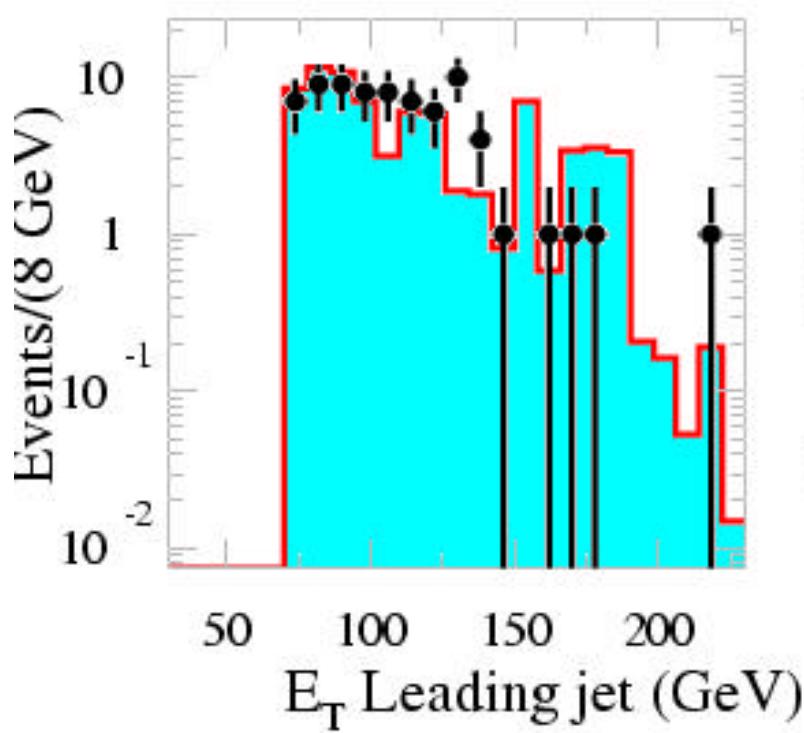
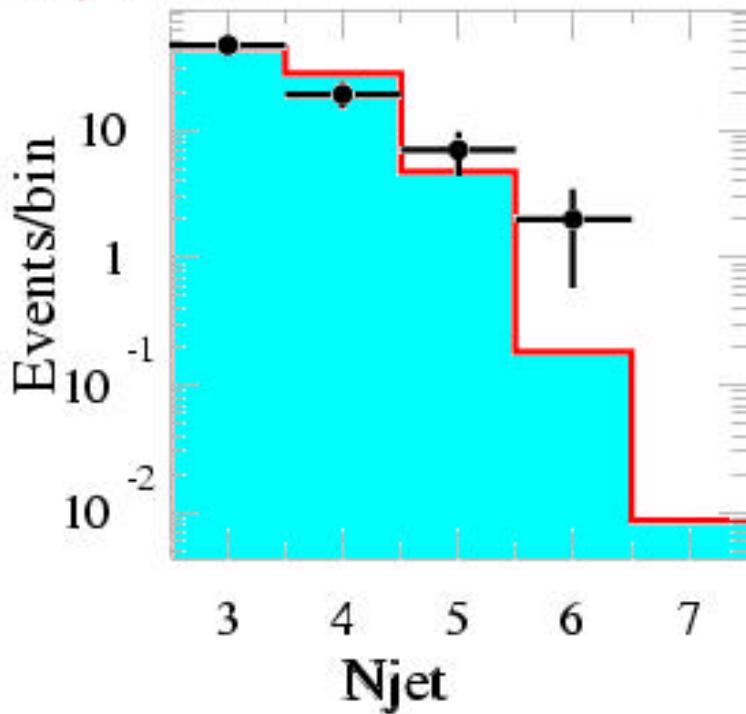
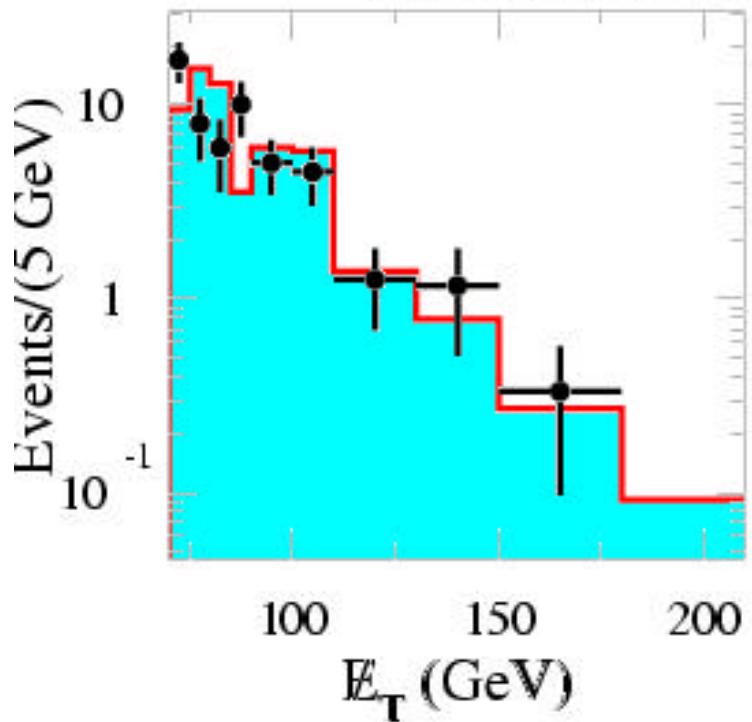
# "The BOX"

The Box: SM Expected 76 



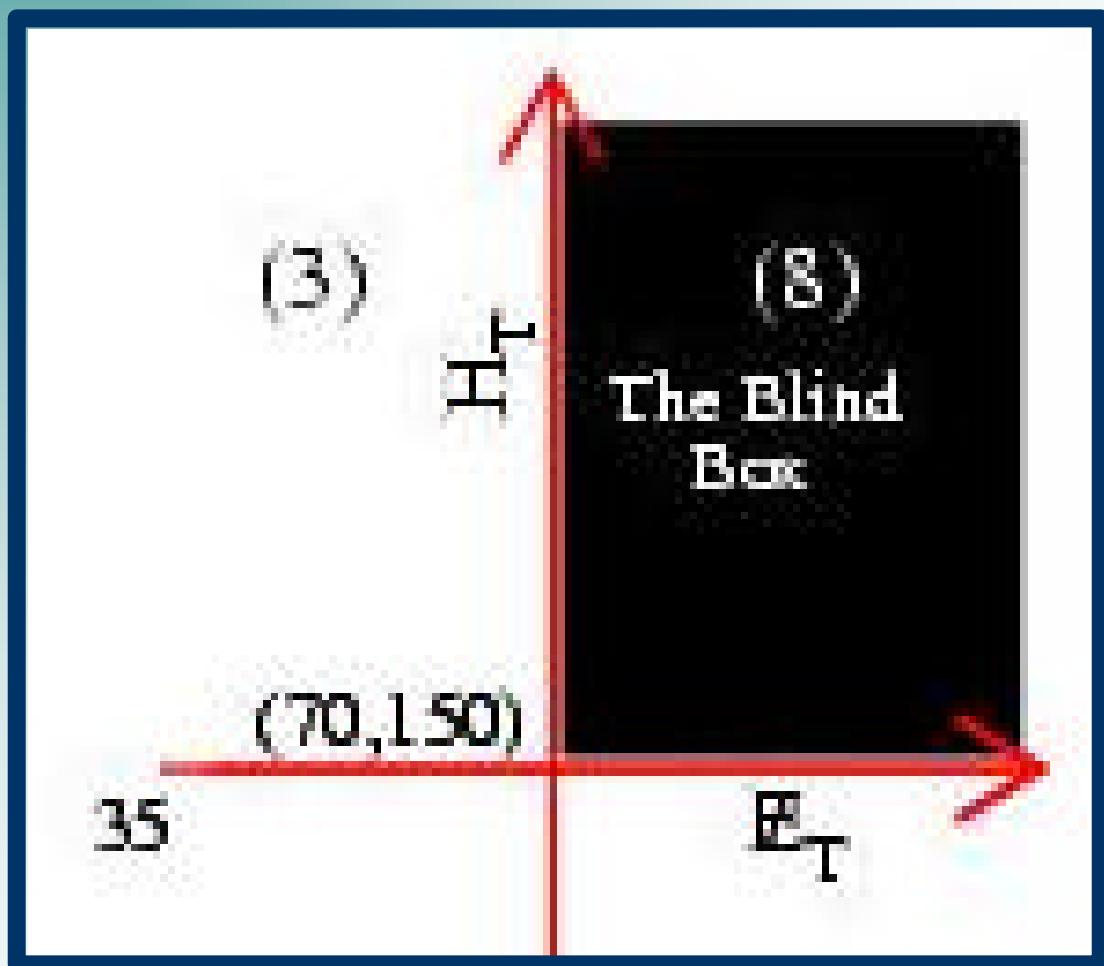
# "The BOX"

CDF PRELIMINARY  $\int L = 84 \text{ pb}^{-1}$   $\sqrt{s} = 1.8 \text{ TeV}$   
BOX. SM Prediction=76, Data=74



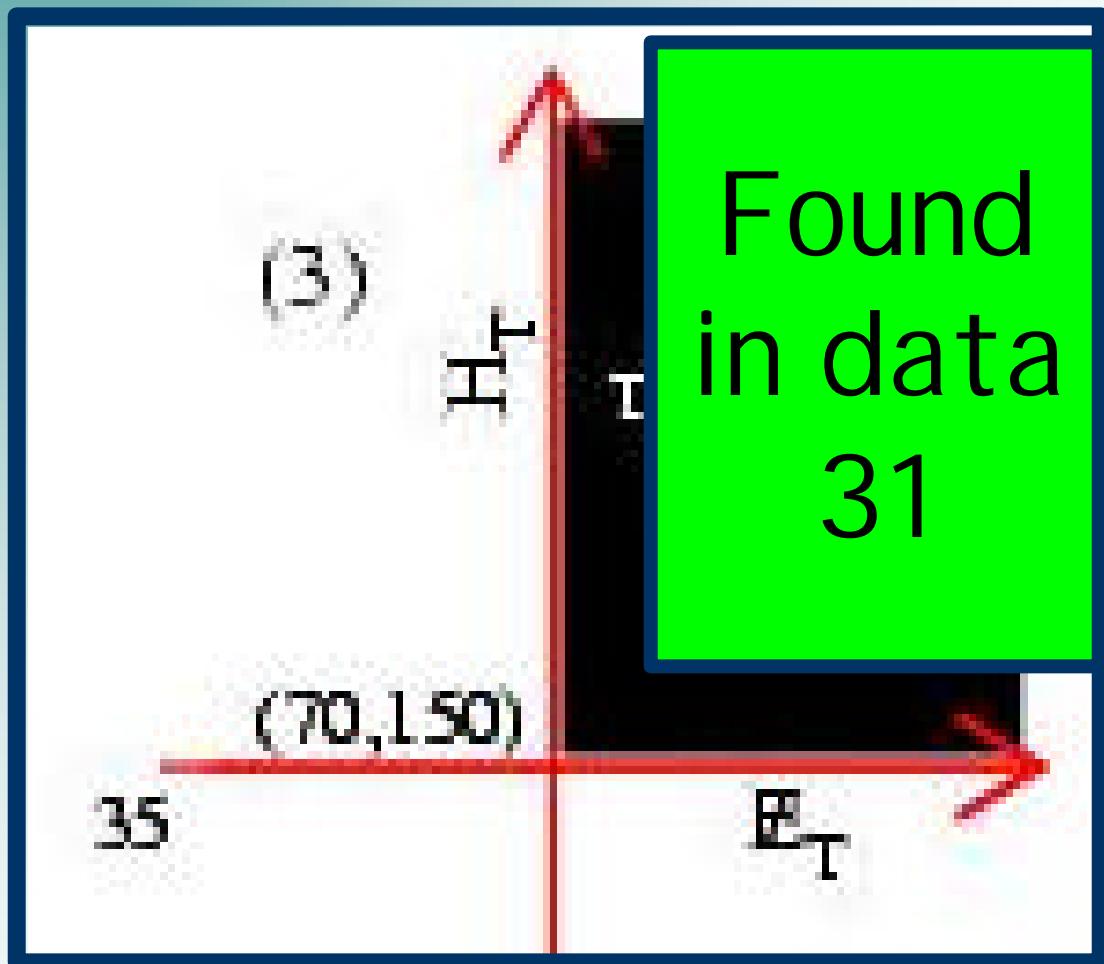
# "The other BOXes"

A/D SUSY boxes:  
SM Expected 337



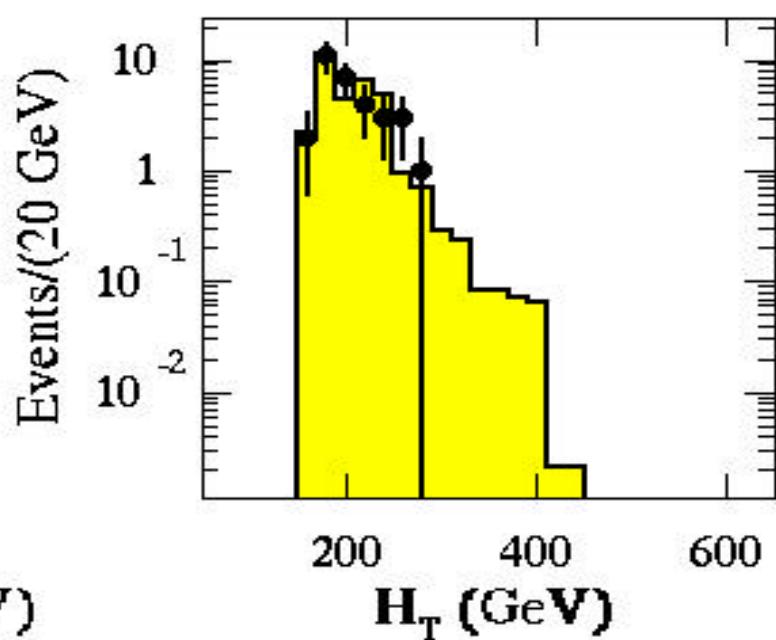
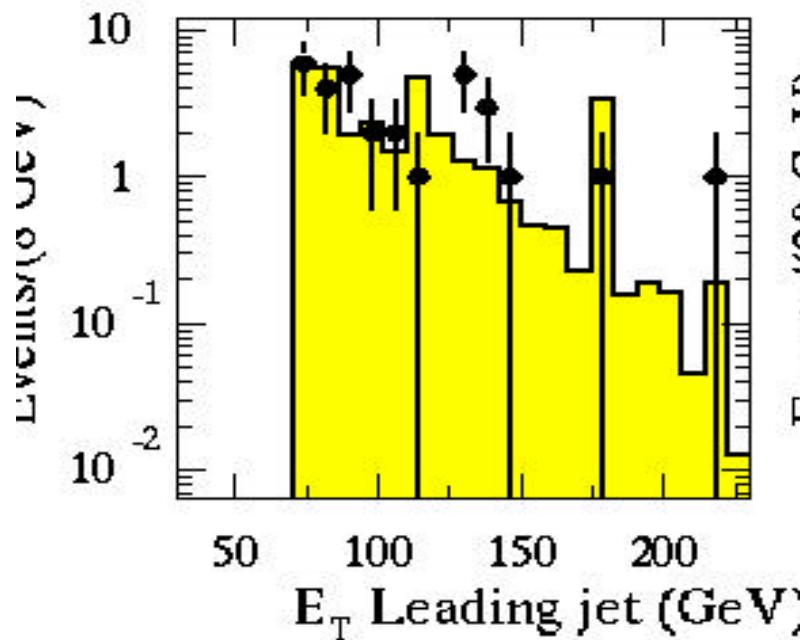
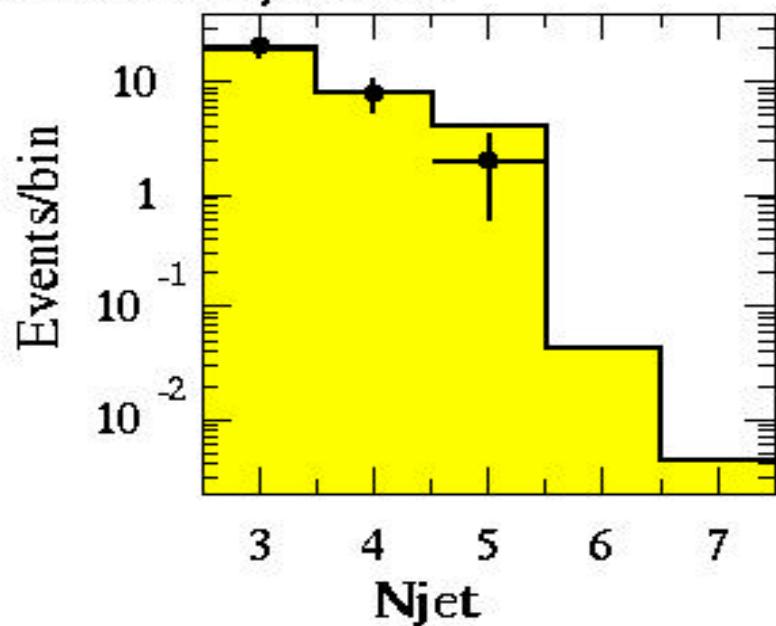
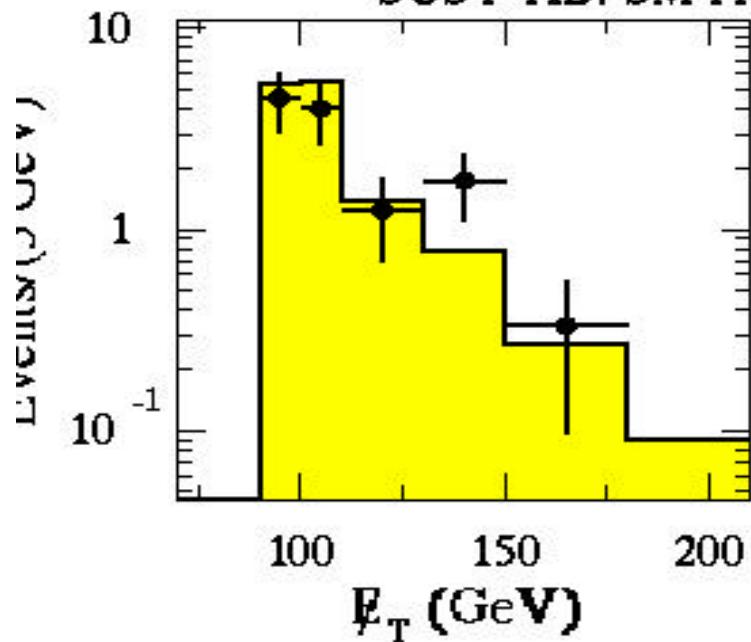
# "The other BOXes"

A/D SUSY boxes:  
SM Expected 33  7



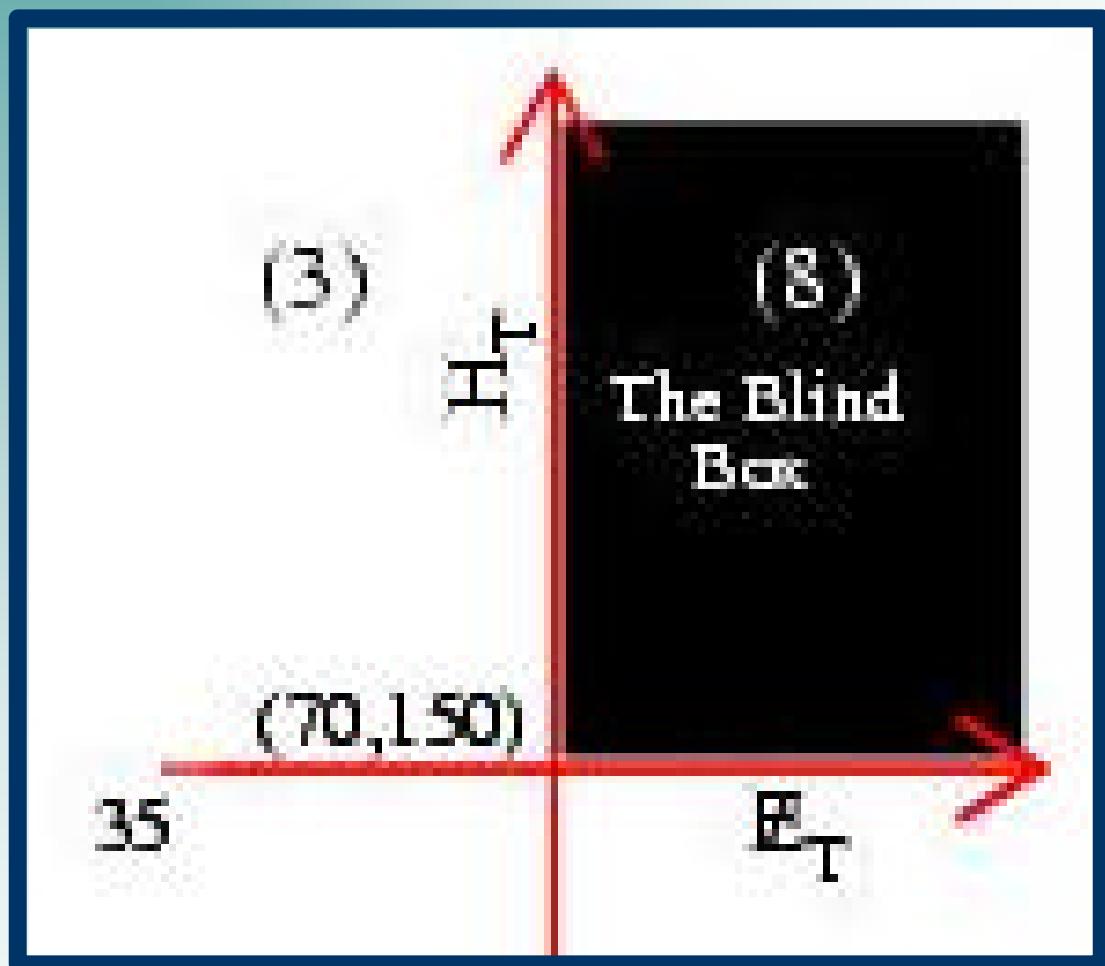
# "The other BOXes"

CDF PRELIMINARY  $\text{JLdt}=84 \text{ pb}^{-1}$   $\sqrt{s}=1.8 \text{ TeV}$   
SUSY-AD. SM Prediction=32.7, Data=31



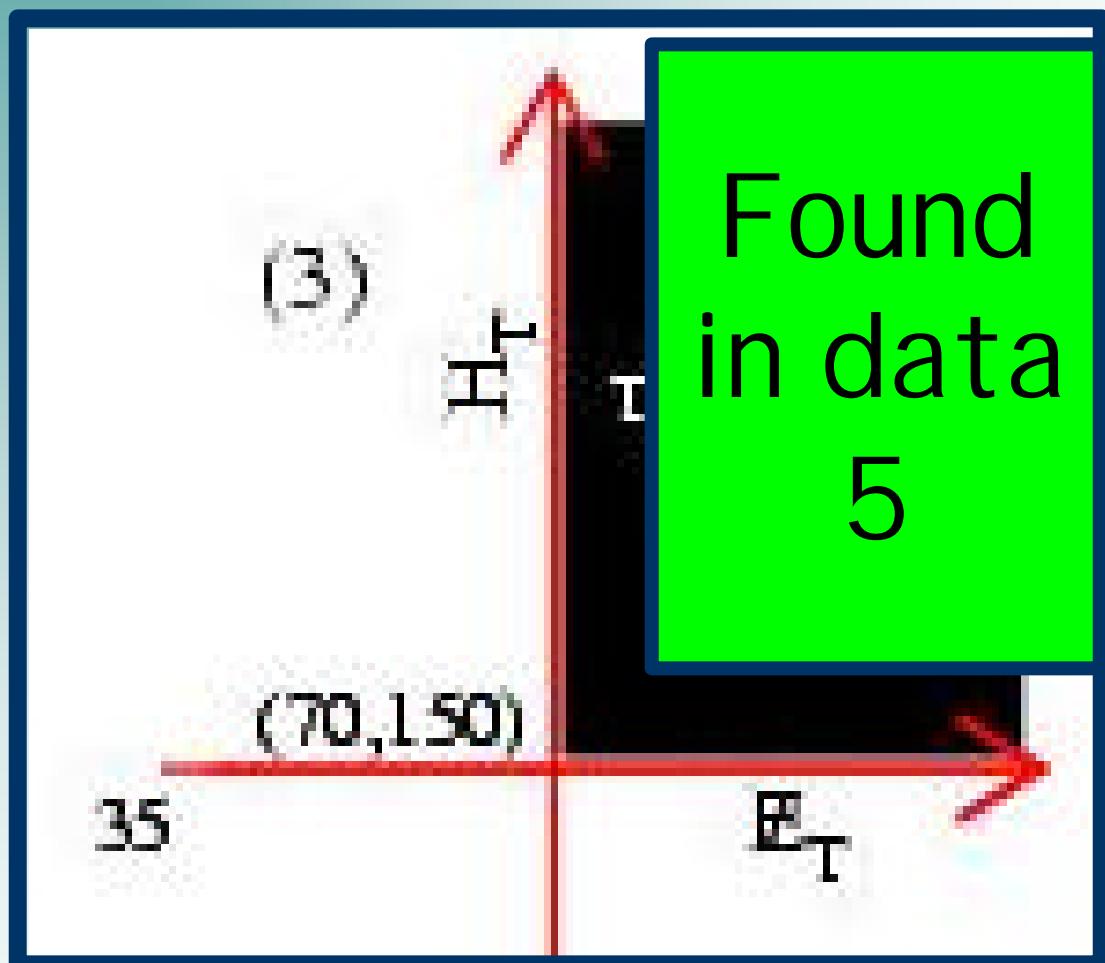
# "The other BOXes"

SUSY box B  
SM Expected 3.7  0.5



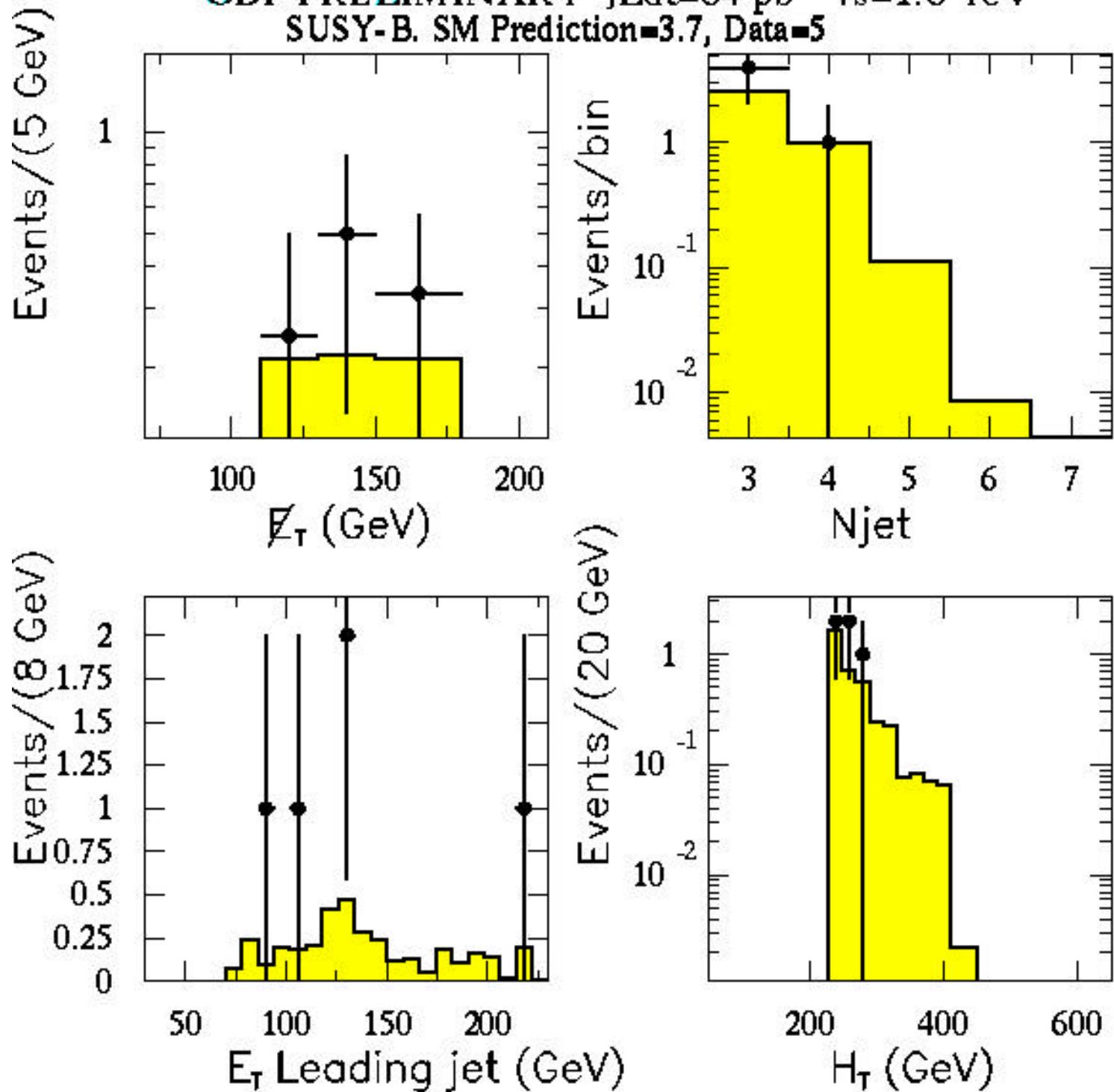
# “The other BOXes”

SUSY box B  
SM Expected 3.7  0.5



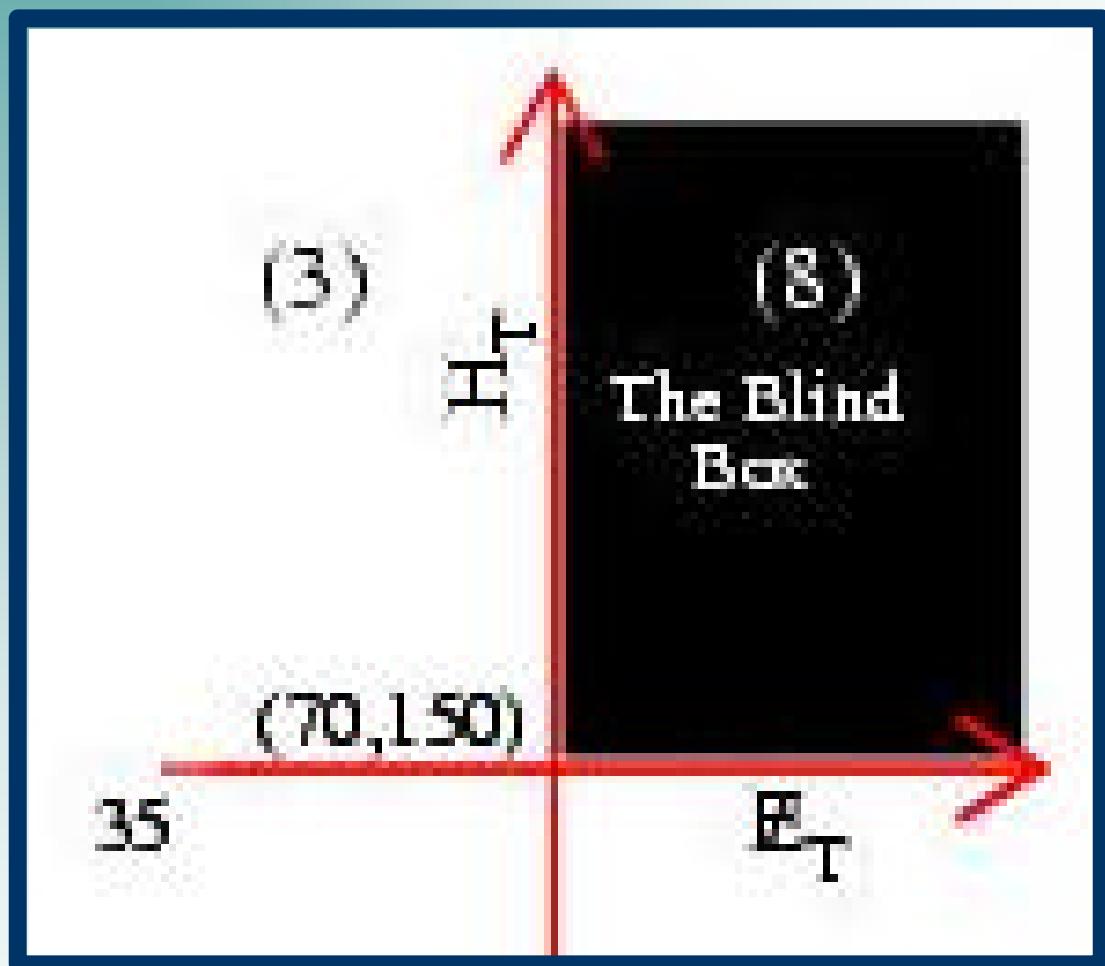
# "The other BOXes"

CDF PRELIMINARY  $\int L dt = 84 \text{ pb}^{-1}$   $\sqrt{s} = 1.8 \text{ TeV}$   
SUSY-B. SM Prediction = 3.7, Data = 5



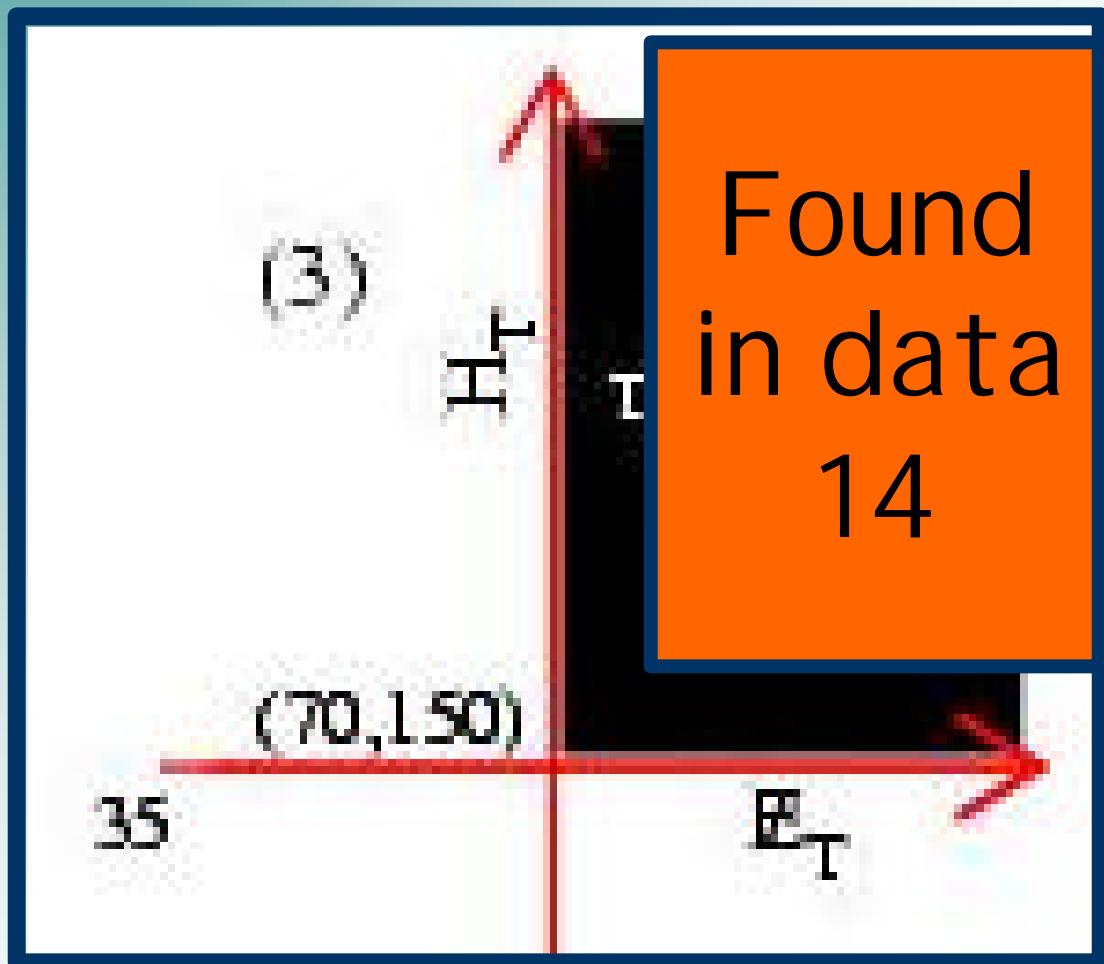
# "The other BOXes"

SUSY box C:  
SM Expected 10.6✓1



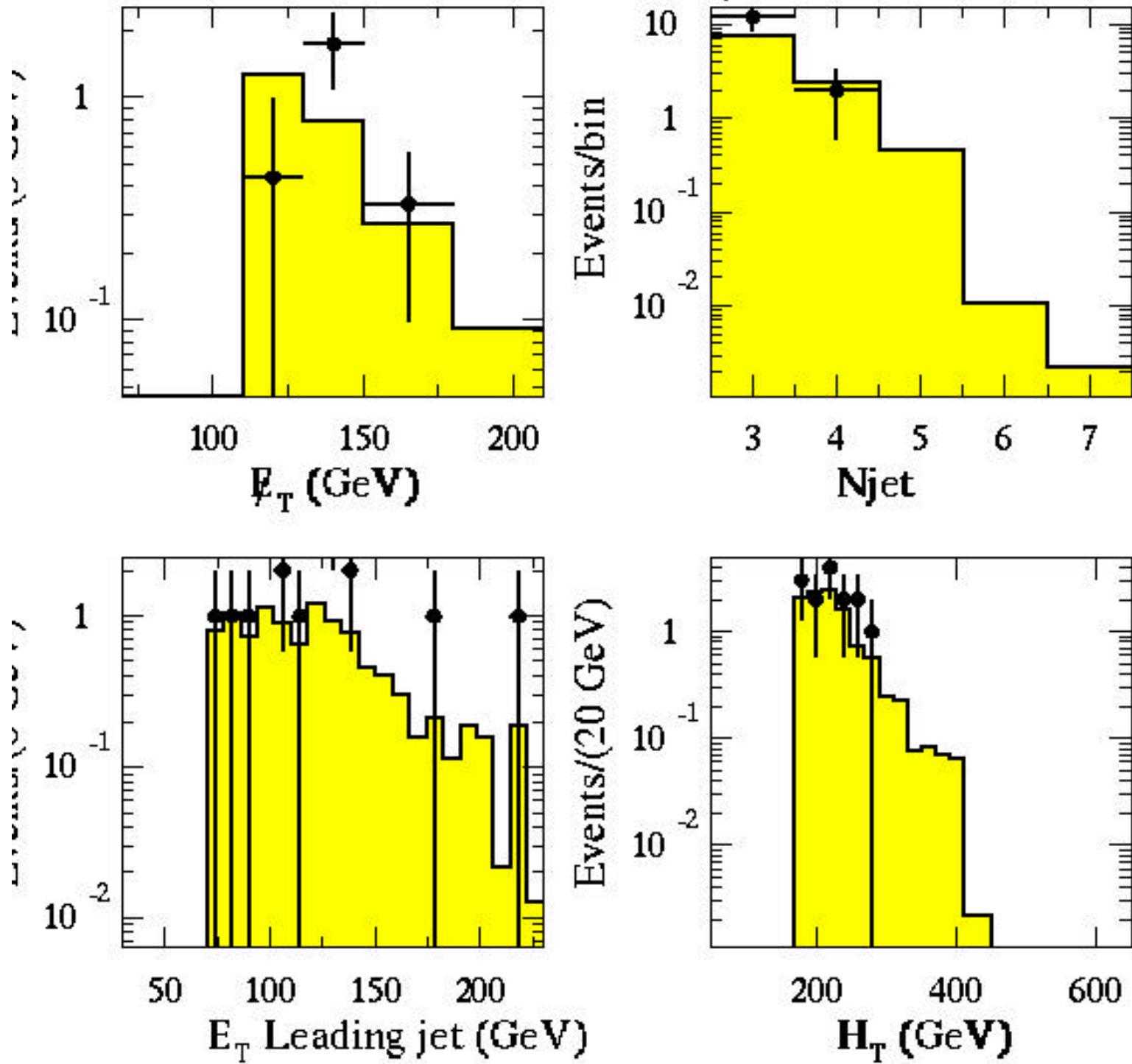
# “The other BOXes”

SUSY box C:  
SM Expected 10.6  1



# "The other BOXes"

CDF PRELIMINARY  $\int L dt = 84 \text{ pb}^{-1}$   $\sqrt{s} = 1.8 \text{ TeV}$   
SUSY-C. SM Prediction = 10.6, Data = 14



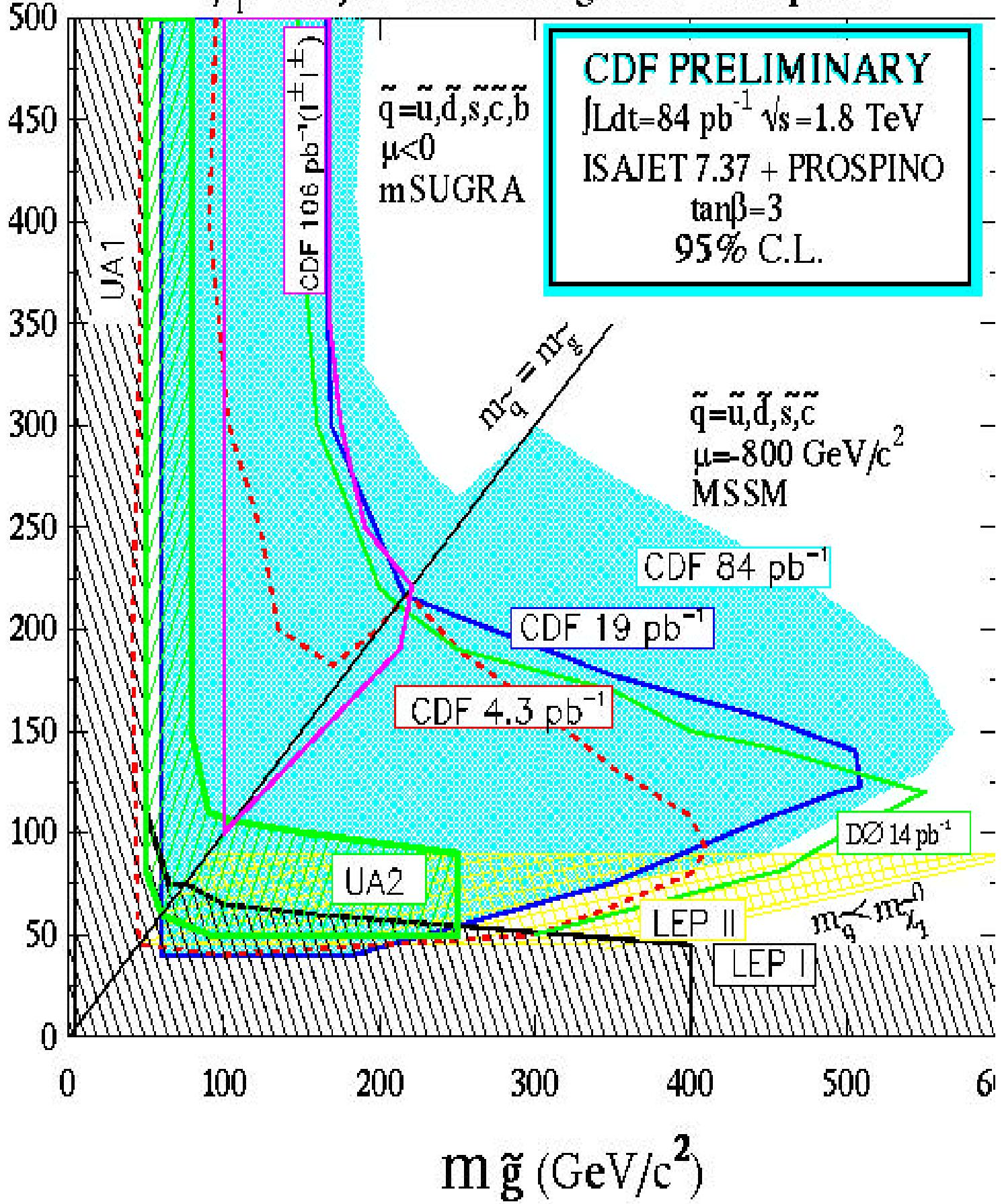
Box	MET,HT	Expected	Observed	$N_{95\% C.L.}$
A	90,160	$32.7 \pm 6.7$	31	17.7
B	110,230	$3.7 \pm 0.5$	5	7.4
C	110,170	$10.6 \pm 1$	14	11.9
D	90,160	$32.7 \pm 6.7$	31	17.3

## % Overall Relative Uncertainty on Signal Acceptance

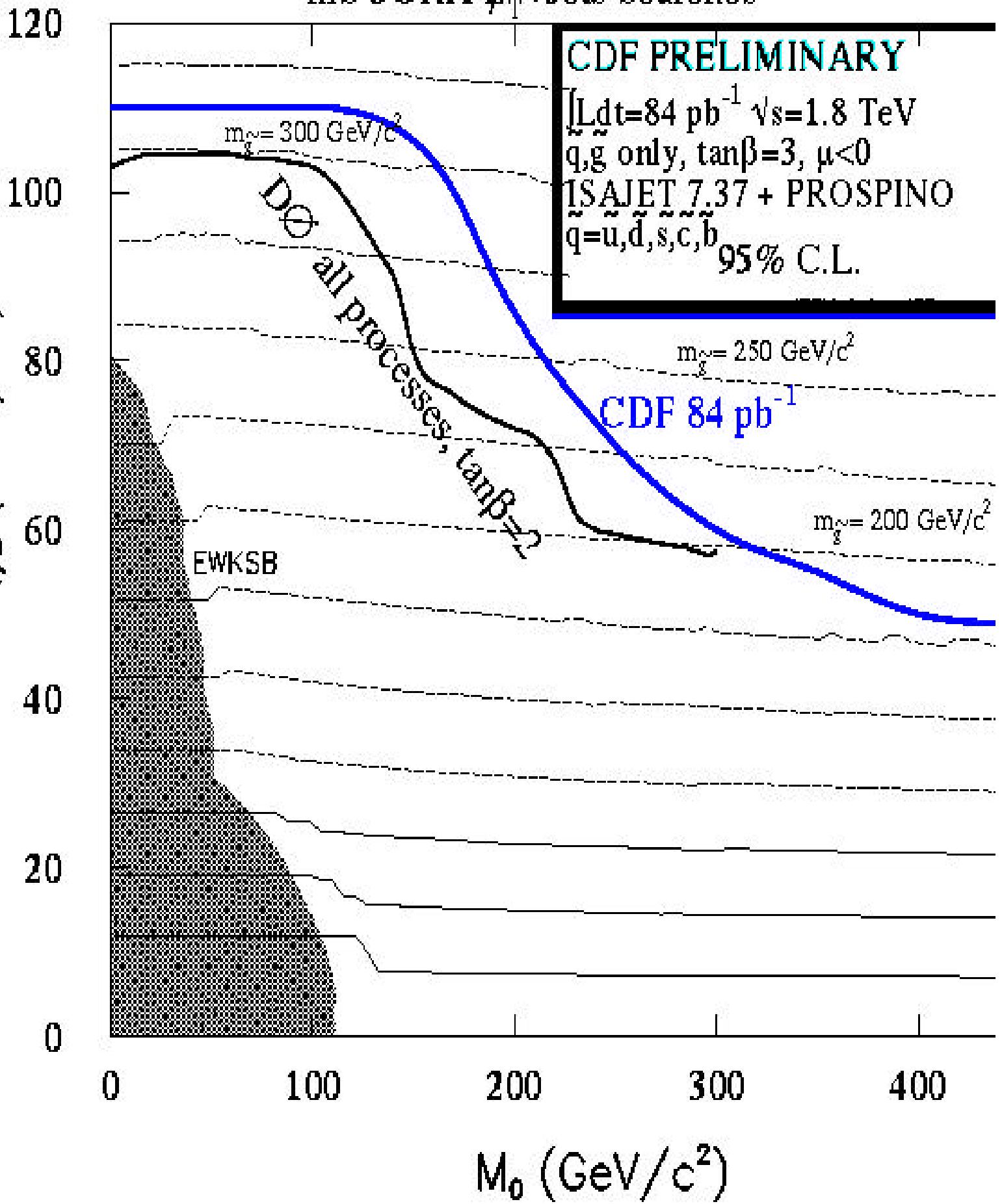
ind	a16	a14	b13	b4	d18	d6
% <PDFs >	6.5	3.5	5.5	4	3	5
% max(Radiation)	12.5	6	3	4	3	3
% max( $Q^2$ )	6.5	6.5	5.5	5.5	4	9
% <JET>	4.5	3.5	6	6	3	4
% Trigger				2		
% MC stat.				<0.2		

	A	B	C	D
$\sigma_A \%$	15	11	11	10

# $E_T + \geq 3$ jets search for gluinos and squarks



# mSUGRA $\mathbb{E}_T$ +Jets Searches



- or  $m_{\tilde{q}} \approx m_{\tilde{g}}$   $m < 300$  GeV/c<sup>2</sup>
- or  $m_{\tilde{q}} \ll m_{\tilde{g}}$   $m_{\tilde{g}} < 570$  GeV/c<sup>2</sup>
- or  $m_{\tilde{q}} \gg m_{\tilde{g}}$   $m_{\tilde{g}} < 195$  GeV/c<sup>2</sup>

## phenomenological Implications/Discussion

If the sparticles are too heavy then SUSY requires fine tuning and the hierarchy problem reappears. How much fine tuning is tolerable determines how probable low energy supersymmetry is and how soon it will be discovered.

It has been recently pointed out (Bastero-Gil et al./ Dimopoulos et al.) that the electroweak scale looks more natural if  $M_3$  is relatively small.

## phenomenological Implications/Discussion

$$= -1.7\mu^2 + 7.2M_3^2 - 0.24M_2^2 + 0.014M_1^2 +$$

The required cancellation is easier if the gluino mass is not so big.

$$M_3 \geq 300 \rightarrow \frac{7.2M_3^2}{M_Z^2} \geq 80$$

with gaugino mass unification

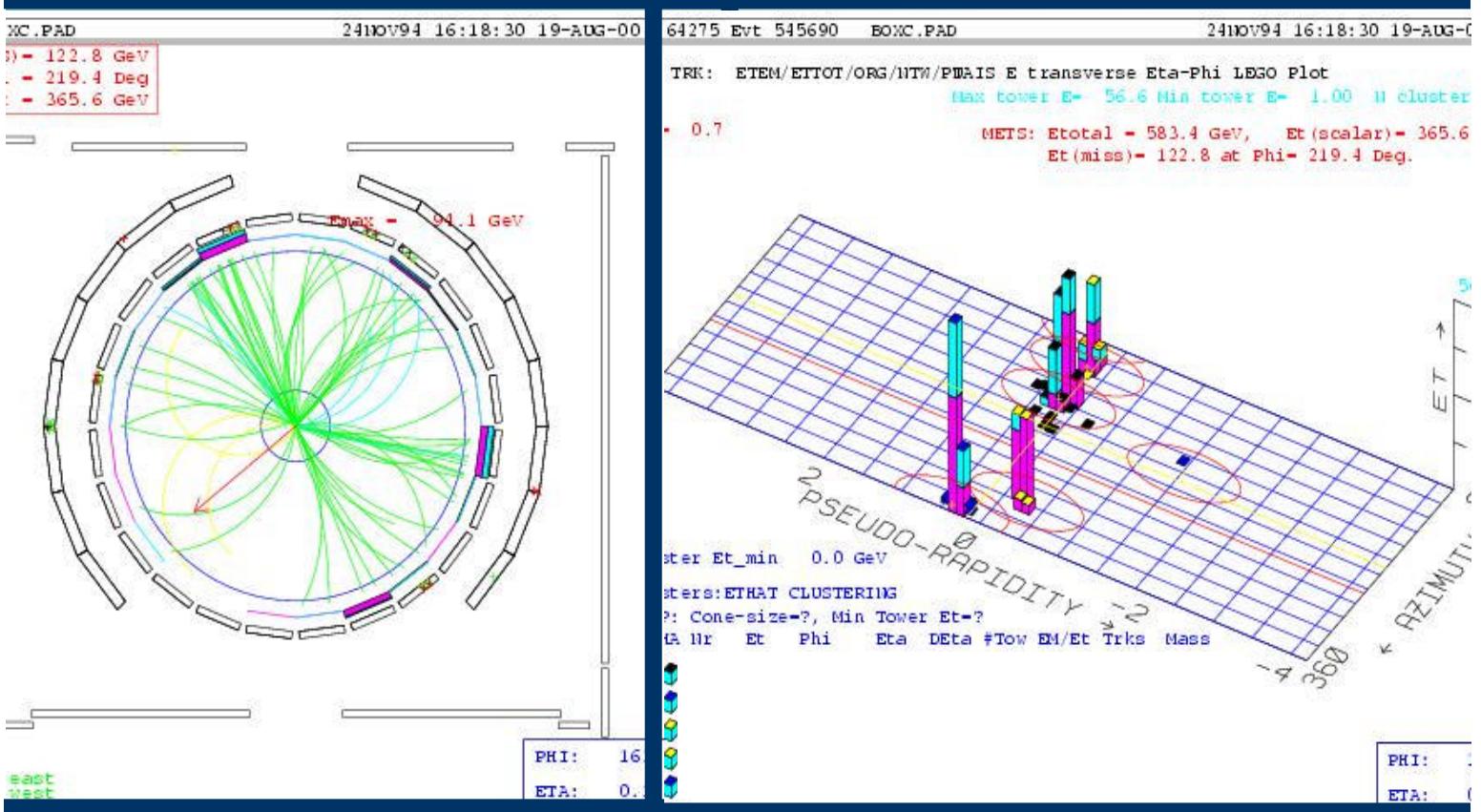
$M_1:M_2:M_3::0.5:1:3$ .

The result of this analysis as well as the LEP result on the chargino  $M_2 < 90$  GeV make it interesting to drop gaugino unification and allow lower gluino mass.

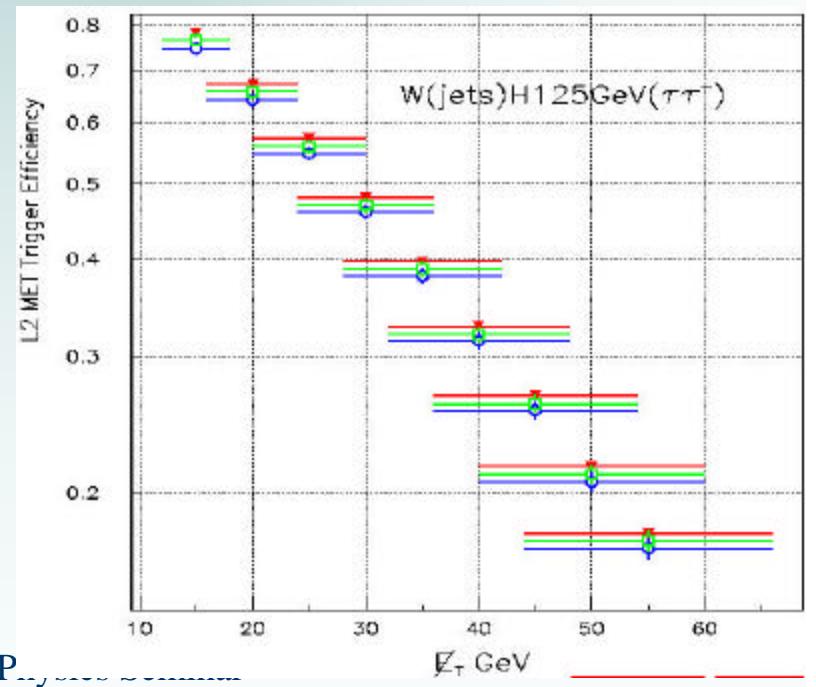
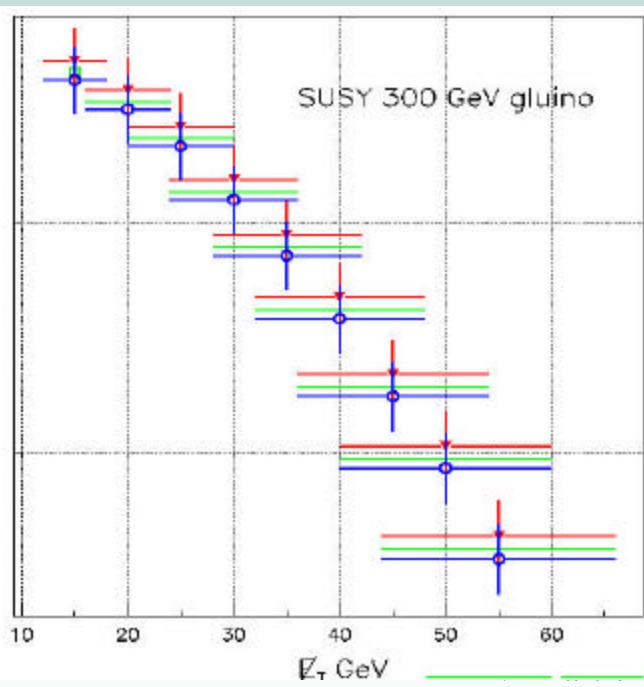
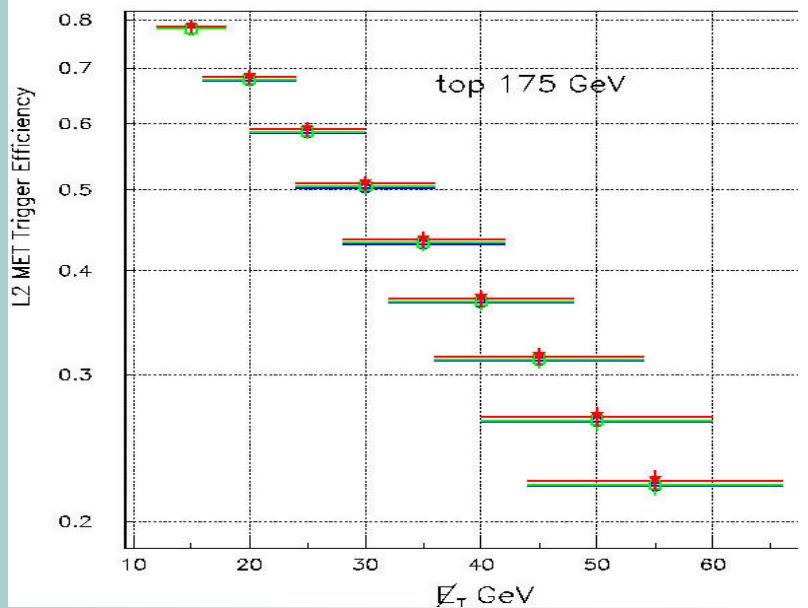
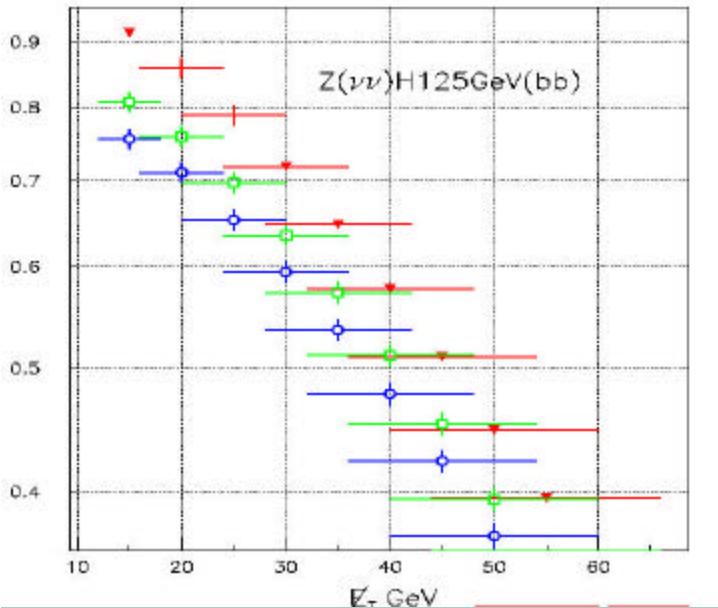
# phenomenological Implications/Discussion

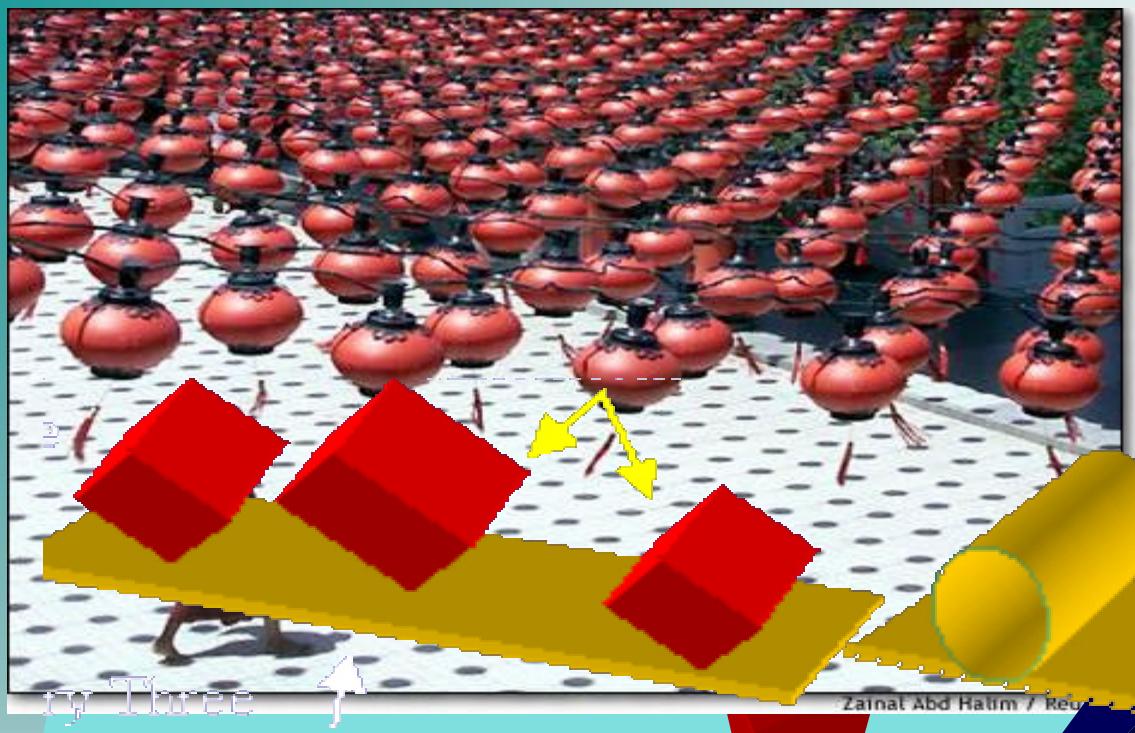
If low energy supersymmetry exists and given that the amount of fine tuning depends critically on the gluino mass, this result indicates that RUNII and the missing energy + jets channel (with lepton veto) constitute a very good probe and have discovery potential.

# Candidate Event



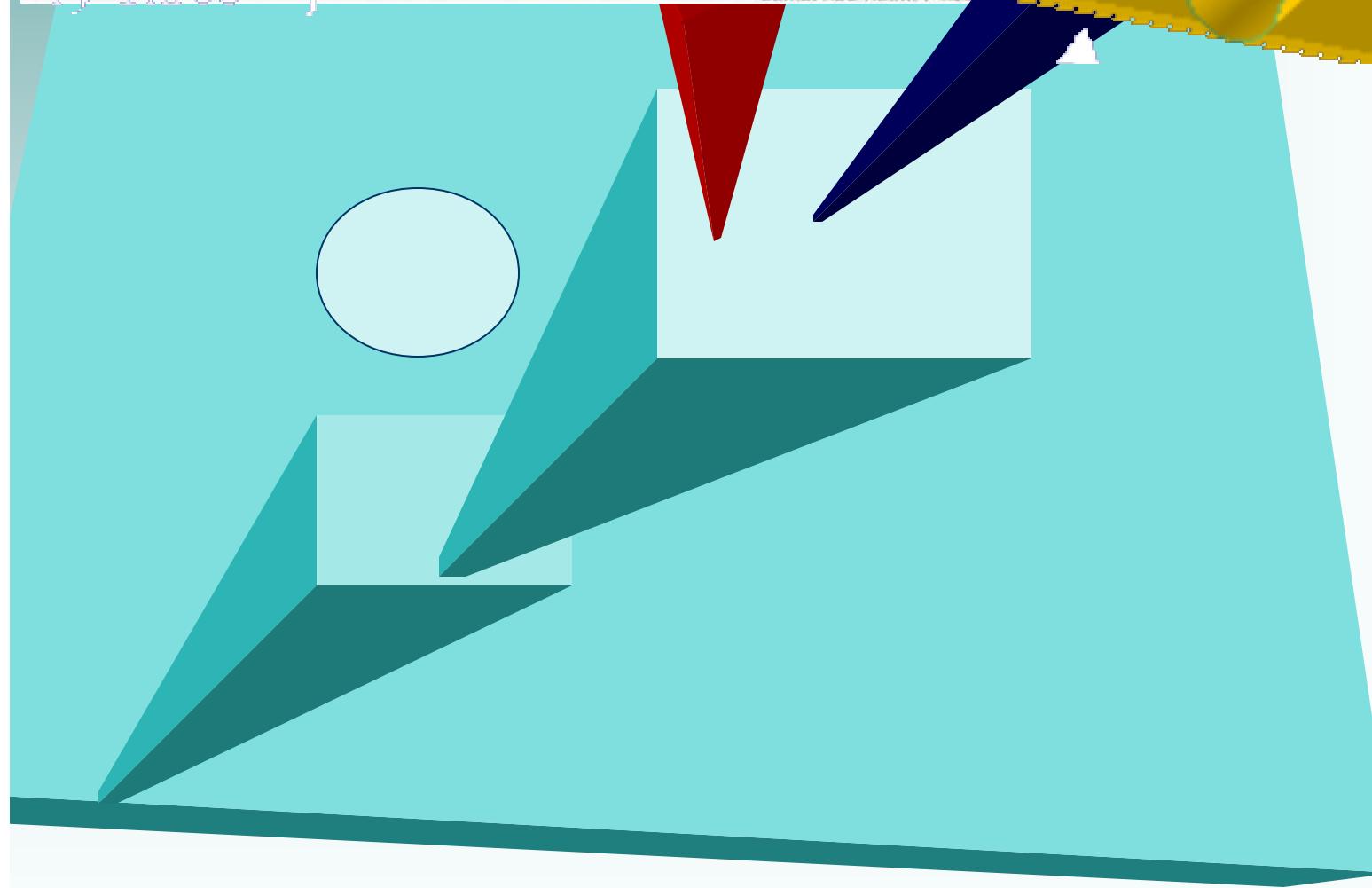
# DF L2 MET trigger for RUNII





My Three

Zainal Abd Halim / Reut



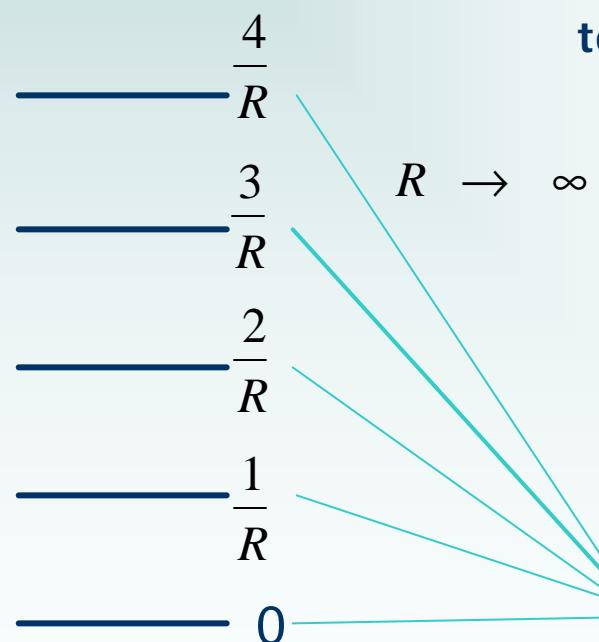
# Kaluza-Klein modes

If a spatial dimension is periodic then the momentum in that dimension quantized:

$$p = \frac{n}{R}$$

From our dimensions of view the KK modes get mass:

$$p^2 = m_0^2 + \frac{n^2}{R^2}$$



KK momentum  
tower of states

# Gauss's Law

If the  $d$  extra dimensions are compactified down to size  $R$ , then Gauss's Law

$$V(r) \sim \frac{1}{M_{Pl(4+d)}^{d+2}} \frac{m_1 m_2}{r^{d+1}} \quad r \ll R$$

$$V(r) \sim \frac{1}{M_{Pl(4+d)}^{d+2}} \frac{m_1 m_2}{R^d} \frac{1}{r} \quad r \gg R$$

$$M_{Planck}^2 \sim R^d M_{Pl(4+d)}^{2+d}$$

The Planck Scale  
from our dimension  
of view,  $10^{19}$  GeV

↑ 4+ $\delta$  Planck Scale  
 $M_s$   
 $M_D$   
 $M_*$

any scale that in the  
higher dimensional theor  
is taken  $O(\text{TeV})$

The size of the extra dimension  
Set the higher dimensional Planck scale to  $m_{EWK}$   
the Planck scale to  $10^{19} \text{ GeV}$   
then

$$R \sim 2 \cdot 10^{\frac{31}{d}-17} \text{ cm}$$

$$= 1 \quad \Rightarrow \quad R \sim 10^9 \text{ Km}$$

No way

$$= 2 \quad \Rightarrow \quad R \sim 1 \text{ mm}$$

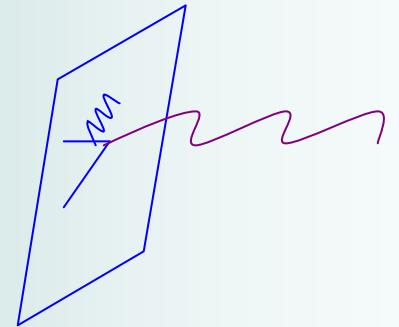
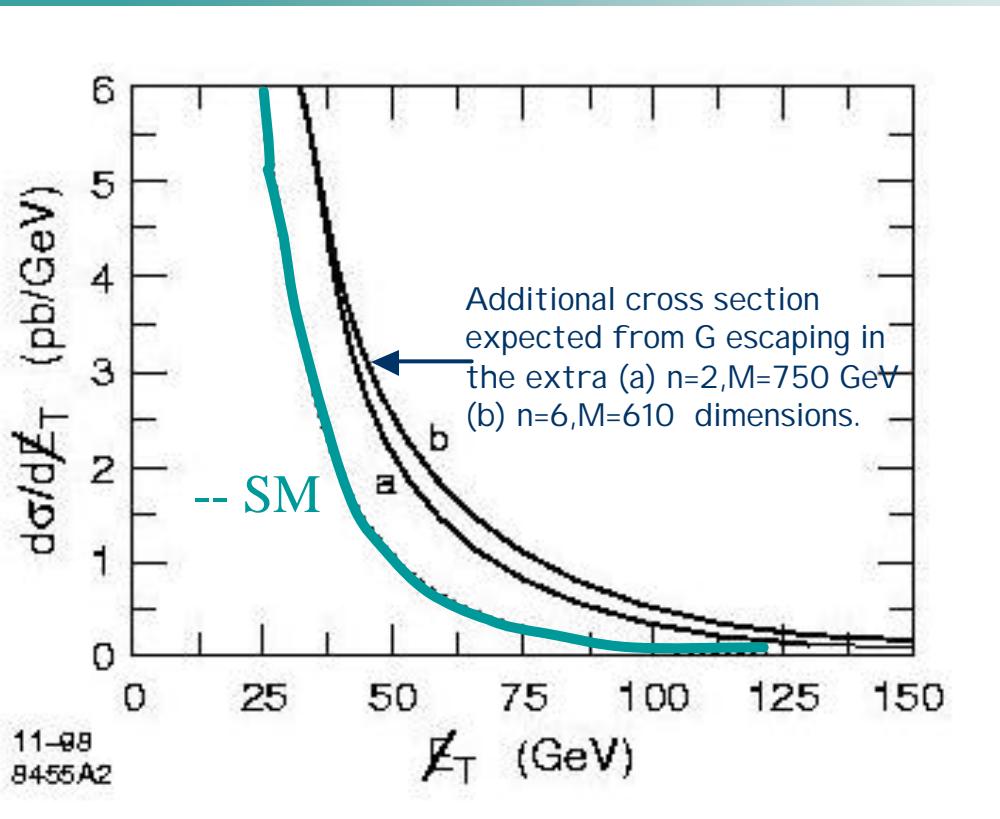
Explore in sub-mm  
gravitational  
experiments/collider...

$$= 3 \quad \Rightarrow \quad R \sim 1 \text{ nm}$$

$$= 6,7 \quad \Rightarrow \quad R \sim 10^{-17} \text{ fm}$$

M-theory limits

# Monojets+Missing Energy



The monojet+Missing Energy result from CDF 88-89 can put the following constraints :

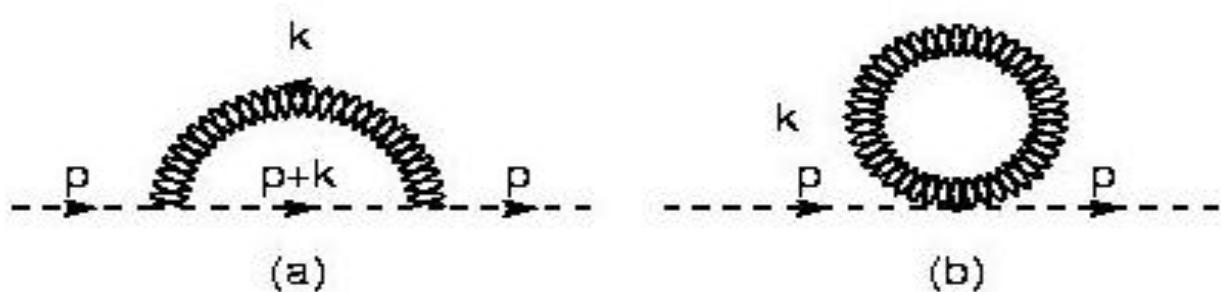
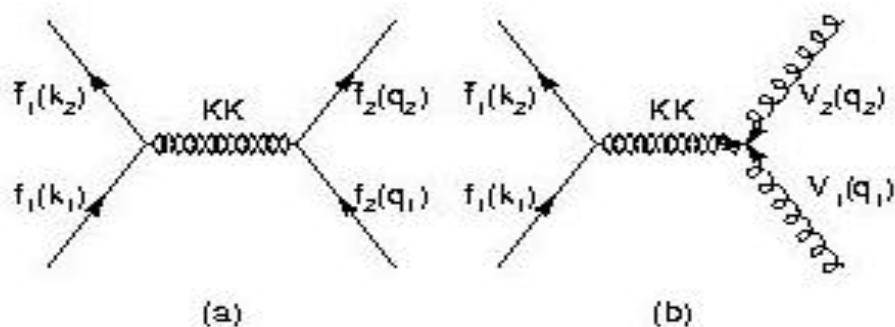
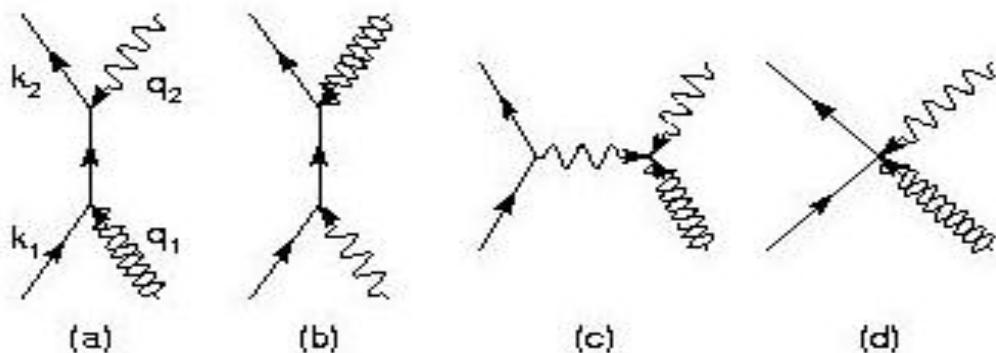
a. $n=2, M=750 \text{ GeV}$	$R < 0.11 \text{ cm}$	$M > 750 \text{ GeV}$
b. $n=6, M=610 \text{ GeV}$	$R < 5.8 \times 10^{-12}$	$M > 610 \text{ GeV}$

An observation of an excess of Missing Energy events above the SM expectation can provide a direct evidence for this class of models.

# The extra world picture

- The SM is confined on a 4d wall
- Gravity exists in a 4+d “bulk”
- Gravity feels weak on the wall because of the enormity of the bulk volume
- Each KK-graviton state couples to the wall with Planck suppressed strength
- The number of KK-states  $\sim (ER)^\delta$
- The sum over all KK-states is not  $M_{Pl}$  suppressed but  $M_{Pl(4+\delta)}$  suppressed i.e.  $M_{EWK}$  suppressed so we have sizable cross sections

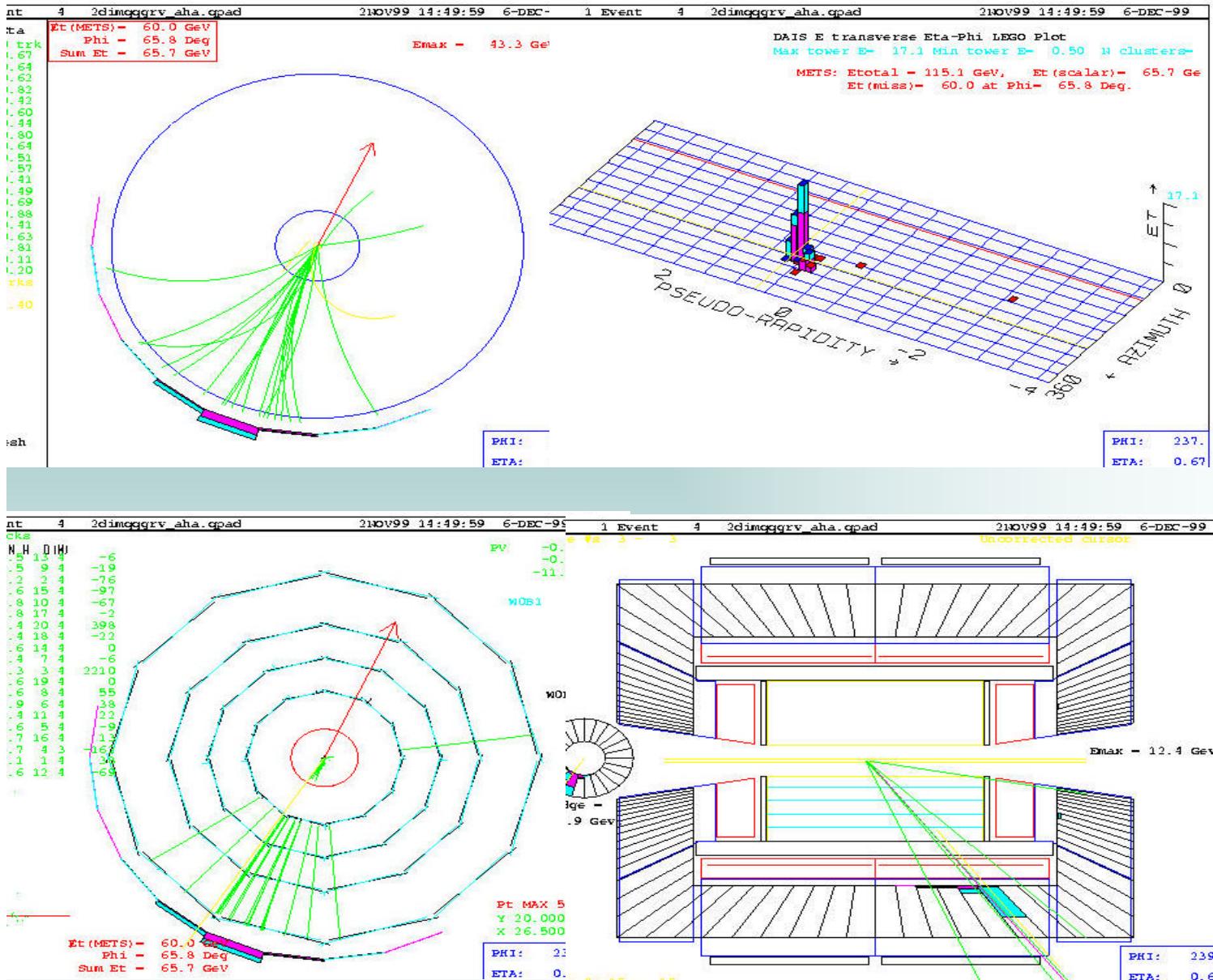
# Graviton emission/exchange



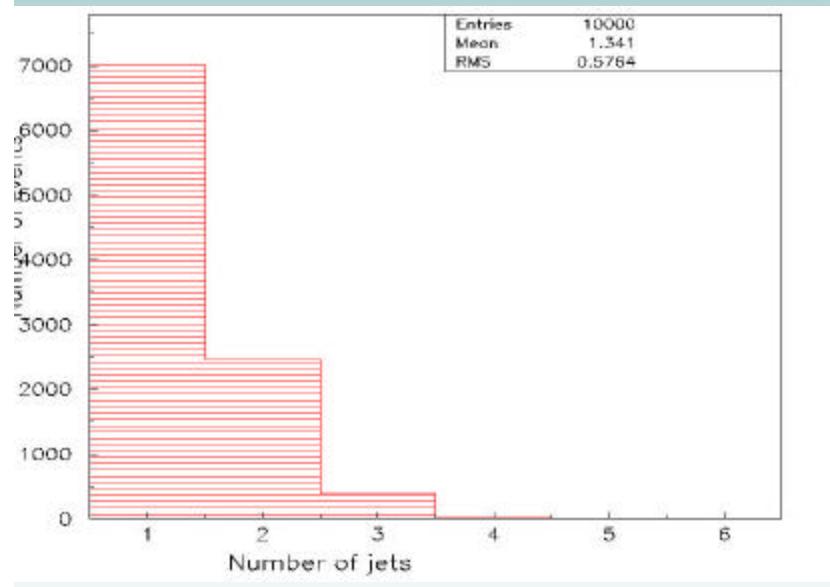
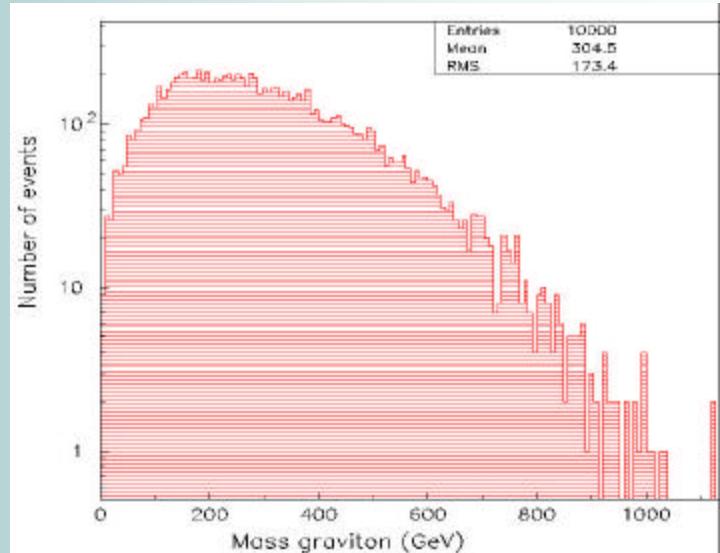
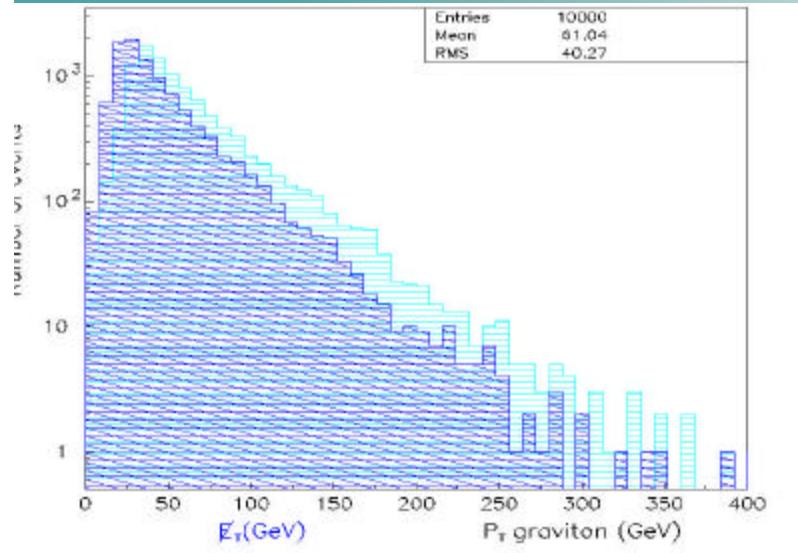
T. Han, J. Lykken, R-J Zhang, hep-ph/0811350

# Graviton @CDF

N=2 M=1TeV

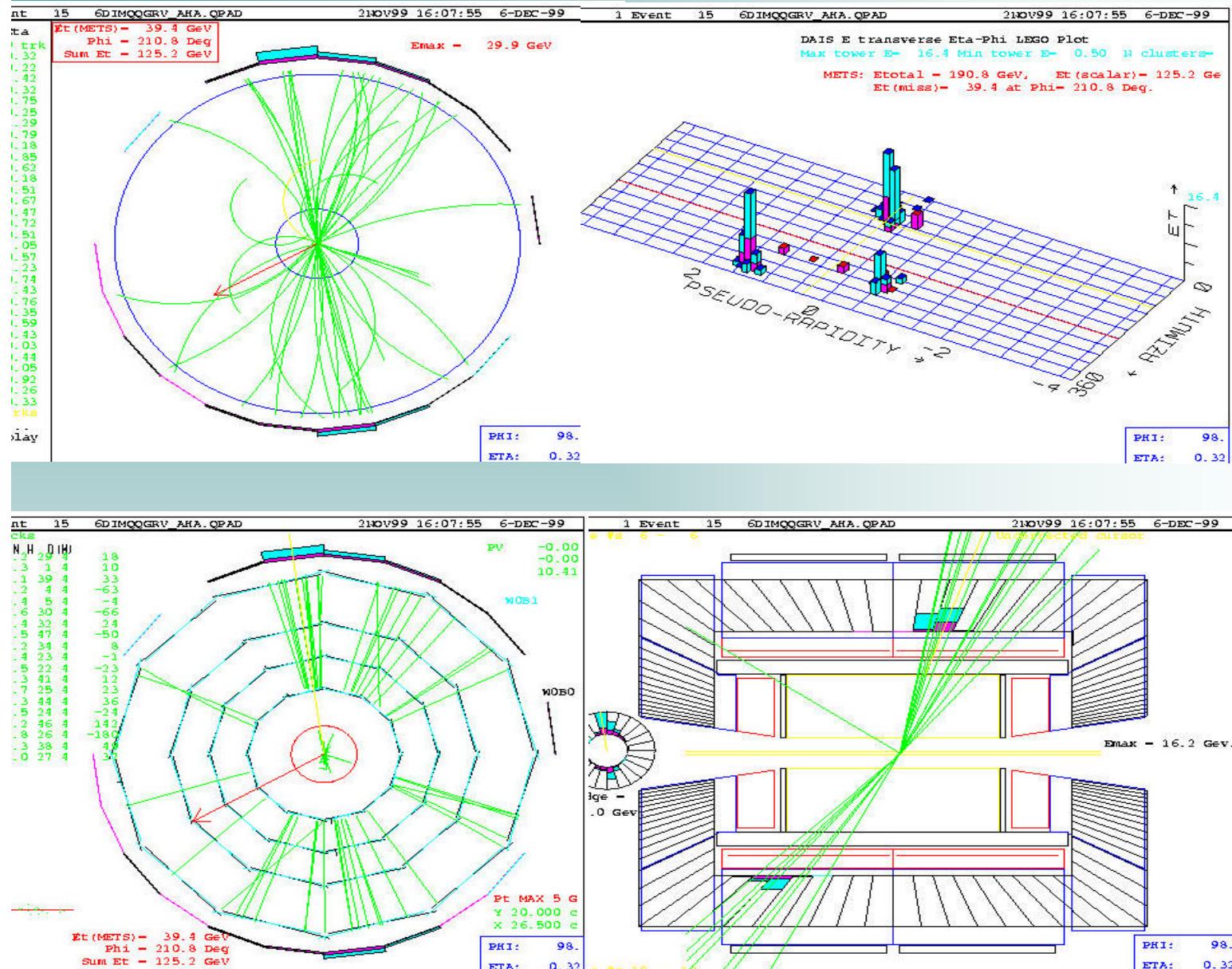


# J=2, M=1TeV



Only qqbar->g G  
(PYTHIA 6.115 +  
graviton process)

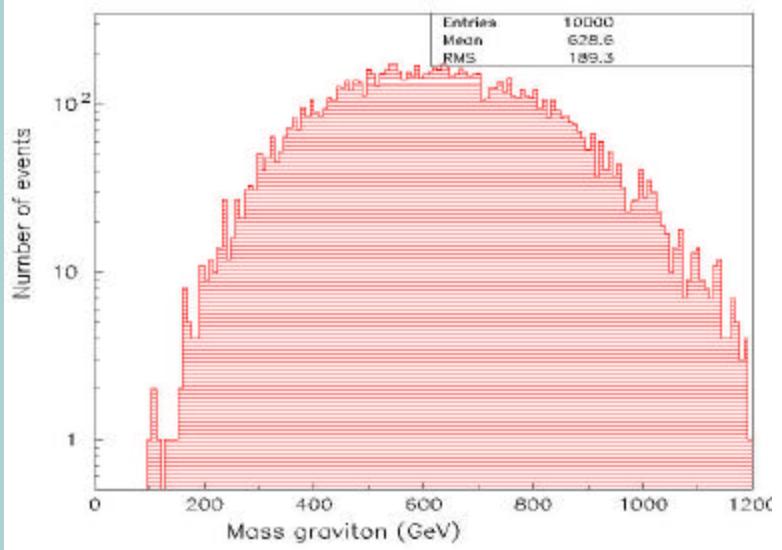
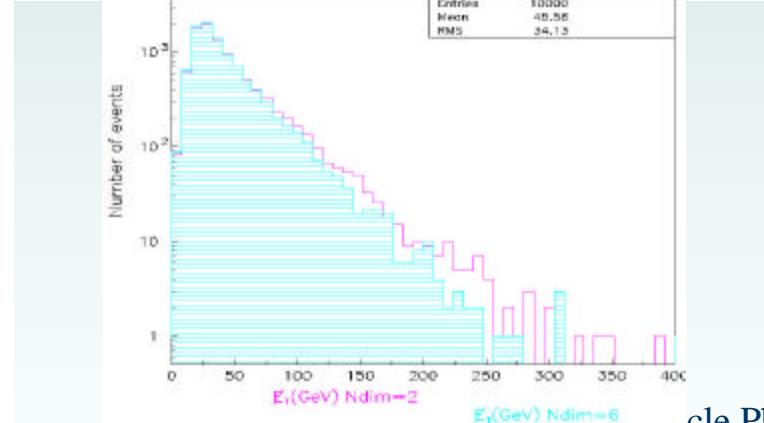
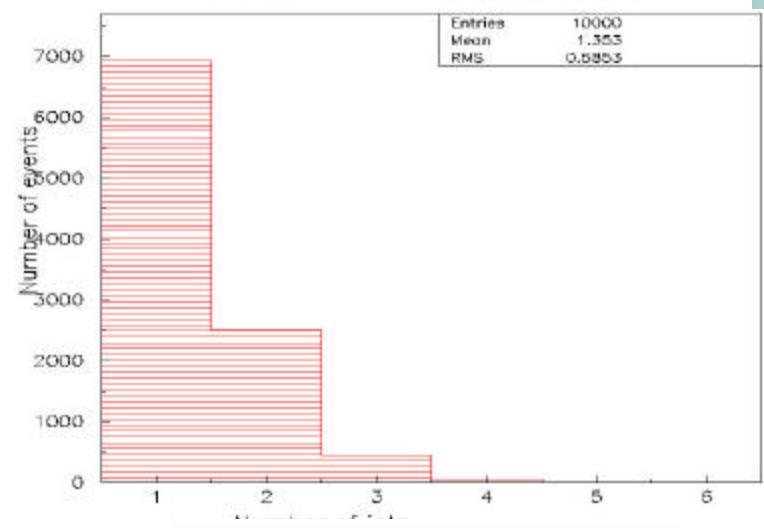
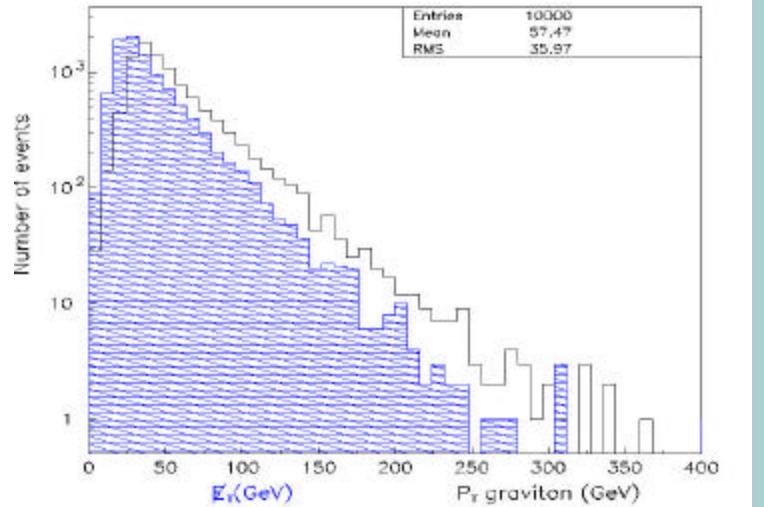
# GRAVITON @CDF



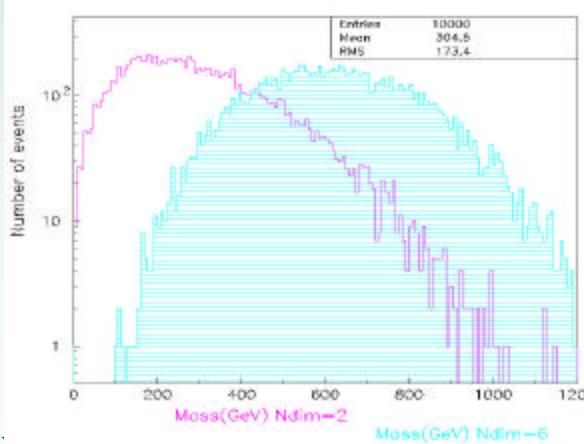
N=6 M=1TeV

BNL Particle Physics Seminar

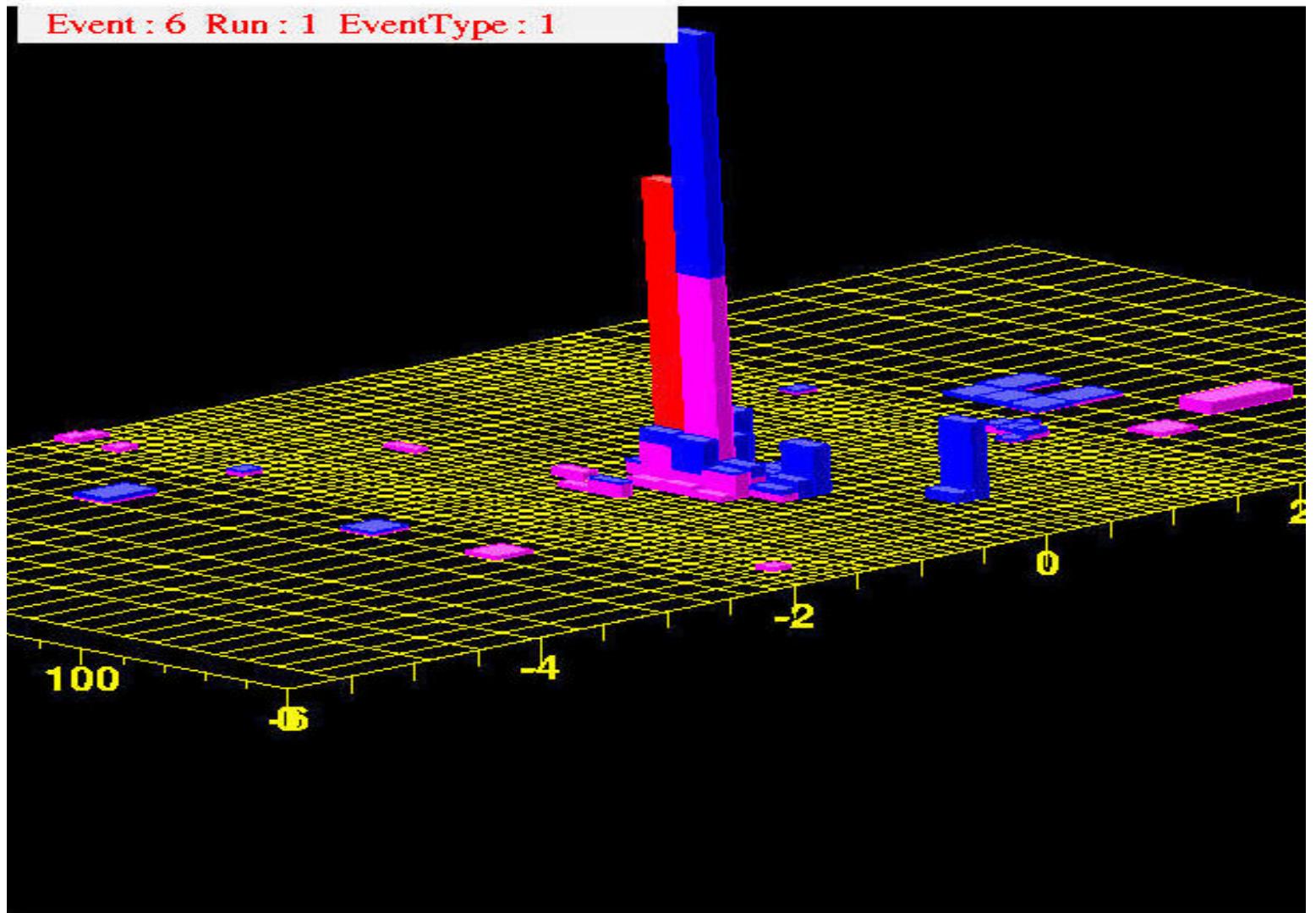
# J=6 , M=1TeV



Only qqbar->g G  
(PYTHIA 6.115 +  
gravion process)

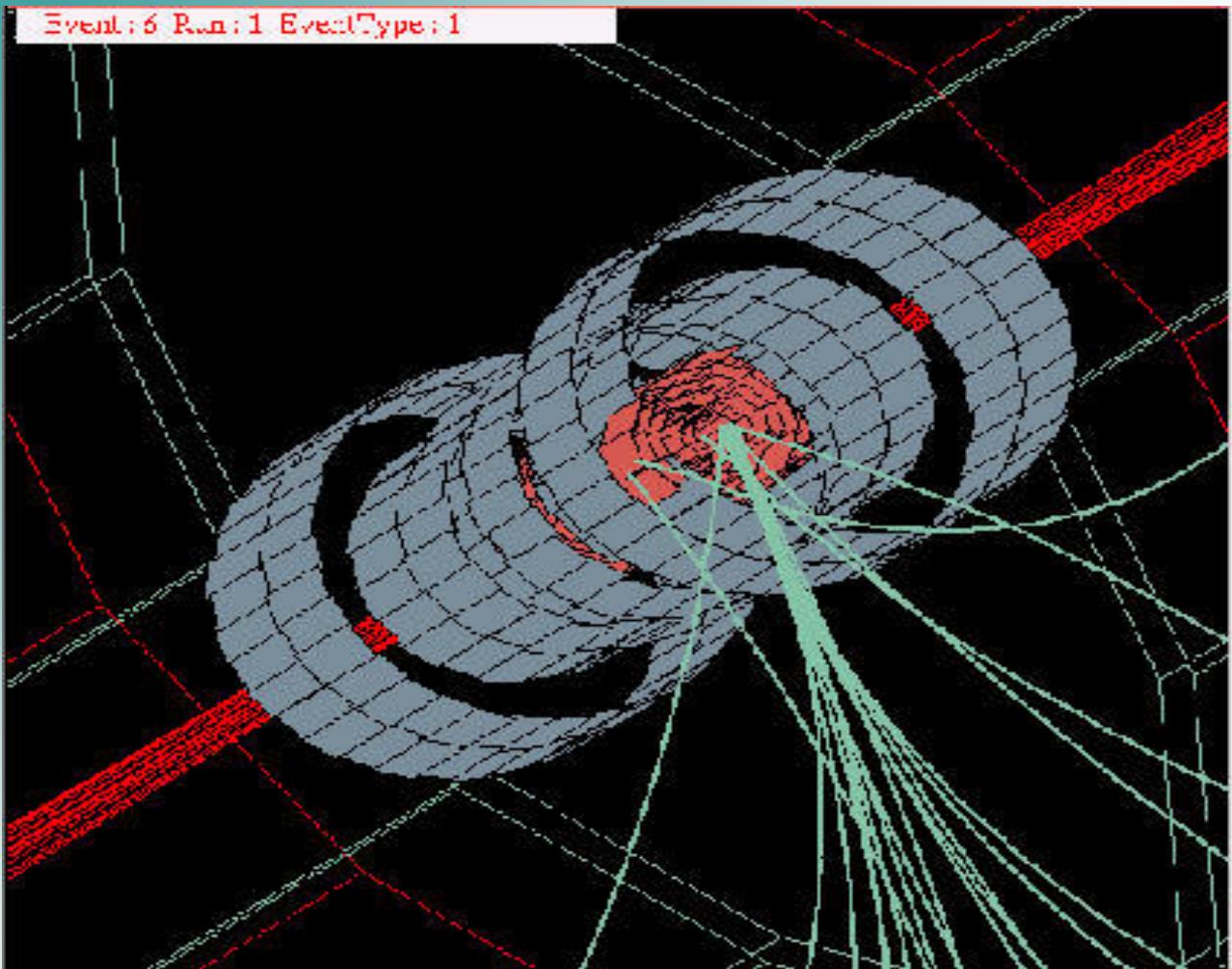


# RUNI I Display



Only qbar->g G (PYTHIA 6.115 + graviton process),  $\delta=6$ ,  $M=1\text{TeV}$ ,  $\sqrt{s}=2\text{TeV}$ , GEANT CDF preliminary  
RUNI I simulation and display

# RUNI I Display



Only qbar->g G (PYTHIA 6.115 + graviton process),  $\delta=6$ ,  $M=1\text{TeV}$ ,  $\sqrt{s}=2\text{TeV}$ , GEANT CDF  
preliminary  
BNL Particle Physics Seminar  
RUNI I simulation and display